POST GRADUATE COMMON ENTRANCE TEST - 2015

DATE & TIME	COURSE	SUBJECT		
08-08-2015 10.30 AM TO 12.30 PM	ME / M.Tech/ M.Arch / Courses Offered by VTU / UVCE / UBDTC	MECHANICAL SCIENCES MC / IPE / IEM / AE / MSE		

MAXIMUM MARKS	TOTAL DURATION	MAXIMUM TIME FOR ANSWERING		
100	150 MINUTES	120 MINUTES		

MENTION YOUR PGCET NO.	QUESTION BOOKLET SERIAL NUMBER	301425		
	VERSION CODE	A – 1		

DOs:

- Check whether the PGCET No. has been entered and shaded in the respective circles on the OMR answer sheet.
- Ensure whether the circles corresponding to course and the specific branch have been shaded on the OMR answer sheet.
- 3. This question booklet is issued to you by the invigilator after the 2nd bell i.e., after 10.25 am.
- 4. The serial number of this question booklet should be entered on the OMR answer sheet.
- 5. The version code of this question booklet should be entered on the OMR answer sheet and the respective circles should also be shaded completely.
- 6. Compulsorily sign at the bottom portion of the OMR answer sheet in the space provided.

DON'Ts:

- 1. THE TIMING AND MARKS PRINTED ON THE OMR ANSWER SHEET SHOULD NOT BE DAMAGED / MUTILATED / SPOILED.
- THE 3RD BELL RINGS AT 10.30 AM, TILL THEN;
 - Do not remove the seal / staple present on the right hand side of this question booklet.
 - · Do not look inside this question booklet.
 - Do not start answering on the OMR answer sheet.

IMPORTANT INSTRUCTIONS TO CANDIDATES

- 1. This question booklet contains 75 (items) questions and each question will have one statement and four answers. (Four different options / responses.)
- After the 3rd Bell is rung at 10.30 am, remove the seal / staple stapled on the right hand side of this
 question booklet and check that this booklet does not have any unprinted or torn or missing pages or
 items etc., if so, get it replaced by a complete test booklet. Read each item and start answering on the
 OMR answer sheet.
- During the subsequent 120 minutes:
 - Read each question (item) carefully.
 - Choose one correct answer from out of the four available responses (options / choices) given
 under each question / item. In case you feel that there is more than one correct response, mark
 the response which you consider the best. In any case, choose only one response for each item.
 - Completely darken / shade the relevant circle with a blue or black ink ballpoint pen against the question number on the OMR answer sheet.
- Use the space provided on each page of the question booklet for Rough Work. Do not use the OMR answer sheet for the same.
- After the last bell is rung at 12.30 pm, stop marking on the OMR answer sheet and affix your left hand thumb impression on the OMR answer sheet as per the instructions.
- 6. Hand over the **OMR answer sheet** to the room invigilator as it is.
- 7. After separating the top sheet (KEA copy), the invigilator will return the bottom sheet replica (candidate's copy) to you to carry home for self evaluation.
- 8. Preserve the replica of the OMR answer sheet for a minimum period of ONE year.
- 9. Only Non-programmable calculators are allowed.

MARKS DISTRIBUTION

PART - A : (SECTION - 1) 30 QUESTIONS : 30 X 1 = 30; (SECTION - 2) 15 QUESTIONS : 15 X 2 = 30

PART - B : (SECTION - 1) 20 QUESTIONS : $20 \times 1 = 20$; (SECTION - 2) 10 QUESTIONS : $10 \times 2 = 20$

MECHANICAL SCIENCE

IMPORTANT INSTRUCTIONS & BRANCHWISE INDEX FOR THE CANDIDATES

Question Nos. 1 to 45 compulsory and common to all the branches. Question Nos. 46 to 75 are optional. sub-branches are there in this booklet. The candidate has to opt for any one branch according to his / her Application Form.

Sub -	Subject	Subject			
Branch	Subject	From	То		
1.	Automobile Engineering (AE)	8	12		
2.	Mechanical Engineering (MC)	13	15		
3.	Industrial and Production Engineering (IPE)	16	19		
4.	Industrial Engineering and Management (IEM)	20	22		
5.	Manufacturing Science and Engineering (MSE)	23	27		

MECHANICAL SCIENCES COMMON TO AE/MC/IPE/IEM/MSE PART - A (SECTION - I)

(Each question carries one mark)

(30 X 1 = 30)

For what values of h, the following system is consistent

$$x - 3y = h$$
$$-2x + 6y = 5$$

- a) h = 0
- b) h = -5/2
- c) h = -5
- d) h = 5/2
- 2. The eigen values of the matrix $\begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 2 \\ 2 & 1 & 0 \end{bmatrix}$ are
 - a) 0, -1, 2
- b) -1, 0, 1
- c) 0, 1, 2
- d) None
- 3. The rank of the matrix will depend on
 - a) Number of rows of a matrix
 - b) Determinant of a matrix
 - c) Number of non-zero rows of a matrix
 - d) None
- Gauss Jordon and Gauss elimination methods are
 - a) Step by step methods
 - b) Analytical methods
 - c) Self correcting methods
 - d) Iterative methods
- 5. The ability of a meterial to resist fracture due to high impact loads, is called
 - a) Strength
- b) Stiffness
- c) Toughness
- d) Brittleness

- 6. In low carbon steels, presence of small quantities of sulphur improves
 - a) Weldability
 - b) Formability
 - c) Mechinability
 - d) Hardenability
- 7. 18/8 stainless steel consists of
 - a) 18% nickel and 8% chromium
 - b) 18% chromium and 8% Nickel
 - c) 18% nickel and 18% chromium
 - d) 8% nickel and 8% chromium
- Mass moment of inertia of a uniform thin rod of mass "M" and length "l" about its mid-point and perpendicular to its length is

a)
$$\frac{2}{3}M1^2$$

b)
$$\frac{1}{3}$$
 M1

c)
$$\frac{3}{4}M1^2$$

d)
$$\frac{4}{3}$$
 M1

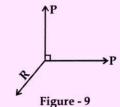


Figure 9 shows the two equal forces at right angles acting at a point. The value of force R acting along their bisector and in opposite direction is

a) P/2

b) 2P

- c) $\sqrt{2}$ P
- d) $P/\sqrt{2}$

Space For Rough Work

9.

10. In a biaxial stress problem, the stresses in

x - and y - directions are σ_x = 200 MPa,

 σ_y = 100 MPa. The maximum pricipal stress in MPa is

- a) 50
- b) 100
- c) 150
- d) 200
- 11. the second moment of a circular area about the diameter is given by (D is the diameter)
 - a) $\frac{\pi D^4}{4}$
- b) $\frac{\pi D^4}{16}$
- c) $\frac{\pi D^4}{32}$
- d) $\frac{\pi D^4}{64}$
- 12. The relationship between Young's modulus (E) Bulk modulus (K) and Poisson's ratio (γ) is given by
 - a) $E = 3K(1-2\gamma)$
 - b) $K = 3E(1-2\gamma)$
 - c) $E = 3K(1-\gamma)$
 - d) $K = 3E(1-\gamma)$
- A vessel of 4m³ contains an oil which weighs 30 KN. The specific weight of oil is
 - a) 4.5 KN/m^3
- b) 6 KN/m³
- c) 7.5 KN/m^3
- d) 10 KN/m³
- 14. The pressure at a point 4m below the free surface of water is
 - a) 19.24 kPa
- b) 29.24 kPa
- c) 39.24 kPa
- d) 49.24 kPa

- 15. Bernoulli's equation is applied to
 - a) Venturimeter
 - b) Orificemeter
 - c) Pitot tube
 - d) All of the above
- 16. Which of the following is an intensive property of a thermodynamic system?
 - a) Volume
- b) Temperature
- c) Mass
- d) Energy
- The sum of internal energy (U) and the product of pressure and volume (p, v) is known us
 - a) Work done
- b) Entropy
- c) Enthalpy
- d) None of these
- 18. The gas constant (R) is equal to the
 - a) Sum of two specific heats
 - b) Difference of two specific heats
 - c) Product of two specific heats
 - d) Ratio of two specific heats.
- In a kinematic chain, a quaternary joint is equivalent to
 - a) One binary joint
 - b) two binary joint
 - c) Three binary joint
 - d) Four binary joint
- 20. In vibration isolation system, if $\omega/\omega_n > 1$, then the phase difference between the transmitted force and the disturbing force is
 - a) 0^{0}
- b) 90°
- c) 180°
- d) 270°

- The temperature at which the new grains 21. are formed in the metal is called
 - Lower critical temperature
 - b) Recrystallisation temperature
 - c) Upper critical temperature
 - Eutectic temperature d)
- 22. The sand used for making cores is
 - a) green sand
- Oil sand b)
- c) Loam sand
- d) Dry sand
- 23. Seam welding is a
 - Process of used for joining round bars
 - b) Multi-spot welding process
 - Continuous spot welding c)
 - d) Arc welding process
- 24. The drill spindles are provided with standard taper known as
 - a) Morse taper
 - b) Chapman taper
 - Sellers taper c)
 - d) Brown and sharp taper
- 25. Which of the following property is desirable in parts subjected to shock and impact loads?
 - Strength a)
- b) Stiffness
- c) Toughness
- d) Brittleness
- Which of the following welded joint is 26. designed for shear strenght?
 - Transverse fillet welded joint a)
 - Parallel fillet welded joint b)
 - Buff welded joint c)
 - d) All of these

- The resilience of a bolt may be increased by 27.
 - increasing its shank diameter
 - increasing its length b)
 - c) decreasing its shank diameter
 - decreasing its length
- When a shaft is subjected to combined 28. twisting moment (T) and bending moment (M) then the equivalent bending moment is equal to

a)
$$\frac{1}{2}\sqrt{M^2+T^2}$$

b)
$$\sqrt{M^2+T^2}$$

b)
$$\sqrt{M^2 + T^2}$$

c) $\frac{1}{2} \left(M + \sqrt{M^2 + T^2} \right)$

d)
$$M + \sqrt{M^2 + T^2}$$

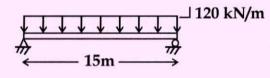
- 29. Work study involves
 - Method study and work measurement a)
 - Only work measurement b)
 - Only method study c)
 - Only motion study
- 30. CPM requires
 - Single time estimate
 - Double time estimate b)
 - Triple time estimate
 - None of these

- 31. The two links OA and OB are connected by a pin joint at O. If the link OA turns with angular velocity 4 rad/s in the clockwise direction and the link OB turns with angular velocity 2 rad/s in the anticlockwise direction, then the rubbing velocity at the pin joint O is
 - a) 8r
- b) 2r
- c) 6r
- d) 4r

where r = Radius of the pin at O

- 32. There are six gears A, B, C, D, E and F in a compound train. The number of teeth in the gears are 20, 60, 30, 80, 25 and 75 respectively. The ratio of angular speeds of the driven (F) to the driver (A) of the drive is
 - a) 1/24
- b) 1/8
- c) 4/15
- d) 12
- 33. A shaft of mass (m_c) and stiffness (S) is fixed at one end and carries a mass (m) at the other end. The natural frequency of the longitudinal vibration is equal to
 - a) $2\pi \sqrt{\frac{S}{m+m_c}}$
 - b) $2\pi \sqrt{\frac{S}{m + m_c/3}}$
 - c) $\frac{1}{2\pi} \sqrt{\frac{S}{m+m_c}}$
 - $\frac{1}{2\pi}\sqrt{\frac{S}{m+m_c/3}}$

- 34. A solid circular shaft of 60 mm diameter transmits a torque of 1600 N-m. The value of maximum shear stress developed is
 - a) 37.72 MPa
- b) 47.72 MPa
- c) 57.72 MPa
- d) 67.72 MPa
- 35. A steel bar of 40mm x 40mm square crosssection is subjected to an axial compressive load of 200 KN. If the length of the bar is 2m and E = 200 GPa, the compression of the bar will be
 - a) 1.25 mm
- b) 2.70 mm
- c) 4.05 mm
- d) 5.40 mm
- 36. A steel beam of breadth 120mm and height 750 mm is loaded as shown in figure. Assume E_{steel} = 200 GPa. The beam is subjected to a maximum bending moment of



- a) 4750 KN m
- b) 3375 KN m
- c) 6750 KN m
- d) 8750 KN -m
- 37. An oil of kinematic viscosity 0.4 stoke flows through a pipe of diameter 300 mm at the rate of 300 lps. The value of Reynolds number is
 - a) 3.18 x 10⁴
- b) 31.8 x 10⁴
- c) 318 x 10⁴
- d) 0.318 x 10⁴

- 38. The diameters of a pipe at the sections 1 and 2 are 10cm and 15cm respectively. Velocity of water at section 1 is 5 m/s. The velocity at section 2 is
 - a) 3.33 m/s
- b) 2.22 m/s
- c) 4.44 m/s
- d) 1.11 m/s
- 39. The dimension of the physical quantity torque is
 - a) $ML^2\bar{T}^2$
- b) $M^2 L \bar{T}^2$
- c) $ML\bar{T}^3$
- d) $ML^3\bar{T}^3$
- 40. If the value fo n = 0 in the equation $pv^n = c$, then the process is called
 - a) Isobaric process
 - b) Adiabitic process
 - c) Isochoric porcess
 - d) Isothermal process
- 41. Otto cycle is also known as
 - a) Constant pressure cycle
 - b) Constant volume cycle
 - c) Constant temperature cycle
 - d) Constant temperature and pressure cycle

- 42. Two helical tensile springs of the same material and also having identical mean coil diameter and weight, have wire diameters d and d/2. The ratio of their stiffness constants is
 - a) 16
- b) 4
- c) 64
- d) 128
- 43. The number of teeth on pinion and gear are 15 and 45 respectively. If the module of the gear is 8, then centre distance between the shaft is
 - a) 360 mm
- b) 480 mm
- c) 240 mm
- d) 120 mm
- 44. A bearing is designated by the number 405, it means that a bearing is of
 - a) Light series with bore of 5 mm
 - b) heavy series with bore of 25 mm
 - c) medium series with bore of 15 mm
 - d) light series with width of 20 mm
- 45. If F is the fixed cost, V is the variable cost per unit (or total variable cost) and P is the selling price of each unit (or total sales value), then break-even point is equal to
 - a) $\frac{FXV}{P}$
- b) $\frac{\text{FXP}}{\text{V}}$
- c) $\frac{F}{1+(\sqrt{P})}$
- d) $\frac{F}{1-(V/P)}$

(AE : AUTOMOBILE ENGINEERING)

PART - B (SECTION - I)

(Each question carries one mark)

(20 X 1 = 20)

The rolling resistance is because of the 46. 49. If clearance volume of I.C. engines is friction between the increased, the compression ratio will a) Wheel rim and type increase b) Tyre and the road surface b) decrease Wheel rim and road surface c) remain constant c) None of these d) d) be doubled 47. The torque available at the contact between 50. The acid used in automobile battery is driving wheels and road is known as hydrochloric acid Brake effort a) a) Clutch effort hydrofluoric acid b) **b**) Tractive effort c) nitric acid c) None of these d) sulphuric acid d) 48. For the same maximum pressure and 51. The function of an alternator in an temperature automobile is to a) Diesel cycle is more efficient that otto Supply electric power a) b) Convert mechanical energy into b) Otto cycle is more efficient than diesel electrical energy cycle Continually recharge the battery Both otto cycle and Diesel cycle are c) c) equally efficient d) Partly convert engine power into None of the above d) electric power

52.	When there is a reduction in amplitude over every cycle of vibration, then the body is said to have		56.		high speed engines, a rocker arm of should be used
	a)	Free vibration		a)	I - Section
	b)	Forced vibration		b)	Rectangular section
	c)	Damped vibration		c)	T - Section
	d)	None of the above		d)	Circular
53.		factor which affects the critical speed of aft is	57.	The	skirt of piston
	a)	Diameter of the disc		a)	is used to withstand the pressure of gas
	b)	Span of the shaft			in the cylinder
	c)	Eccentricity		b)	acts as a bearing for the side thrust of the connecting rod.
	d)	All of these			
5 4	TL -	unation of the mannious disulations of		c)	is used to seal the cylinder in order to prevent leakage of the gas past the piston
54.	the f	ratio of the maximum displacement of orced vibration to the deflection due to tatic force, is known as		d)	None of the above
	a)	damping factor			
	b)	damping coefficient	58.	Lewi	s equation in spur gears is applied
	c)	logarithmic decrement		a)	Only to the pinion
	d)	magnification factor		b)	Only to the gear
	77.5	1		c)	To stronger of the pinion or gear
55.		esigning a connecting rod, it is dered like for buckling about its.		d)	To weaker of the pinion or gear
	a)	Both ends fixed	59.	The o	overdrive consists of gear train
	b)	Both ends hinged		a)	Simple
	c)	One end is fixed and the other end		b)	Compound
	۷)	hinged		c)	Epicylic
	d)	One end fixed and the other end free		d)	Reverted
				ч,	

Space For Rough Work

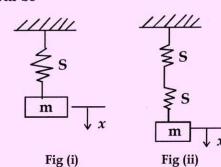
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- 60. The type of fit that occurs when two toleranced mating parts are sometimes an interference fit and sometimes a clearance fit when assembled
 - a) Interference fit
 - b) Clearance fit
 - c) Transition fit
 - d) Geometric fit
- 61. A hole is dimension $\phi g^{+0.015}$ mm.

 The corresponding shaft is of dimension $\phi g^{+0.010}$ mm. The resulting assembly has
 - a) Loose running fit
 - b) Close running fit
 - c) Transition fit
 - d) Interference fit
- 62. A CNC vertical milling machine has to cut a straight slot of 10 mm width and 2mm depth by a cutter of 10mm diameter between points (0,0) and (100, 100) on the xy plane (dimensions in mm). The feed rate used for milling is 50mm/min milling time for the slot (in seconds) is
 - a) 120
- b) 170
- c) 180
- d) 240

- 63. The crank radius of a single cylinder I.C. engine is 60mm and the diameter of the cylinder is 80mm. The swept volume of the cylinder in cm³ is
 - a) 48
- b) 96
- c) 302
- d) 603
- 64. The function of interpolater in a CNC machine controller is to
 - a) Control spindle speed
 - b) Coordinate feed rates of axes
 - c) Control tool rapid approach speed
 - d) Perform miscellaneous (M) functions (tool change, coolant control etc.)
- 65. The centre distance between two meshing involute gears are equal to
 - a) $\frac{\text{Sum of base circle radii}}{\cos \phi}$
 - b) $\frac{\text{Difference of base circle radii}}{\cos \phi}$
 - c) $\frac{\text{Sum of pitch circle radii}}{\cos \phi}$
 - d) $\frac{\text{Difference of pitch circle radii}}{\cos \phi}$

- 66. The coefficient of rolling resistance for a truck weighing 63500 N is 0.018. The rolling resistance to the truck is
 - a) 1.143 N
- b) 11.43N
- c) 114.3N
- d) 1143N
- 67. A petrol engine of a car develops 125 N-m torque at 2700 rpm. The car is driven in second gear having gear ratio of 1.75. The final drive ratio is 4.11. If the overall transmission efficiency is 90%. then the torque available at the driving wheels is
 - a) 8.091 N-m
- b) 80.91 N-m
- c) 809.1 N-m
- d) 8091 N-m
- 68. For a spring -mass system as shown in figure (i) the frequency of vibration is f_n . When one more similar spring is added in series as shown in figure (ii) the frequency of vibration will be

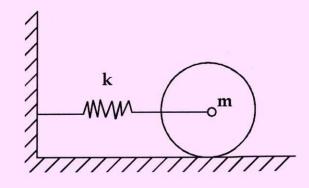


- a) $f_n/\sqrt{2}$
- b) f_n
- c) $\sqrt{2} \cdot f_n$
- d) $2f_n$

69. The equation of motion for a single degree of freedom system with viscous damping is

$$4\frac{d^2x}{dt^2} + 9\frac{dx}{dt} + 16x = 0$$
. The damping ratio of the system is

- a) 9/8
- b) $9/8\sqrt{2}$
- c) 9/16
- d) 9/128
- 70. A disc of mass m is attached to a spring of stiffness k as shown in the figure. The disc rolls without slipping on a horizontal surface. The natural frequency of vibration of the system is



- a) $\frac{1}{2\pi}\sqrt{\frac{K}{m}}$
- b) $\frac{1}{2\pi}\sqrt{\frac{2K}{m}}$
- c) $\frac{1}{2\pi} \sqrt{\frac{2K}{3m}}$
- d) $\frac{1}{2\pi}\sqrt{\frac{3K}{2m}}$

- 71. Cylindrical pins of $25^{+0.020}$ mm diameter are electroplated in a shop. Thickness of the plating is $30^{+2.0}$ micron. Neglecting gage tolerances, the size of the GO gage in mm to inspect the plated component is
 - a) 25.042
 - b) 25.052
 - c) 25.074
 - d) 25.084
- 72. A triangular facet in a CAD model has vertices: $P_1(0, 0, 0)$, $P_2(1, 1, 0)$ and $P_3(1, 1, 1)$ The area of facet is
 - a) 0.500
- b) 0.707
- c) 1.414
- d) 1.732
- 73. Allowance in limits and fits refers to
 - a) Maximum clearance between shaft and hole
 - b) Minimum clearance between shaft and hole
 - c) Difference between maximum and minimum size of hole
 - d) Difference between maximum and minimum size of shaft

- 74. The tool of an NC machine has to move along a circular arc from (5, 5) to (10, 10) while performing an operation. The centre of the arc is at (10, 5). Which one of the following NC tool path commands performs the above mentioned operation?
 - a) N010 G01 X10 Y10 X5 Y5 R5
 - b) N010 G03 X10 Y10 X5 Y5 R5
 - c) N010 G01 X5 Y 5 X10 Y10 R5
 - d) N010 G02 X5 Y5 X10 Y10 R5
- 75. The firing order for an in-line four cylinder I.C. engine is
 - a) 1 3 2 u
 - b) 1-3-4-2
 - c) 1-2-u-3
 - d) 1-2-3-u

(MC: MECHANICAL ENGINEERING)

PART - B (SECTION - I)

(Each question carries one mark)

 $(20 \times 1 = 20)$

- 46. For a given heat flow and for the same thickness the temperature drop across the material will be maximum for
 - a) Copper
 - b) Steel
 - c) Glass-wool
 - d) Refractory circle
- 47. In case of one dimensional heat conduction in a medium with constant properties, T is the temperature at postion, X at time t, then $\frac{\partial T}{\partial t}$ is propotional to
 - a) $\frac{T}{X}$
- b) $\frac{\partial T}{\partial x}$
- c) $\frac{\partial^2 t}{\partial x \partial t}$
- d) $\frac{\partial^2 T}{\partial x^2}$
- 48. For the same inlet and outlet temperature of hot and cold fluids, the Log Mean Temperature Difference (LMTD) is
 - a) Greater for parallel flow
 - b) Greater for counter flow
 - c) Same for both
 - d) Dependent on the properties of fluids
- 49. In a pulverized fuel fired large power boiler the heat transfer from the burning fuel to the wall of the furnace is
 - a) by conduction only
 - b) by convection only
 - c) by conduction and convection
 - d) Predominantly by radiation

- 50. Cavitation in a hydraulic turbine is most likely to occur at the turbine
 - a) Entry
- b) Exit
- c) Stator exit
- d) Rotor exit
- 51. Streamlines, pathlines, streak lines are virtually identical for
 - a) Uniform flow
 - b) Flow of ideal fluids
 - c) Steady flow
 - d) Non-uniform flow
- 52. A fluid is said to be Newtonian when the shear strees is
 - a) Directly proportional to velocity gradient
 - Inversely proportional to velocity gradient
 - c) Independent of velocity gradient
 - d) None of these
- 53. In flow through a pipe, the transition from laminar to turbulent flow does not depend on
 - a) Velocity of the fluid
 - b) Density of the fluid
 - c) Diameter of the pipe
 - d) Length of the pipe
- 54. Kaplan turbine is
 - a) A high head mixed flow turbine
 - b) A low axial flow turbine
 - c) An outward flow reaction turbine
 - d) An Impulse inward flow turbine

55.		PERT, the distrib	utio	n of activity times is	60.	-	eration manageme Translation	ent is b)		process
	a)	Normal	b)	Gamma		a)			Trans	
	c)	Beta	d)	Exponential		c)	Transaction	d)	Trans	111011
	Cj	Beta	щ	Daponemia	61	11/1	sigh of those would	d on a	norotic	no monger
E6	ТЬ		m 1 v r	wood oritorio for	61.		nich of these would t be responsible for		operano	nis manger
56.		easuring forecast		used criteria for		a)	Safety and main	tenai	nce	
	a)	Mean absolute	devia	tions		b)	Sales and marke	eting		
	b)	Mean absolute	perce	entage error		c)	Selecting supplie	er		
	c) Mean standard error					d)	Recruiting emplo	oyees		
	d)	Mean square er	ror							
	,				62.		ansducers produce	out	put vol	tage in the
57.	A11	to Collimator is u	ised	to check			m of		¥	
07.	a)	Roughness	ioca	to officer		a)	an analog voltage			
	b)	Flatness				b)	an analog voltage			
	c)	Angle			Ter	c)	an analog voltage	ın th	e form (or pressure
	d)	Automobile balar	200			d)	all of the above			
	щ	Automobile balai	ice		62	117L	at is sissal sandi	tioni.	.~	
F0	3371	.:-h	£-11	i	63.	-	nat is signal condi			
58.				owing forecasting or making forecasts		a) b)	To analyse any s Conversion or mo			f aignal
	for	planning produ		schedules in the			Conversion of an			
		ort range				c) d)	Conversion of dig		4.50	
	a)	Moving average				щ	Conversion of dig	itai t	o anaio	g signai
	b)	Exponential mo	3.277	average	64.	NC	contouring is an	evam	nle of	
	c)	Regression ana	lysis		0 1.	a)	Continuous path			
	d)	Delphi				b)	Point to point pos		_	
						c)	Absolute position			
59.				rference fit, it is limit of the shaft		d)	Incremental posi		ng.	
		ould be	lower	mint of the shart			*.			
	a)	Greater than t	he ı	apper limit of the	65.		the following g hnique which are			
	b)	Lesser than the	uppe	er limit of the hole		a)	Wireframe model	ling		
	c)	Greater than t	he l	ower limit of the		b)	Drafting			
		hole				c)	Surface modelling	g		
	d)	Lesser than the	lowe	r limit of the hole.		d)	Solid modelling			

Space For Rough Work

d) Solid modelling

- 66. A turbine develope 9000 kW when running at 100rpm head on turbine is 30m. If head on the turbine is reduced to 18m, the power developed by turbine is
 - a) 4182.84 kW
- b) 3228.48 kW
- c) 2182.48 kW
- d) 2382.84 kW
- 67. A turbine operaters under a head of 25m at 200 rpm, Discharge is 9 m³/s, overall efficiency is 90% power developed is
 - a) 1986.5 kW
- b) 2986.5 kW
- c) 986.5 kW
- d) 3986.5 kW
- 68. Pelton wheel develops 2000 kW under a head of 100 m and with and overall efficiency of 85% the discharge is
 - a) $0.4 \text{ m}^3/\text{s}$
- b) $2.4 \text{ m}^3/\text{s}$
- c) $1.4 \text{ m}^3/\text{s}$
- d) $3.4 \text{ m}^3/\text{s}$
- 69. An electric cable of aluminium conductor (K=240w/mk) is to be insultated with rubber (K=0.15w/mk). The cable is to be located in air (h=6w/m²), the critical thickness insulation will be
 - a) 25mm
- b) 40mm
- c) 160mm
- d) 800mm
- 70. When t_{c1} and t_{c2} are the temperature of cold fluid at entry and exit respectively and t_{h1} and t_{h2} are the temperature of hot fluid at entry and exit point and cold fluid has lower heat capacity rate as compared to hot fluid, then effectiveness of the heat exchanger is given by
 - $\frac{t_{c1}-t_{c2}}{t_{h1}-t_{c2}}$
- b) $\frac{t_{h2} t_{h1}}{t_{c1} t_{h1}}$
- c) $\frac{t_{h1} t_{h2}}{t_{h1} t_{c1}}$
- d) $\frac{t_{c2} t_{c1}}{t_{h1} t_{c1}}$

- 71. In a forecasting model, at the end of the period 13, the forecasted value for period 14 is 75. Actual value in the periods 14 to 16 are constant at 100. If the assumed simple exponential smoothing parameter is 0.5, then the MSE at the end of period 16 is
 - a) 820.31
- b) 273.44
- c) 43.75
- d) 14.58
- 72. In computing wilsons economic lot size for an item, by mistake the demand rate estimate used was 40% higher than the true demand rate. Due to this error in the lot size computation, the total cost of setups plus inventry holding per unit time, would rise above the true optimum by approximately
 - a) 1.4%
- b) 6.3%
- c) 18.3%
- d) 8.7%
- 73. A manufacturer produces two types of products 1 and 2, at production levels of x_1 and x_2 respectively. The profits is given by $2x_1 + 5x_2$. The production constraints are

$$x_1 + 3x_2 \le 40$$

$$3x_1 + x_2 \le 24$$

$$x_1 + x_2 \le 10$$

 $x_1 > 0, x_2 > 0$ the maximum profit which can meet the contraints is

- a) 29
- b) 38
- c) 44
- d) 75
- 74. A fit is specified as 25 H8/e8. The tolerance value for a nominal diameter of 25 mm in IT8 is 33 microns and fundamental deviation for the shaft is 40 microns, the maximum clearence of the fit in micron is
 - a) -7
- b) 7
- c) 73
- d) 106
- 75. Match the following configuration of robot
 - P. Cartesian
- 1 α β γ
- Q. Cylindrical
- 2xyZ
- R. Articulated
- $3xy\theta$

where xyz linear co-ordinate and rest are angular

- a) P-2, Q-3, R-1
- b) P-1, Q-2, R-3
- c) P-3, Q-2, R-1
- d) None of these

IPE - INDUSTRIAL AND PRODUCTION ENGINEERING

PART - B (SECTION - I)

(Each question carries one mark)

(20 X 1 = 20)

- 46. The gauge used to check the clearence between two mating parts
 - a) Screw gauge b) Radius gauge
 - c) Feeler gauge d) Wire gauge
- 47. The straight surface between the crest and root of the thread is called
 - a) Flank
- b) Lead
- c) Pitch
- d) None
- 48. Diameter of the best size wire D_b is
 - a) $\frac{P}{2}\cos\phi$
- b) $\frac{P}{2} \sec \phi$
- c) $\frac{P^2}{2} \sin \phi$
- d) None
- 49. A feasible solution requires that all artificial variable is
 - a) Greater than zero
 - b) Less than zero
 - c) Equal to zero
 - d) None of these
- 50. Which type of control chart should be used when it is possible to have more than one mistake per item
 - a) X-bar chart
- b) C-chart
- c) R chart
- d) P chart

- 51. In acceptence sampling the producer risk is the risk of having a
 - a) bad lot accepted
 - b) good lot rejected
 - c) bad lot rejected
 - d) good lot accepted
- 52. For the last 30 days, the number of mistakes on the daily report has averaged 4.5. What would the UCL be if a 3-sigma C-chart was constructed
 - a) 18
- b) 10.86
- c) 7.5
- d) 2.12
- 53. Calculating the time required to do a job so that one can then work out how many people are required is termed
 - a) Method study
 - b) Ergonomics
 - c) Work measurement
 - d) Technology study
- 54. The process of allocating a large number of tasks to individual is called
 - a) Job empowerment
 - b) Job enlargement
 - c) Job enrichment
 - d) Job rotation

55.	The	computerised	techno	ology that is used to	60.	TIG	welding is also	knov	vn as
		gn part is knov		ω		a)	Metal inert ga	as we	elding
	a)	CIM	b)	CAM	-	b)	Torch inert ga	as we	elding
	c)	CAD	d)	All of these		c)	Gas shielded	meta	l arc welding
						d)	Tungsten iner	rt ga	s welding
56.		erically contro	olled n	g are true about nachines pre-programmed to	61.	tran			hnique in which the an angle to the test
	aj	drill, turn, m		pre-programmed to		a)	Angle beam t	estin	g
	b)	NC machines	are t	he most commonly		b)	Immersion te	sting	g
		used form of	flexibl	e automation		c)	Contact testing	ng	
	c)	a) and b)				d)	Through-tran	smis	sion testing
	d)	None of the a	bove					NAMES OF STREET	1: 1
					62.		ch of the following city of ultrasour		nedia has the lowest
57.				d effector can be		a)	Water	b)	Plastic
		h of the follow		ent task, including		c)	Air	d)	Steel
	a)	Spot welding			63.	Whic	ch machining p	roces	s are used for gear
	b)	Spray painting	painting			manufacture			
	c)	Material han	dling			1.	Form milling	2.	Broaching
	d)	All of the abo				3.	Roll forming	4.	Hobbing
		y or une above						8	he code given below
58.	Wh:	ah af tha fal	1	a mashaa ia maat		a.	1, 2 & 3	b.	1, 3 & 4
38.	com	nonly used for	testin	g probes is most g welded metals for		c.	1, 2 & 4	d.	2, 3 & 4
				beam inspection	64.	Flan		mair	nly on which of the
	a)	Surface wave	570			a)	Nose part & top	face	
	b)	Twin crystal	•			b)	Wearing edge o		
	c)	Single crysta	•			c)	Nose part, from	nt rel	ief face & side relief
	d)	An angle prol	be				face of cutting e	===	1
						d)	Face of the tool	ing ed	ige
59.	Soun	id can propaga	te as		65.	The o	casting materia	ls for	coated carbide tool
	a)	Longitudinal	wave			inclu	de		
	b)	Shear waves				a)	Tic, Tin and Na	aCN	
	c)	Surface wave	s			b)	Tic & Tin		
	d)	All of these				c)	Tin and NaCN Tic and NaCN		
				Snoo For	D1	d)			

Space For Rough Work

- 66. A medium carbon steel work piece is turned on a lathe of 50m/min tooling speed, 0.8mm/rev feed and 1.5 mm depth of cut. What is the value of material removal rate
 - a) 1000 mm²/min
 - b) 60,000 mm³/min
 - c) 20,000 mm³/min
 - d) Cannot be calculated with the given data
- 67. The rake angle of a cutting edge is 15° shear angle 45° and tooling velocity 35m/min. What is the velocity of chip along the cut face
 - a) 28.5 m/min
 - b) 27.3 m/min
 - c) 25.3 m/min
 - d) 23.5 m/min
- 68. Consider the following statements

A nomenclature 50 H8/P8 denotes that

- 1. Hole diameter is 50 mm
- 2. it is a shaft base system
- 3. 8 indicates fundamental deviation

Which of the statement given above is/ are correct

- a) 1, 2, & 3
- b) 1 & 2 only
- c) 1 & 3 only
- d) 3 only

- 69. Twenty samples of size 100 are taken the total number of defective item is 75. What is the UCL of the 3 sigma (Z =3) P-chart
 - a) 0.094
 - b) 0.793
 - c) 0.0375
 - d) 0.165
- 70. A box of 1000 parts is subjected to an acceptance sampling plan that examines only 50 parts. The actual fraction defective in the box is 0.02 and the sampling plan has a 0.53 probability of accepting a box of this quality. What is average outgoing quality for the scenario
 - a) 0.53
 - b) 0.02
 - c) 0.51
 - d) 0.01

- 71. In an NC maching operation, the tool has to be moved from point (5,4) to point (7,2) along a circular path with centre at (5,2) before starting the operations. The tool is at (5,4) the correct G and M code for this motion
 - a) N010 G03 X7 Y2 I5 J2
 - b) N010 G02 X7 Y2 I5 J2
 - c) N010 G01 X7 Y2 I5 J2
 - d) N010 G00 X7 Y2 I5 J2
- 72. The fluorescent dyes used in the liquid penetrant testing process are most active when energised with black light of what wave length? (A° stands for angstrom units)
 - a) 2000 A^o
 - b) 2500 A^o
 - c) 3250 A^o
 - d) 3650 A^o
- 73. What is the magnetic field strength at the surface of a 100 mm diameter bar as compared to that at the surface of a 50mm diameter bar, each carrying 1000 amps of current
 - a) Twice
 - b) One half
 - c) One quater
 - d) Four times

74. Consider the following linear programming problem

maximize $Z = 3x_1 + 2x_2$

subject to

$$x_1 \leq 4$$

$$x_2 \le 6$$

$$3x_1 + 2x_2 \le 18$$

$$x_1 \ge 0, \ x_2 \ge 0$$

- The LPP has a unique optimal solution
- b) The LPP is infeasible
- c) The LPP is unbounded
- d) The LPP has multiple optimal solution
- 75. A manufacture produces two types of products 1 and 2, at production level of x₁ and x₂ respectively. The profit is given is 2x₁ + 5x₂. The production constraints are:

$$x_1 + 3x_2 \le 40$$
, $3x_1 + x_2 \le 24$,

$$x_1 + x_2 \le 10, \ x_1 > 0, \ x_2 > 0$$

the maximum profit which can meet the constraints is

- a) 29
- b) 38
- c) 44
- d) 75

IEM: INDUSTRIAL ENGINEERING AND MANAGEMENT PART - B (SECTION - I)

(Each question carries one mark)

(20 X 1 = 20)

46.	Erg	gonomics has evolved to be concerned with	51.	In	LPP, degenerac	y occu	rs in	stages
	a)	Design of work equipment		a)	One	b)	Two	
	b)	Adapting the person to the workplace		c)	Three	d)	Four	
	c)	Design and development of equipment						
47.	d)	Design of whole systems of work to is known as "the father of scientific	52.	un	riven transporta balanced, if the total			
47.		nagement"?		a)	Optimisation	Đ		
	a)	Fredrick W. Taylor		b)	Demand			
	b)	Henry Fayol		c)	Cost			
	c)	Robert Owen		d)	None of the a	bove		
	d)	Non of these						
48.	For	rces affecting organisational behaviour	53.		gistics is the par h the forward a			
		People b) Environment	1	a)	Goods	b)	Services	
	a) c)	Technology d) All of the above		c)	Cash	d)	All of the	above
49.		o is recognised as "father of human ations"?	54.	The	e first activity of			
	a)	William Gilbreth		aj	purchase	ing it	equiremen	it to the
	b)	Hendry Fayol		b)	Source select	ion an	d developm	nent
	c)	F.W. Taylor		c)	Recognising t	he nee	d for procu	ırement
	d)	Elton Mayo		d)	Inspection of a	goods		
50.	of c	erations Research involves attack omplex problems to arrive at the optimum ution	55.		difference bet size and minim			
	a)	Scientific		a)	Size tolerance	e		
	b)	Systematic		b)	Tolerance Zon	ne		
	c)	Both "a" and "b"		c)	Standard tole	rance		
	d)	Statistical		d)	All of the above	re		
		Space For	Pough	Was	-1-			

- 56. In time study, the rating factor is applied to determine
 - a) Standard time of a job
 - b) Merit rating of the worker
 - c) Fixation of incentive rate
 - d) Normal time of a worker
- 57. PERT analysis is based upon
 - a) Optimistic time
 - b) Pessimistic time
 - c) Most likely time
 - d) All of these
- 58. A B C analysis is used in
 - a) CPM
 - b) PERT
 - c) Inventory control
 - d) All of these
- 59. In order to avoid excessive multiplication of facilities, the layout preferred is
 - a) Product layout
 - b) Process layout
 - c) Group layout
 - d) Static layout
- 60. Gantt chart is used for
 - a) Inventory control
 - b) Material handling
 - c) Production schedule
 - d) Machine repair schedules

- 61. The factors to be considered for production scheduling are
 - a) Component design
 - b) Route sheet
 - c) Time Standards
 - d) All of these
- 62. The computerized technology that is used to design part is known as
 - a) CIM
- c CAM
- c) CAD
- d) All of these
- 63. Which of the following are true about numerically controlled machines?
 - a) NC machines are pre-programmed to drill, turn, mill
 - b) NC machines are the most commonly used form of flexible automation
 - c) (a) and (b)
 - d) None of the above
- 64. Auto collimator is used to check
 - a) Roughness
 - b) Flatness
 - c) Angle
 - d) Automobile balance
- 65. In the specification of dimensions and fits
 - a) Allowance is equal to bilateral tolerance
 - b) Allowance is equal to unilateral tolerance
 - c) Allowance is independent of tolerance
 - d) Allowance is equal to the difference between maximum and minimum dimension specified by the tolerance.

- 66. For a small scale industry, the fixed cost per month is Rs. 5,000. The variable cost per product is Rs. 20 and sales price is Rs. 30 per piece. The break-even production per month will be
 - a) 300
- b) 460
- c) 500
- d) 1000
- 67. In CPM, the cost slope is determined by
 - a) Crash cost
 Normal cost
- b. Crash cost Normal cost
 Normal time crash time
- c) Normal cost
- d. Normal cost Crash cost
 Normal time Crash time
- 68. If A is the total items consumed per year, P is the procurement cost per order and C is the annual inventory carrying cost per item, then the most economic ordering quantity is given by
 - a) AP/C
- b) 2AP/C
- c) $\sqrt{\frac{2AF}{C}}$
- d) $\left(\frac{AP}{C}\right)^2$
- 69. The mathematical technique for finding the best use of limited resources of a company in the maximum manner is known as
 - a) Value analysis
 - b) Network analysis
 - c) Linear programming
 - d) Queing theory
- 70. When the dimension is expressed as $20^{+0.035}_{-0.025}$ then the tolerance is
 - a) 0.035 mm
- b) 0.025 mm
- c) 0.01 mm
- d) 0.06 mm

- 71. The accuracy of micrometers, calipers, dial indicators can be checked by a
 - a) Feeler gauge
- b) Slip gauge
- c) Ring gauge
- d) Plug gauge
- 72. A company uses 2555 units of an item annually. Delivery lead time is 8 days. The recorder point (in number of units) to achieve optimum inventory is
 - a) 7

b) 8

c) 56

- d) 60
- 73. Arrivals at a telephone booth are considered to be poission, with an average time of 10 minutes between successive arrivals. The length of a phone call is distributed exponentially with mean 3 minutes. The probability that an arrival doesnot have to wait before service is
 - a) 0.3
- b) 0.5
- c) 0.7
- d) 0.9
- 74. Vehicle manufacturing assembly line is an example of
 - a) Product layout
 - b) Process layout
 - c) Manual layout
 - d) Fixed layout
- 75. In a CNC program block, N002 G02 G91 X40 Z40, G02 and G91 refer to
 - a) Circular interpolation in CCW direction and incremental dimension
 - b) Circular interpolation in CCW direction and absolute dimension
 - c) Circular interpolation in clockwise direction and incremental dimension
 - d) Circular interpolation in clockwise direction and absolute dimension

MSE: MANUFACTURING SCIENCE AND ENGINEERING PART - B (SECTION - I)

(Each question carries one marks)

 $(20 \times 1 = 20)$

- 46. In D.C. welding, the staight polarity (Electrode negative) results in
 - a) Lower penetration
 - b) Lower deposition rate
 - c) Less heating of workpiece
 - d) Smaller weld pod
- 47. In oxyacetylene gas welding, temperature at the inner core of the flame is around
 - a) 3500°C
- b) 3200°C
- c) 2900°C
- d) 2550°C
- 48. In deep drawing of sheets, the value of limiting draw ratio depends on
 - a) Percentage elongation of sheet metal
 - b) Yield strength of sheet metal
 - c) Type of press used
 - d) Thickness of sheet
- 49. Hot rolling of mild-steel carried out
 - a) at re-crystalization temperature
 - b) between 100°C and 150°C
 - c) between re-crystalization temperature
 - d) Above re-crystalization temperature

- 50. In a point to point control NC machine, the slides are positioned by an itegrally mounted stepper motor drive. If the specification of the motor is 1°/pulse, and the pitch of the lead screw is 3.6 mm, what is the expected position accuracy
 - a) 1mm
- b) 10 mm
- c) 50 mm
- d) 100 mm
- 51. In a point to point type of NC system
 - Control of position and velocity of the tool is essential
 - b) Control of only position of the tool is sufficient
 - c) Control of only velocity of the tool is sufficient
 - Neither position nor velocity need to be controlled
- The effect of rake angle on the mean friction angle in maching can be explained by
 - a) Sliding model of friction
 - Sticking and then sliding model of friction
 - c) Sticking friction
 - d) Sliding and then sticking model of friction

53.	Cutting power consumption in turning can be significantly reduced by		56.		ummy activity is used in PERT network escribe
	a)	Increasing rake angle of the tool		a)	Precedence relationship
				b)	Necessary time delay
	b)	Increasing the cutting angle of the tool		c)	Resource restriction
	c)	Widening the nose radius of the tool		d)	Resource idleness
	d)	Increasing the clearance angle			
			57.	The	general tools used in presses are
				a)	Drill bits
54.	A sh	naft (diameter $20^{+0.05}_{-0.15}$ mm) and a hole		b)	Boxing tools
	(diar	meter $20^{+0.20}_{-0.1}$ mm) when assembled would		c)	Dies and punches
	yield			d)	None of these
	a)	Transition fit			
	b)	Interference fit	58.		ch of the following materials is an icial abrasive
	c)	Clearance fit		a)	Sand stone
	۵۱,	None of those		b)	Diamond
	d)	None of these		c)	Emery
				d)	Silicon carbide
55.		fit on a hole-shaft system is specified as 56. The type of fit is	F 0	Th a	anaustian of familiar dama in a classed
	a)	Clearance fit	59.	impr	operation of forging done in a closed ression die by means of drop hammers alled as
	b)	Sliding fit		a)	Press forging
	c)	Push fit		b)	Drop forging
	_n	Daniel Ch		c)	Upset forging
	d)	Force fit		d)	None of these
		Space For I	Rough	Worl	K.

A ring gauge is used to measure Controlling of machine tools by means of 63. 60. prepared program consisting of blocks or Outside diameter but not roundness series of numbers are known as a) Roundness but not outside diameter b) Numerical control a) Both outside diameter and roundness c) b) Automatic control d) Only external threads Mechanical control c) None of these d) Simplex method of solving linear 64. programming problem are The dimensional limits on a shaft of 2547 All the points in the feasible region a) are Only the corner points of the feasible b) 25.000, 25.021 mm a) region b) 25.000, 24.979 mm Intermediate points within the feasible c) region 25.000, 25.007 mm c) Only the interior points in the feasible d) region 25.000, 24.993 mm d) Which of the following is not the robot 65. In PERT analysis a critical activity has 62. programming method a) Maximum float Walk through method b) Zero float b) Lead through method

Space For Rough Work

c)

d)

Half-line programming

Transfer-line programming

c)

d)

Maximum cost

Minimum cost

- 66. Tool life of 10 hours is obtained when cutting with single point tool at 63m/min. If Taylors constant C = 257.35, tool life on doubling the velocity will be
 - a) 5 hours
- b) 25.7 min
- c) 38.3 min
- d) Unchanged
- 67. In a typical metal cutting operation using a cutting tool of positive rake $r = 10^{\circ}$, it was observed that the shear angle was 20° the friction angle is
 - a) 45°
- b) 30°
- c) 60°
- d) 40°
- 68. A brace billet is to be extruded from its initial diameter of 100mm to a final diameter of 50mm. The working temperature of 700°C and the extrusion constant is 250 Mpa. The force recuired for extrusion is
 - a) 5.44 MN
 - b) 2.72 MN
 - c) 1.36 MN
 - d) 0.36 MN

- 69. In a CNC program block, N02 G02 G91 X40 Z40, G02 and G91 refer to
 - a) Circular interpolation in CCW and incremental dimensions
 - b) Circular interpolation in CCW and absolute dimensions
 - c) Circular interpolation in CW and incremental dimensions
 - d) Circular interpolation in CW and absolute dimensions
- 70. What is the percentage increase in tool life when the cutting speed is halved
 - a) 50%
- b) 200%
- c) 300%
- d) 400%
- 71. Match the following:

NC code	Definition					
P.M05	1.	Absolute cordination				
Q.G01	2.	Linear interpolation				
R.G04	3.	Spindle stop				
S.G90	4.	Linear interpolation				

- a) P-2, Q-3, R-4, S-1
- b) P-3, Q-4, R-1, S-2
- c) P-3, Q-4, R-2, S-1
- d) P-4, Q-3, R-2, S-1

- 72. In open-die forging, the disc of diameter 200mm and height 60mm is compressed without any barreling effect. The final diameter of the disc is 400mm, the true strain is
 - a) 1.986
 - b) 1.686
 - c) 1.386
 - d) 0.602
- 73. A project consists of three parallel paths with mean duration and variance of (10,4), (12,4) and (12,9) respectively. According to the standard PERT assumptions the distribution of project duration is
 - a) Beta with mean 10 and standard deviation 2
 - b) Beta with mean 12 and standard deviation 2
 - c) Normal with mean 10 and standard deviation 3
 - d) Normal with mean 12 and standard deviation 3

74. What are the upper and lower limits of the shaft represented by 60f8

use the following data / Diameter 60 lies in the diameter step of 50-80 mm

fundamental tolerance unit i, in $U_m = 0.45$ D^{1/3}+0.001 D where D is representative size in mm. Tolerance value for IT8 = 25i, fundamental deviation for t shaft = -5.5 D^{0.41}

- a) lower limit = 59.924 mm, upper limit = 59.970 mm
- b) Lower limit = 59.954 mm, upper limit = 60.000 mm
- c) lower limit = 59.970 mm, upper limit = 60.016 mm
- d) lower limit = 60.000 mm, upper limit = 60.046 mm
- 75. The expected time (t_o) of a PERT activity interms of optimistic time (t_o), pessimistic time (t_o) and most likely time (t_i) is given by

a)
$$t_e = \frac{t_o + 4t_1 + t_p}{6}$$

b)
$$t_e = \frac{t_o + 4t_p + t_1}{6}$$

c)
$$t_e = \frac{t_o + 4t_1 + t_p}{3}$$

d)
$$t_e = \frac{t_o + 4t_1 + t_1}{3}$$