Marking Scheme <u>CLASS: XII</u> Session: 2021-22				
Mathematics (Code-041)				
lerm - 2				
	<u>SECTION – A</u>			
1	Finds (logx			
	Find: $\int \frac{1}{(1+\log x)^2} dx$	4/2		
	Solution: $\int \frac{1}{(1+\log x)^2} dx = \int \frac{1}{(1+\log x)^2} dx = \int \frac{1}{1+\log x} dx - \int \frac{1}{(1+\log x)^2} dx$	1/2		
	$=\frac{1}{1+\log x} \times x - \int \frac{1}{(1+\log x)^2} \times \frac{1}{x} \times x dx - \int \frac{1}{(1+\log x)^2} dx = \frac{1}{1+\log x} + c$ OR	1+1/2		
	Find: $\int \frac{\sin 2x}{\sqrt{9-\cos^4 x}} dx$			
	Solution: Put $cos^2 x = t \Rightarrow -2cosxsinxdx = dt \Rightarrow sin2xdx = -dt$	1		
	The given integral $= -\int \frac{dt}{\sqrt{3^2 - t^2}} = -\sin^{-1}\frac{t}{3} + c = -\sin^{-1}\frac{\cos^2 x}{3} + c$	1		
2.	Write the sum of the order and the degree of the following differential $d \begin{pmatrix} dy \end{pmatrix} = \pi$			
	equation: $\frac{1}{dx}\left(\frac{1}{dx}\right) = 5$			
	Solution: Order = 2	1		
	Degree = 1 Sum = 3	1/2		
		/2		
3.	If \hat{a} and \hat{b} are unit vectors, then prove that			
	$ \hat{a} + \hat{b} = 2\cos\frac{\theta}{2}$, where θ is the angle between them.			
	Solution: $(\hat{a} + \hat{b}) \cdot (\hat{a} + \hat{b}) = \hat{a} ^2 + \hat{b} ^2 + 2(\hat{a}, \hat{b})$	1		
	$\left \hat{a} + \hat{b}\right ^2 = 1 + 1 + 2\cos\theta$			
	$=2(1+\cos\theta)=4\cos^2\frac{\theta}{2}$	1/2		
	$ \hat{a} + \hat{b} = 2\cos\frac{\theta}{\pi}$	1/2		
4.	Find the direction cosines of the following line: 3 - r = 2y - 1 = z			
	$\frac{3-x}{-1} = \frac{2y-1}{2} = \frac{2}{4}$			
	Solution: The given line is			
	$\left \frac{x-3}{1} = \frac{y-\overline{2}}{1} = \frac{z}{4} \right $	1		
	Its direction ratios are <1, 1, 4>	1/2		
	1 1 1 4	1/		
	$\left(\frac{1}{3\sqrt{2}}, \frac{1}{3\sqrt{2}}, \frac{1}{3\sqrt{2}}\right)$	/2		

5.	A bag contains 1 red and 3 white balls. Find the probability distribution of the number of red balls if 2 balls are drawn at random from the bag one-by-one without replacement.			
	Solution: Let X be the random variable defined as the number of red balls. Then X = 0, 1 $P(X=0) = {}^{3} \times {}^{2} = {}^{6} = {}^{1}$			1/2 1/2
	$P(X=0) = \frac{1}{4} \times \frac{1}{3} = \frac{1}{12} = \frac{1}{2}$ $P(X=1) = \frac{1}{4} \times \frac{3}{3} + \frac{3}{4} \times \frac{1}{4} = \frac{6}{4}$	$-\frac{1}{2}$		172
	$P(X=1) = \frac{1}{4} \times \frac{1}{3} + \frac{1}{4} \times \frac{1}{3} = \frac{1}{12} = \frac{1}{2}$ Probability Distribution Table:			1/2
	X	0	1	
	P(X)	$\frac{1}{2}$	$\frac{1}{2}$	1/2
 6	Two cords are drawn at r	andom from a pools of EQ.	arda ana hy ana without	
6.	replacement. What is the probability of getting first card red and second card Jack?			
	Solution: The required probability = $P((The first is a red jack card and The second is a jack card) or (The first is a red non-jack card and The second is a jack card))$			1
	$=\frac{2}{52} \times \frac{3}{51} + \frac{24}{52} \times \frac{4}{51} = \frac{1}{26}$			1
		SECTION – B		I
 7.	Find: $\int \frac{x+1}{(x^2+1)^2} dx$			
	Solution: Let $\frac{x+1}{x+1} = \frac{Ax+B}{x+1} + \frac{C}{x+1} = \frac{(Ax+B)x+C(x^2+1)}{x+1}$		1/2	
$\Rightarrow x + 1 = (Ax + B)x + C(x^{2} + 1) $ (An identity)				., 2
	Equating the coefficients,	we get		
	B = 1, C = 1, A + C = 0 Hence, $A = -1, B = 1, C = 1$			1/2
	The given integral = $\int \frac{-x+1}{x^2+1} dx + \int \frac{1}{x} dx$			
	$= \frac{-1}{2} \int \frac{2x-2}{x} dx + \int \frac{1}{2} dx$			1/2
	$\begin{bmatrix} -\frac{1}{2} \int \frac{1}{x^2 + 1} dx + \int \frac{1}{x} dx \\ -1 \int \frac{1}{2x} dx + \int \frac{1}{x} dx \end{bmatrix}$			
	$= \frac{1}{2} \int \frac{1}{x^2 + 1} dx + \int \frac{1}{x^2 - 1} dx$	$\frac{1}{x}dx + \int \frac{1}{x}dx$		
	$= \frac{-1}{2}\log(x^2 + 1) + \tan^{-1}x + \log x + c$			1+1/2
	-			
8.	Find the general solution	of the following differentia	l equation:	
	$x\frac{dy}{dx} = y - x\sin(\frac{y}{x})$			
	Solution: We have the differential equation:			
	$\frac{dy}{dx} = \frac{y}{x} - \sin(\frac{y}{x})$			
	The equation is a homoge	eneous differential equation	on.	1
Putting $y = vx \Rightarrow \frac{dy}{dx} = v + x \frac{dy}{dx}$ The differential equation becomes				
	$\frac{dv}{v + r - u - sinu}$			
$\begin{bmatrix} v & x & \frac{dx}{dx} & -v & \sin v \\ \frac{dy}{dx} & \frac{dx}{dx} & \frac{dx}{dx} \end{bmatrix}$				
	$\Rightarrow \frac{d}{sinv} = -\frac{d}{x} \Rightarrow cosecvd$	$v = -\frac{1}{x}$		1/2
	Integrating both sides, we get			

	log cosecv - cotv = -log x + logK, K > 0 (Here, $logK$ is an arbitrary	
	constant.)	1
	$\Rightarrow log (cosecv - cotv)x = logK$	
	$\Rightarrow (cosecv - cotv)x = K$ $\Rightarrow (cosecv - cotv)x = \pm K$	
	$\Rightarrow (cosecv - covv)x = \pm K$	1/2
	$\Rightarrow (cosec \frac{1}{x} - cot \frac{1}{x}) x = C$, which is the required general solution.	72
	OR	
	Find the particular solution of the following differential equation, given that y	
	= 0 when $x = \frac{\pi}{1}$:	
	$dy \qquad 2$	
	$\frac{d}{dx} + ycotx = \frac{1}{1 + sinx}$	
	Solution:	
	The differential equation is a linear differential equation	1
	$IF = e^{\int cotx dx} = e^{\log sinx} = sinx$	I
	The general solution is given by	
	$ysinx = \int 2\frac{sinx}{1+sinx}dx$	1/2
	$\int 1 + \sin x$ $\int \sin x + 1 - 1$ (1	
	$\Rightarrow ysinx = 2 \int \frac{1}{1 + sinx} dx = 2 \int [1 - \frac{1}{1 + sinx}] dx$	
	$\Rightarrow ysinx = 2 \int \left[1 - \frac{1}{\sqrt{\pi}}\right] dx$	
	$\int 1 + \cos\left(\frac{x}{2} - x\right)$	
	$\Rightarrow ysinx = 2 \int \left[1 - \frac{1}{2 - x}\right] dx$	
	$\int \frac{2\cos^2\left(\overline{4}-\overline{2}\right)}{1-\pi}$	
	$\Rightarrow ysinx = 2 \int \left[1 - \frac{1}{2}sec^2\left(\frac{\pi}{4} - \frac{x}{2}\right)\right]dx$	
	$\Rightarrow ysinx = 2[x + \tan\left(\frac{\pi}{4} - \frac{x}{2}\right)] + c$	1
	Given that $y = 0$, when $x = \frac{\pi}{4}$,	
	Hence, $0 = 2[\frac{\pi}{4} + tan\frac{\pi}{2}] + c$	
	$\Rightarrow c = -\frac{\pi}{2} - 2tan = 0$	
	$=\frac{1}{2}-\frac{1}{2}-\frac{1}{8}$	
	Hence, the particular solution is (π, x) (π, π)	
	$y = cosecx[2\{x + tan(\frac{1}{4} - \frac{1}{2})\} - (\frac{1}{2} + 2tan\frac{1}{8})]$	1/2
9	If $\vec{a} \neq \vec{0}$ \vec{a} $\vec{b} = \vec{a}$ \vec{a} $\vec{a} \neq \vec{b} = \vec{a} \times \vec{a}$ then show that $\vec{b} = \vec{a}$	
01	If $\vec{u} \neq 0$, $\vec{u} \cdot \vec{v} = \vec{u} \cdot \vec{c}$, $\vec{u} \neq \vec{v} = \vec{u} \cdot \vec{c}$, then show that $\vec{v} = \vec{c}$.	
	Solution. We have $u_{-}(\vec{v} - \vec{v}) = 0$	
	$\Rightarrow (b-c) = 0 \text{ or } a \perp (b-c)$	
	$\Rightarrow b = \vec{c} \text{ or } \vec{a} \perp (b - \vec{c})$	1
	Also, $\vec{a} \times (\vec{b} - \vec{c}) = \vec{0}$	
	\Rightarrow $(\vec{b} - \vec{c}) = \vec{0} \text{ or } \vec{a} \parallel (\vec{b} - \vec{c})$	
	$\Rightarrow \vec{b} = \vec{c} \text{ or } \vec{a} \parallel (\vec{b} - \vec{c})$	1
	$ec{a}$ can not be both perpendicular to $(ec{b}-ec{c})$ and parallel to $(ec{b}-ec{c})$	
	Hence, $\vec{b} = \vec{c}$.	1
10.	Find the shortest distance between the following lines:	
	$\vec{r} = (\hat{\imath} + \hat{\jmath} - \hat{k}) + s(2\hat{\imath} + \hat{\jmath} + \hat{k})$	
	$\vec{r} = (\hat{\imath} + \hat{\jmath} + 2\hat{k}) + t(4\hat{\imath} + 2\hat{\jmath} + 2\hat{k})$	

	Solution: Here, the lines are parallel. The shortest distance = $\frac{ (a_2 - a_1) \times b }{ \vec{b} }$		
	$\left \left (3\hat{k}) \times (2\hat{\imath} + \hat{\jmath} + \hat{k}) \right \right $	1+1/2	
	$-\frac{1}{\sqrt{4+1+1}}$		
	$(3\hat{k}) \times (2\hat{i} + \hat{j} + \hat{k}) = \begin{vmatrix} i & j & k \\ 0 & 0 & 3 \\ 2 & 1 & 1 \end{vmatrix} = -3\hat{i} + 6\hat{j}$	1	
	Hence, the required shortest distance = $\frac{3\sqrt{5}}{\sqrt{6}}$ units	1⁄2	
	OR		
	Find the vector and the cartesian equations of the plane containing the point $\hat{i} + 2\hat{j} - \hat{k}$ and parallel to the lines $\vec{r} = (\hat{i} + 2\hat{j} + 2\hat{k}) + s(2\hat{i} - 3\hat{j} + 2\hat{k})$ and $\vec{r} = (2\hat{i} + \hat{i} - 2\hat{k}) + t(\hat{i} - 2\hat{i} + \hat{k})$		
	Solution: Since, the plane is parallel to the given lines, the cross product of the vectors $2\hat{i} - 3\hat{j} + 2\hat{k}$ and $\hat{i} - 3\hat{j} + \hat{k}$ will be a normal to the plane		
	$ (2\hat{\imath} - 3\hat{\jmath} + 2\hat{k}) \times (\hat{\imath} - 3\hat{\jmath} + \hat{k}) = \begin{vmatrix} \hat{\imath} & \hat{\jmath} & k \\ 2 & -3 & 2 \\ 1 & -3 & 1 \end{vmatrix} = 3\hat{\imath} - 3\hat{k} $	1	
	The vector equation of the plane is $\vec{r} \cdot (3\hat{i} - 3\hat{k}) = (\hat{i} + 2\hat{j} - \hat{k}) \cdot (3\hat{i} - 3\hat{k})$ or, $\vec{r} \cdot (\hat{i} - \hat{k}) = 2$	1	
	and the cartesian equation of the plane is $x - z - 2 = 0$	1	
<u>SECTION – C</u>			
	<u>SECTION – C</u>		
11.	$\frac{\text{SECTION} - C}{\text{Evaluate: } \int_{-1}^{2} x^3 - 3x^2 + 2x dx}$		
11.	SECTION – C Evaluate: $\int_{-1}^{2} x^3 - 3x^2 + 2x dx$ Solution: The given definite integral = $\int_{-1}^{2} x(x - 1)(x - 2) dx$		
11.	$\frac{\text{SECTION} - C}{\text{Evaluate: } \int_{-1}^{2} x^{3} - 3x^{2} + 2x dx}$ Solution: The given definite integral = $\int_{-1}^{2} x(x - 1)(x - 2) dx$ = $\int_{-1}^{0} x(x - 1)(x - 2) dx + \int_{0}^{1} x(x - 1)(x - 2) dx + \int_{1}^{2} x(x - 1)(x - 2) dx$	1+1/2	
11.	$\frac{\text{SECTION} - \text{C}}{\text{Evaluate: } \int_{-1}^{2} x^3 - 3x^2 + 2x dx}$ Solution: The given definite integral = $\int_{-1}^{2} x(x-1)(x-2) dx$ $= \int_{-1}^{0} x(x-1)(x-2) dx + \int_{0}^{1} x(x-1)(x-2) dx + \int_{1}^{2} x(x-1)(x-2) dx$ $= -\int_{-1}^{0} (x^3 - 3x^2 + 2x) dx + \int_{0}^{1} (x^3 - 3x^2 + 2x) dx - \int_{1}^{2} (x^3 - 3x^2 + 2x) dx$	1+1/2 1/2	
11.	$\frac{\text{SECTION} - \text{C}}{\text{Evaluate: } \int_{-1}^{2} x^{3} - 3x^{2} + 2x dx}$ Solution: The given definite integral = $\int_{-1}^{2} x(x - 1)(x - 2) dx$ $= \int_{-1}^{0} x(x - 1)(x - 2) dx + \int_{0}^{1} x(x - 1)(x - 2) dx + \int_{1}^{2} x(x - 1)(x - 2) dx$ $= -\int_{-1}^{0} (x^{3} - 3x^{2} + 2x) dx + \int_{0}^{1} (x^{3} - 3x^{2} + 2x) dx - \int_{1}^{2} (x^{3} - 3x^{2} + 2x) dx$ $= -[\frac{x^{4}}{4} - x^{3} + x^{2}]_{-1}^{0} + [\frac{x^{4}}{4} - x^{3} + x^{2}]_{0}^{1} - [\frac{x^{4}}{4} - x^{3} + x^{2}]_{1}^{2}$	1+1/2 1/2	
11.	$\frac{\text{SECTION} - \text{C}}{\text{Evaluate: } \int_{-1}^{2} x^{3} - 3x^{2} + 2x dx}$ Solution: The given definite integral = $\int_{-1}^{2} x(x - 1)(x - 2) dx$ $= \int_{-1}^{0} x(x - 1)(x - 2) dx + \int_{0}^{1} x(x - 1)(x - 2) dx + \int_{1}^{2} x(x - 1)(x - 2) dx$ $= -\int_{-1}^{0} (x^{3} - 3x^{2} + 2x) dx + \int_{0}^{1} (x^{3} - 3x^{2} + 2x) dx - \int_{1}^{2} (x^{3} - 3x^{2} + 2x) dx$ $= -[\frac{x^{4}}{4} - x^{3} + x^{2}]_{-1}^{0} + [\frac{x^{4}}{4} - x^{3} + x^{2}]_{0}^{1} - [\frac{x^{4}}{4} - x^{3} + x^{2}]_{1}^{2}$ $= \frac{9}{4} + \frac{1}{4} + \frac{1}{4} = \frac{11}{4}$	1+1/2 1/2 2	
11.	$\frac{\text{SECTION} - \text{C}}{\text{Evaluate: } \int_{-1}^{2} x^{3} - 3x^{2} + 2x dx}$ Solution: The given definite integral = $\int_{-1}^{2} x(x - 1)(x - 2) dx$ = $\int_{-1}^{0} x(x - 1)(x - 2) dx + \int_{0}^{1} x(x - 1)(x - 2) dx + \int_{1}^{2} x(x - 1)(x - 2) dx$ = $-\int_{-1}^{0} (x^{3} - 3x^{2} + 2x) dx + \int_{0}^{1} (x^{3} - 3x^{2} + 2x) dx - \int_{1}^{2} (x^{3} - 3x^{2} + 2x) dx$ = $-[\frac{x^{4}}{4} - x^{3} + x^{2}]_{-1}^{0} + [\frac{x^{4}}{4} - x^{3} + x^{2}]_{0}^{1} - [\frac{x^{4}}{4} - x^{3} + x^{2}]_{1}^{2}$ = $\frac{9}{4} + \frac{1}{4} + \frac{1}{4} = \frac{11}{4}$	1+1/2 1/2 2	
11.	$\frac{\text{SECTION} - \text{C}}{\text{Evaluate: } \int_{-1}^{2} x^{3} - 3x^{2} + 2x dx}$ Solution: The given definite integral = $\int_{-1}^{2} x(x - 1)(x - 2) dx$ = $\int_{-1}^{0} x(x - 1)(x - 2) dx + \int_{0}^{1} x(x - 1)(x - 2) dx + \int_{1}^{2} x(x - 1)(x - 2) dx$ = $-\int_{-1}^{0} (x^{3} - 3x^{2} + 2x) dx + \int_{0}^{1} (x^{3} - 3x^{2} + 2x) dx - \int_{1}^{2} (x^{3} - 3x^{2} + 2x) dx$ = $-[\frac{x^{4}}{4} - x^{3} + x^{2}]_{-1}^{0} + [\frac{x^{4}}{4} - x^{3} + x^{2}]_{0}^{1} - [\frac{x^{4}}{4} - x^{3} + x^{2}]_{1}^{2}$ = $\frac{9}{4} + \frac{1}{4} + \frac{1}{4} = \frac{11}{4}$	1+1/2 1/2 2	
11.	$\frac{\text{SECTION} - \text{C}}{\text{Evaluate: } \int_{-1}^{2} x^{3} - 3x^{2} + 2x dx}$ Solution: The given definite integral = $\int_{-1}^{2} x(x - 1)(x - 2) dx$ = $\int_{-1}^{0} x(x - 1)(x - 2) dx + \int_{0}^{1} x(x - 1)(x - 2) dx + \int_{1}^{2} x(x - 1)(x - 2) dx$ = $-\int_{-1}^{0} (x^{3} - 3x^{2} + 2x) dx + \int_{0}^{1} (x^{3} - 3x^{2} + 2x) dx - \int_{1}^{2} (x^{3} - 3x^{2} + 2x) dx$ = $-[\frac{x^{4}}{4} - x^{3} + x^{2}]_{-1}^{0} + [\frac{x^{4}}{4} - x^{3} + x^{2}]_{0}^{1} - [\frac{x^{4}}{4} - x^{3} + x^{2}]_{1}^{2}$ = $\frac{9}{4} + \frac{1}{4} + \frac{1}{4} = \frac{11}{4}$	1+1/2 1/2 2	
11.	Evaluate: $\int_{-1}^{2} x^{3} - 3x^{2} + 2x dx$ Solution: The given definite integral = $\int_{-1}^{2} x(x - 1)(x - 2) dx$ $= \int_{-1}^{0} x(x - 1)(x - 2) dx + \int_{0}^{1} x(x - 1)(x - 2) dx + \int_{1}^{2} x(x - 1)(x - 2) dx$ $= -\int_{-1}^{0} (x^{3} - 3x^{2} + 2x) dx + \int_{0}^{1} (x^{3} - 3x^{2} + 2x) dx - \int_{1}^{2} (x^{3} - 3x^{2} + 2x) dx$ $= -\left[\frac{x^{4}}{4} - x^{3} + x^{2}\right]_{-1}^{0} + \left[\frac{x^{4}}{4} - x^{3} + x^{2}\right]_{0}^{1} - \left[\frac{x^{4}}{4} - x^{3} + x^{2}\right]_{1}^{2}$ $= \frac{9}{4} + \frac{1}{4} + \frac{1}{4} = \frac{11}{4}$	1+1/2 1/2 2	
11.	$\frac{\text{SECTION} - C}{\text{Solution: The given definite integral} = \int_{-1}^{2} x(x-1)(x-2) dx}$ $= \int_{-1}^{0} x(x-1)(x-2) dx + \int_{0}^{1} x(x-1)(x-2) dx + \int_{1}^{2} x(x-1)(x-2) dx$ $= -\int_{-1}^{0} (x^{3} - 3x^{2} + 2x) dx + \int_{0}^{1} (x^{3} - 3x^{2} + 2x) dx - \int_{1}^{2} (x^{3} - 3x^{2} + 2x) dx$ $= -[\frac{x^{4}}{4} - x^{3} + x^{2}]_{-1}^{0} + [\frac{x^{4}}{4} - x^{3} + x^{2}]_{0}^{1} - [\frac{x^{4}}{4} - x^{3} + x^{2}]_{1}^{2}$ $= \frac{9}{4} + \frac{1}{4} + \frac{1}{4} = \frac{11}{4}$	1+1/2 1/2 2	
11.	$\frac{\text{SECTION} - C}{\text{Solution: The given definite integral}} = \int_{-1}^{2} x(x-1)(x-2) dx$ $= \int_{-1}^{0} x(x-1)(x-2) dx + \int_{0}^{1} x(x-1)(x-2) dx + \int_{1}^{2} x(x-1)(x-2) dx$ $= -\int_{-1}^{0} (x^{3} - 3x^{2} + 2x) dx + \int_{0}^{1} (x^{3} - 3x^{2} + 2x) dx - \int_{1}^{2} (x^{3} - 3x^{2} + 2x) dx$ $= -[\frac{x^{4}}{4} - x^{3} + x^{2}]_{-1}^{0} + [\frac{x^{4}}{4} - x^{3} + x^{2}]_{0}^{1} - [\frac{x^{4}}{4} - x^{3} + x^{2}]_{1}^{2}$ $= \frac{9}{4} + \frac{1}{4} + \frac{1}{4} = \frac{11}{4}$	1+1/2 1/2 2	



	The required area = the shaded area = $\int_0^1 \sqrt{3}x dx + \int_1^2 \sqrt{4 - x^2} dx$	
	$\sqrt{3} \left[x^{2} \right]^{1} + \frac{1}{1} \left[x \left(\frac{1}{4} - x^{2} + 4 \sin^{-1} x \right)^{2} \right]^{2}$	1
	$\begin{bmatrix} -\frac{1}{2} \begin{bmatrix} x \\ y \end{bmatrix}_{0} + \frac{1}{2} \begin{bmatrix} x \\ y \end{bmatrix}_{0} + \frac{1}{2} \begin{bmatrix} x \\ y \end{bmatrix}_{1} + \frac$	
	$=\frac{\sqrt{3}}{2}+\frac{1}{2}\left[2\pi-\sqrt{3}-2\frac{\pi}{2}\right]$	
	$=\frac{2\pi}{2\pi}$ square units	1
	3 3 3 4 4 4 7 5 4 1 1 5 7	
13.	Find the foot of the perpendicular from the point $(1, 2, 0)$ upon the plane $x = 3y + 2z = 9$. Hence, find the distance of the point $(1, 2, 0)$ from the given	
	r = 3y + 2z = 3. Thence, and the distance of the point (1, 2, 0) non-the given plane.	
	Solution: The equation of the line perpendicular to the plane and passing	
	x - 1 $y - 2$ z	1
	$\frac{1}{-1} = \frac{1}{-3} = \frac{1}{2}$	
	The coordinates of the foot of the perpendicular are $(\mu + 1, -3\mu + 2, 2\mu)$ for some μ	1/2
	These coordinates will satisfy the equation of the plane. Hence, we have	
	$\mu + 1 - 3(-3\mu + 2) + 2(2\mu) = 9$	
	$\Rightarrow \mu = 1$ The foot of the perpendicular is (2 -1 2)	1
	Hence, the required distance = $\sqrt{(1-2)^2 + (2+1)^2 + (0-2)^2} = \sqrt{14}$ units	1

14.	CASE-BASED/DATA-BASED		
	Fig 3		
	An insurance company believes that people can be divided into two classes: those who are		
	accident prone and those who are not. The company's statistics show that an accident-prone		
	person will have an accident at sometime within a fixed one-year period with probability 0.6,		
	whereas this probability is 0.2 for a person who is not accident prone. The company knows that		
	20 percent of the population is accident prone.		
	Based on the given information, answer the following questions.	1	
	(i)what is the probability that a new policyholder will have an accident within a year of purchasing a policy?		
	(ii) Suppose that a new policyholder has an accident within a year of purchasing a policy. What is the probability that he or she is accident prone?		
	Solution: Let E_1 = The policy holder is accident prone. E_2 = The policy holder is not accident prone. E = The new policy holder has an accident within a year of purchasing a policy.		
	(i) $P(E) = P(E_1) \times P(E/E_1) + P(E_2) \times P(E/E_2)$ $= \frac{20}{100} \times \frac{6}{10} + \frac{80}{100} \times \frac{2}{10} = \frac{7}{25}$	1	
	(ii) By Bayes' Theorem, $P(E_1/E) = \frac{P(E_1) \times P(E/E_1)}{P(E)}$	1	
	$=\frac{\frac{20}{100}\times\frac{6}{10}}{\frac{280}{1000}}=\frac{3}{7}$	1	
