**Question:** Find the significant figure in \(50000.020 \times 10^{-3}\)

**Options:**
(a) 5  
(b) 6  
(c) 7  
(d) 8  

**Answer:** (d)

**Solution:**
All the digits in the number part are significant. Therefore, number of significant figures is 8.

**Question:** A block of mass, 2 kg is kept on a smooth surface as shown. It is being applied by force \(\vec{F} = 20\hat{i} + 10\hat{j}\). Find the displacement of the block in 10 seconds.

**Options:**
(a) 500 m  
(b) 10 m  
(c) 100 m  
(d) 50 m  

**Answer:** (a)

**Solution:**
Component of force in x-direction = 20 N  
Acceleration in x-direction = \(\frac{20}{2} = 10 \text{ m/s}^2\)  
Displacement in x-direction in 10s,
\[
\frac{1}{2}a_x\times t^2 = \frac{1}{2}\times 10\times 10^2 = 500 m
\]

**Question:** A tunnel is dug is the earth as shown. A particle of mass ‘m’ is released in the tunnel, find the time period of SHM of the particle: -

(ρ: density of earth)

**Options:**

(a) \[T = \frac{2\pi}{\sqrt{\frac{3}{4\pi \rho G}}}
\]

(b) \[T = \frac{2\pi}{\sqrt{\frac{3}{2\pi \rho G}}}
\]

(c) \[T = \frac{2\pi}{\sqrt{\frac{3}{\pi \rho G}}}
\]

(d) \[T = \frac{2\pi}{\sqrt{\frac{3}{4\rho G}}}
\]

**Answer:** (a)

**Solution:**

Time period of a particle along a tunnel dug in earth would be \[T = 2\pi \sqrt{\frac{R}{g}}\]

\[\Rightarrow T = 2\pi \sqrt{\frac{R}{\left(\frac{4\pi R \rho}{3}\right)}} \quad \left[\because g = \frac{4}{3} \pi R \rho\right]
\]

\[\Rightarrow T = 2\pi \sqrt{\frac{3}{4\pi \rho G}}
\]

**Question:** Four solid spheres each of mass m and radius a, have their centers on the vertices of a square whose side is b. Find moment of inertia about the given axis? (Assume spheres are connected using a light frame)

**Options:**
(a) \( m \left( \frac{8a^2}{5} + 2b^2 \right) \)

(b) \( m \left( \frac{8a^2}{5} + 4b^2 \right) \)

(c) \( m \left( \frac{4a^2}{5} + 2b^2 \right) \)

(d) \( m \left( \frac{4a^2}{5} + b^2 \right) \)

Answer: (a)

Solution:

\[
\Rightarrow \text{M.O.I of sphere (1) and (2) around axis } AB = I_1 = I_2 = \frac{2}{5} ma^2
\]

\[
\Rightarrow \text{M.O.I of sphere (3) and (4) around axis } AB = I_3 = I_4 = \left( \frac{mb^2}{5} + \frac{2}{5} ma^2 \right)
\]

(By using Parallel axis theorem)

Total M.O.I = \( I_1 + I_2 + I_3 + I_4 \)

= \( m \left( \frac{8}{5} a^2 + 2b^2 \right) \)

**Question:** For an amplitude modulated wave the max voltage is 16 voltage and minimum voltage is 8 volts then if the modulation factor is \( x = 10^{-2} \), then \( x \) is?

**Answer:** 33.33

**Solution:**

\[
m = \frac{V_{\text{max}} - V_{\text{min}}}{V_{\text{max}} - V_{\text{min}}}
\]

\[
= \frac{(16 - 8)}{(16 + 8)} = \frac{8}{24} = \frac{1}{3}
\]

\[= 0.3333\]
Question: An AC current is given by \( i(t) = I_1 \sin \omega t + I_2 \cos \omega t \). Find the rms value of current.

Options:
(a) \( i_{rms} = \frac{\sqrt{I_1^2 + I_2^2}}{2} \)
(b) \( i_{rms} = \frac{\sqrt{I_1^2 + I_2^2}}{\sqrt{2}} \)
(c) \( i_{rms} = \frac{I_1 + I_2}{2} \)
(d) \( i_{rms} = 2 \left( \sqrt{I_1^2 + I_2^2} \right) \)

Answer: (b)

Solution:
\( i(t) = I_1 \sin \omega t + I_2 \cos \omega t \)
So, we could write:
\[ i(t) = \sqrt{I_1^2 + I_2^2} \sin(\omega t + \phi) \]
[Where \( \phi = \tan^{-1} \left( \frac{I_2}{I_1} \right) \) ]
\[ i(t) = \sqrt{I_1^2 + I_2^2} \sin(\omega t + \phi) \]
So rms value would be
\[ i_{rms} = \frac{\sqrt{I_1^2 + I_2^2}}{\sqrt{2}} \]

Question: Initially two monoatomic gases are placed in an adiabatic container with insulated fixed partition. The initial pressure, volume and numbers of moles of the two gases are given. Now if the partition is removed. Find the final pressure of mixture.

Options:
(a) 1 atm
(b) 2.55 atm
(c) 5 atm
(d) 7 atm
Answer: (b)
Solution:
By conservation of Internal energy

\[ n_1 \left( \frac{3}{2}RT_1 \right) + n_2 \left( \frac{3}{2}RT_2 \right) = (n_1 + n_2) \frac{3}{2}RT \]

\[ \Rightarrow n_1T_1 + n_2T_2 = (n_1 + n_2)T \]

Using \((PV = nRT)\)

\[ \frac{PV_1}{R} + \frac{PV_2}{R} = \frac{P_fV_f}{R} \]

\[ P_f = \frac{PV_1 + PV_2}{V_f} \]

\[ = \frac{PV_1 + PV_2}{V_1 + V_2} \]

\[ = \frac{(4.5)(2) + (5.5)(3)}{10} \]

\[ = 2.55 \text{ atm} \]

Question: Two slabs are placed adjacently having thermal resistance \( R_1 \) & \( R_2 \) their free ends maintained at temperature of \( \theta_1 \) & \( \theta_2 \) respectively. Find the temperature of junction.

Options:
(a) \( \frac{R_1\theta_1 + R_2\theta_2}{R_1 + R_2} \)
(b) \( \frac{R_2\theta_1 + R_1\theta_2}{R_1 + R_2} \)
(c) \( \frac{\theta_1 + \theta_2}{2} \)
(d) \( |\theta_1 - \theta_2| \)
Answer: (b)
Solution:

\[ i_H = \frac{V_f}{R_H} \text{ or } \frac{\Delta Q}{\Delta t} = KA \frac{\Delta \theta}{\Delta x} \]

Now, it is given that both the slabs are in series
So, $i_{HH}$ will same for both the slabs.

Let the temperature of junction be $\theta$

Then,

$$i_{HH} = i_{H2},$$

$$\frac{\theta_1 - \theta}{R_1} = \frac{\theta - \theta_2}{R_2},$$

$$\theta_1 R_2 - \theta R_2 = \theta R_1 - \theta_2 R_1,$$

$$\theta R_1 + \theta R_2 = \theta_1 R_2 + \theta_2 R_1,$$

$$\theta = \frac{\theta_1 R_2 + \theta_2 R_1}{R_1 + R_2}.$$

**Question:** Find the equivalent resistance between A & B if all resistance are ‘R’?

**Options:**

(a) R
(b) 2R
(c) $\frac{R}{2}$
(d) 3R

**Answer:** (a)

**Solution:**

All resistance are R
This circuit satisfies wheat’s stone bridge condition. So, then equivalent circuit is

![Equivalent Circuit Diagram]

**Question:** Some drops, each of radius ‘r’ coalesce to form a large drop of radius ‘R’. The surface tension is T. Find the change in surface energy per unit volume.

**Options:**

(a) \( T \left( \frac{1}{r} - \frac{1}{R} \right) \)
(b) \( 3T \left( \frac{1}{r} - \frac{1}{R} \right) \)
(c) \( 3T \left( \frac{1}{R} - \frac{1}{r} \right) \)
(d) \( T \left( \frac{1}{R} - \frac{1}{r} \right) \)

**Answer:** (b)

**Solution:**

Radius of small drop is \( r \) and radius of big drop is \( R \).

When they coalesce, the volume will the same before and after coalesce.

\[
\frac{4}{3} \pi R^3 = n \cdot \frac{4}{3} \pi r^3 = \text{volume (V)}
\]

\[
R = n^{\frac{1}{3}} r \quad \text{...(1)}
\]

The surface area of large drop is \( 4\pi R^2 \) and surface area of small drop is \( 4\pi r^2 \)

Let

\( \Delta U \) – change in surface energy
\( \Delta A \) – Change in surface area
\( T \) - surface tension

Then, \( \Delta U = T \Delta A \)

\[
\Delta U = T \left( 4\pi R^2 - 4\pi r^2 \right)
\]
\[
\Delta U = \frac{3T}{3} \left( \frac{4\pi R^3}{R} - \frac{4\pi r^3}{r} \right)
\]
\[
\Delta U = 3T \left( \frac{4\pi R^3}{3R} - \frac{4\pi r^3}{3r} \right)
\]
\[
\Delta U = 3T \left( \frac{V}{R} - \frac{V}{r} \right)
\]
\[
\frac{|\Delta U|}{V} = 3T \left( \frac{1}{r} - \frac{1}{R} \right)
\]

**Question:** If the force acting on the body moving in circular motion is proportional to \( r^{-3} \), then the time period of its revolution is proportional to

**Options:**

(a) \( \frac{1}{r} \)

(b) \( \frac{1}{r^2} \)

(c) \( r^2 \)

(d) \( r \)

**Answer:** (c)

**Solution:**

\[ F = \frac{mv^2}{r} \]

According to question, \( F \propto r^{-3} \)

Or \( F = kr^{-3} \)

So, \( \frac{mv^2}{r} = kr^{-3} \)

\[ v^2 = kr^{-2} \]

Or \( v = \sqrt{\frac{k}{m} \cdot r^{-1}} \)

Now, \( T = \frac{2\pi r}{v} \)

\[ \therefore T = \frac{2\pi r}{\sqrt{\frac{k}{m} \cdot r^{-1}}} \]

So \( T \propto r^{2} \)

**Question:** A wire of length ‘L’ carries charge ‘Q’ uniformly distributed along its length. Find the electric field at a distance \( \frac{\sqrt{3L}}{2} \) from the wire at point ‘A’ as shown.
Options:
(a) \( E_A = \frac{Q}{2\sqrt{3\pi} \varepsilon_0 L} \)
(b) \( E_A = \frac{Q}{\sqrt{3\pi} \varepsilon_0 L^2} \)
(c) \( E_A = \frac{Q}{4\sqrt{3\pi} \varepsilon_0 L^2} \)
(d) \( E_A = \frac{2Q}{\sqrt{3\pi} \varepsilon_0 L^2} \)

Answer: (a)

Solution:
Electric field at a distance \( r \) from a uniformly charged finite length rod is given by
\[
E = \frac{2KQ}{r\sqrt{L^2 + 4r^2}}
\]
Where \( L \) is length of the rod and \( r \) is perpendicular distance of point from rod.

So, \( E = \frac{1}{2\pi \varepsilon_0} \frac{\sqrt{3L}Q}{2} \left( \frac{1}{\sqrt{L^2 + 3L^2}} \right) \)

\[
= \frac{1}{2\sqrt{3\pi} \varepsilon_0} \frac{Q}{L^2}
\]

Question: Find the force of attraction between a solid sphere of mass \( M \) and a ring of mass \( m' \) as shown

Options:
(a) \( F = \frac{GMm}{Q \sqrt{3R^2}} \)

(b) \( F = \frac{\sqrt{3}GMm}{8R^2} \)

(c) \( F = \frac{GMm}{8R^2} \)

(d) \( F = \frac{GMm}{3R^2} \)

Answer: (b)

Solution:
Electric field intensity on the axis of ring is given by
\[
\vec{E}_g = \frac{Gmx}{(r^2 + x^2)^\frac{3}{2}}
\]

Here, \( r = R \) and \( x = \sqrt{3}R \)

\[
\therefore \vec{E}_g = \frac{Gm\sqrt{3}R}{(R^2 + 3R^2)^\frac{3}{2}} = \frac{\sqrt{3}Gm}{8R^2}
\]

\[
\vec{F} = M\vec{E}_g = \frac{\sqrt{3}GMm}{8R^2}
\]

Question: A travelling wave is given by \( y = -0.21\sin(x + 3t) \) where \( x \) is in m, \( t \) is in seconds, \( y \) is in mm. (mass per unit length = 0.135 g/cm). Find the tension in the wire.

Options:
(a) \( T = 0.1215 \) N
(b) \( T = 20 \) N
(c) \( T = 15.35 \) N
(d) \( T = 5 \) N

Answer: (a)

Solution:
\[ y = -0.21\sin(x + 3t) \]

Comparing this equation with \( y = A\sin(kt + \omega t) \)
\( A = -0.21, \ k = 1, \ \omega = 3 \)

Velocity of wave,
\[ v = \frac{\omega}{k} = 3 \text{ m/s} \]

Now, \( v = \frac{\sqrt{T}}{\sqrt{\mu}} \)

Where \( \mu \) is mass per unit length of wire.

So, \( T = \mu v^2 \)
\[
= \left[ \frac{0.135 \times 10^{-3}}{10^{-2}} \right] \times (3)^2
\]
\[ = 0.1215 \text{ N} \]
**Question:** If \( W = \text{work done}, T = \text{Temperature}, K_B = \text{Boltzmann constant}, x = \text{Displacement} \) & \( W = \alpha \beta^2 e^{-\frac{x^2}{\alpha K_B T}} \), then find dimensions of \( \beta \)?

**Options:**
(a) \( [M^{1/2}L^2T^{-2}] \)
(b) \( [M^{-1/2}L^2T^{-2}] \)
(c) \( [M^{1/2}L^2T^{-2}] \)
(d) None of these

**Answer:** (c)

**Solution:**

\[ W = \alpha \beta^2 e^{-\frac{x^2}{\alpha K_B T}} \]

So, dimensions of

\[ [W] = [ML^2T^{-2}] \]
\[ [x] = [L] \]
\[ [K_B] = [ML^2T^{-2}K^{-1}] \]
\[ [T] = [K] \]

Now we know that power of e is constant i.e. dimensionless

So, \( \left[ \frac{x^2}{\alpha K_B T} \right] = \left[ M^0L^0T^0K^0 \right] \)

\[ \therefore [\alpha] = [M^{-1}T^2] \]

To find dimensions of \( \beta \)

\[ [W] = [\alpha][\beta^2] \]

\[ [\beta^2] = \left[ \frac{ML^2T^{-2}}{M^{-1}T^2} \right] = \left[ M^2L^4T^{-4} \right] \]

\[ \Rightarrow [\beta] = \left[ MLT^{-2} \right] \]

**Question:** When two capacitors \( C_1 \) and \( C_2 \) are in parallel, the equivalent capacitance is \( C_{11} \). When the same two are in series the equivalent is \( C_s \). The ratio of \( C_{11} : C_s \) is 15 : 4. Find \( \frac{C_2}{C_1} \)

**Answer:** (Bonus)

**Solution:**
\[
\frac{C_{ii}}{C_s} = \frac{15}{4} \\
\frac{C_1 + C_2}{C_s} = \frac{15}{4} \\
4(C_1 + C_2)^2 = 15C_1C_2
\]

This question will not lead to a real solution.
**Question:** Ozone in troposphere prevents us from?
**Options:**
(a) Cause photochemical smog
(b) Protects from UV radiation
(c) Protects from X-ray
(d) Protects from greenhouse effect
**Answer:** (b)
**Solution:** Ozone in troposphere, absorbs radiation especially UV radiations and protects humans and other living species from harmful effects of UV rays emitting from sun.

**Question:** Statement 1: O-nitrophenol is steam volatile due to H- bonding
Statement 2: O-nitrophenol has higher melting point due to H-Bonding
**Options:**
(a) Both statements are true
(b) S₁ is true, S₂ is false
(c) S₁ is false, S₂ is true
(d) Both are false
**Answer:** (b)
**Solution:** O-nitrophenol has intramolecular H-bonding while p-nitrophenol has intermolecular H-bonding. Due to this, molecules of o-nitrophenol are weakly held together and therefore steam volatile.
O – nitrophenol’s melting point = 216°C
P – nitrophenol’s melting point = 279°C

**Question:** Deficiency of which vitamin helps in delaying blood clotting?
**Options:**
(a) Vitamin B
(b) Vitamin K
(c) Vitamin C
(d) Vitamin E
**Answer:** (b)
**Solution:** Blood clotting is delayed or prevented because vitamin K is unavailable to act as an essential element (a cofactor) for the coagulation (clotting).

**Question:**
A and B are?

Options:

(a)

Answer: (a)

Solution:

Question: What is the structure of neoprene?
Question: S1: Dipole-dipole interactions are the only non-covalent interaction that lead to hydrogen bonding.
S2: Fluorine is the most electronegative element and hydrogen bonding in HF is symmetrical.
Options:
(a) Both statements are true
(b) S1 is true, S2 is false
(c) S1 is false, S2 is true
(d) Both are false
Answer: (c)
Solution: ion-dipole interaction can also lead to H-bonding
For example:
\[ KF + HF \rightarrow KHF_2 \]
\[ \downarrow \]
\[ HF^\text{−} \]
\[ F\text{−−−}H\text{−−−}F \]

Question: Number of Bridging CO in Mn₂(CO)₁₀
Question: How many faraday of electricity required to reduce 5 mole of MnO₄⁻ as per the given reaction:
\[ \text{MnO}_4^- + 16\text{H}^+ + 5\text{e}^- \rightarrow \text{Mn}^{2+} + 8\text{H}_2\text{O} \]
Options:
(a) 5 F
(b) 20 F
(c) 25 F
(d) 10 F
Answer: (c)
Solution:
For, 1 mole reduction \[ 5\text{F} \text{ electricity required} \]
For, 5 mole reduction \[ 5 \times 5 = 25\text{F} \text{ electricity required} \]

Question: The product is:
Amine \[ \xrightarrow{\text{Hinsberg's reagent}} \text{Product} \] (insoluble in NaOH)
That amine can also be prepared by ammonolysis of ethyl chloride
Options:
(a)
(b)

Hydrolysis

Answer: (a)
Solution:

Question:

\[ C_4H_8Cl_2 (A) \xrightarrow{\text{Hydrolysis}} C_4H_8O(B) \]

B forms oxime with \( NH_2OH \) but does not give Tollen’s test.

Compound (A) and (B) are respectively:

Options:
(a) 2,2 – Dichlorobutane and 2 - Butanone
(b) 2,2 – Dichlorobutane and 2 – Butanal
(c) 1,1 – Dichlorobutane and 2 – Butanal
(d) 1,2 – Dichlorobutane and 2 – Butanone

Answer: (a)
Solution:
Question: Match I.E with the elements of configuration given below:
(a) 1s^2 2s^2
(b) 1s^2 2s^2 2p^4
(c) 1s^2 2s^2 2p^3
(d) 1s^2 2s^2 2p^1
(i) 810
(ii) 899
(iii) 1300
(iv) 1490

Options:
(a) (a) → (i) ; (b) – (iii)
(b) (a) → (ii) ; (b) – (iii)
(c) (a) → (i) ; (b) – (iv)
(d) (a) → (iv) ; (b) – (iii)

Answer: (b)

Solution: Br has higher I.E than B. It can Bl, the last electron is in s-orbital while in case of B it is in p-orbital removal of electron. From s-orbital requires more energy than the electron from p-orbital 2s^2 2p^3 configuration is more stable than 2s^2 2p^4 due to half-filled p-subshell. So Cl I.E is more as it is filled to remove electron from stable half-filled configuration.

Question:

\[ \text{Compound} + \text{dil H}_2\text{SO}_4 \rightarrow \text{X} \]

\[ \text{H}_2\text{SO}_4 \quad \text{K}_2\text{Cr}_2\text{O}_7 \quad \text{Y} \]

What are X and Y respectively?

Options:
(a) SO_2, Cr_2O_3
(b) SO_3, Cr_2O_3
(c) SO_3, Cr_2(SO_4)_3
(d) SO_2, Cr_2(SO_4)_3

Answer: (d)

Solution:

\[ 3\text{SO}_2 + K_2\text{Cr}_2\text{O}_7 + H_2\text{SO}_4 \rightarrow \text{Cr}_2(\text{SO}_4)_3 + K_2\text{SO}_4 + H_2 \]

Question: Oxidation number of Cr in product, when Cr_2O_7^{2-} reacted with OH^-?

Options:
(a) +4
(b) +3
(c) +6
(d) 0

Answer: (c)
Solution:
\[ \text{Cr}_2\text{O}_7^{2-} + 2\text{OH}^- \rightarrow 2\text{CrO}_4^{2-} + \text{H}_2\text{O} \]
\[ \text{Cr}_2\text{O}_7^{2-} \Rightarrow \text{Oxidation state} = +6 \]
\[ \text{CrO}_4^{2-} \Rightarrow \text{Oxidation state} = +6 \]

**Question:** A gas law obeys \( P(V_m - b) = RT \), and \( \frac{dz}{dp} = \frac{x b}{RT} \), what is the value of \( X \)

**Options:**
(a) 2  
(b) 0.5  
(c) 2.5  
(d) 1  

**Answer:** (d)

**Solution:**
\[ Z = \frac{V_r}{V_i} \rightarrow \text{real gas } V_m \]
\[ P V_m - pb = RT \]
\[ V_m = \frac{RT + pb}{P} \]
\[ Z = \frac{RT + pb}{pV_i} \]
\[ = \frac{RT + pb}{RT} \{ \because P V_m = RT \} \]
\[ Z = 1 + \frac{pb}{RT} \]
\[ \frac{dz}{dp} = \frac{b}{RT} \therefore x = 1 \]

**Question:** Match the following:
(a) Cryolite                       (i) Sn
(b) Cassiterite                   (ii) Chloride
(c) Calamine                      (iii) Zn
(d) Carnallite                    (iv) Fluoride

**Options:**
(a) (a) → i; (b) → ii; (c) → iii; (d) → iv  
(b) (a) → iv; (b) → i; (c) → iii; (d) → ii  
(c) (a) → ii; (b) → i; (c) → iii; (d) → iv  
(d) (a) → iv; (b) → iii; (c) → ii; (d) → i

**Answer:** (b)

**Solution:**
Cryolite \( Na_3AlF_6 \)
Cassiterite \( SnO_2 \)
Calamine \( ZnCO_3 \)
Carnallite \( KCl \cdot MgCl_2 \cdot 6H_2O \)

Question:

\[
\begin{align*}
H & \quad \text{C} = \text{C} \quad H \\
H_3C & \quad < \quad C \quad = \quad C \quad < \quad Br
\end{align*}
\]

(1) NaNH \_ 2

(2) Red hot tube

Fe, 873K

Major product

Options:

(a)

\[
\begin{align*}
& \quad \text{CH}_3 \\
& \quad \text{CH}_3 \\
& \quad \text{CH}_3
\end{align*}
\]

(b)

(c)

(d)

H \_ 3C \quad < \quad \text{CH}_3

Answer: (c)

Solution:
**Question:** Which of the following doesn’t form MO₂ type oxide?

**Options:**
(a) Pr  
(b) Dy  
(c) Nd  
(d) Yb  

**Answer:** (d)  
**Solution:** Oxidation states of +2 & +3 and is not stable in +4 oxidation state so it does not form MO₂ type oxides.

**Question:** $\Delta S = 27 \text{ J/K-mol (values not confirmed)}$

$\Delta H = 80 \text{ KJ/mol}$  
What is the value of temperature at which reaction becomes spontaneous?  

**Options:**
(a) 2960 K  
(b) 2964 K  
(c) 2952 K  
(d) 2949 K  

**Answer:** (b)  
**Solution:**  
$\Delta G = \Delta H - T \cdot \Delta S$  
For spontaneity, $\Delta G < 0$  
$\therefore \Delta G = \Delta H - T \cdot \Delta S$  
$\Delta H - T \cdot \Delta S < 0$  
$\Delta H < T \Delta S$  
$T > \frac{\Delta H}{\Delta S}$  
$T > \frac{80,000}{27}$  
$T > 2963 K$

**Question:** Half heroult’s process is used for
Options:
(a) extraction of Au
(b) extraction of Zn
(c) extraction of Ae
(d) extraction of Ag
Answer: (c)
Solution:
Half heroult’s process is used for extraction of Ae where carbon anode is oxidised to Co and CO₂. Al⁺³ is reduced at cathode to form Al.
\[ 2Al₂O₃ + 3C \rightarrow 4Al + 3CO₂ \]
At Cathode : \( Al^{+3} + 3e^- \rightarrow Al \)
At Anode : \( C + O^{2-} \rightarrow CO + 2e^- \)
\( C + 2O^{3-} \rightarrow CO₂ + 4e^- \)

Question: Orbital having 2 radial and 2 angular nodes is
Options:
(a) 5d
(b) 3d
(c) 4f
(d) 5f
Answer: (a)
Solution:
No. of Radial nodes : \( n - 1 - 1 \)
No. of Angular nodes : 2
\[ \therefore 1 = 2; \rightarrow d\text{-orbital} \]
\[ n - \ell - 1 = 2 \]
\[ n - 2 - 1 = 2 \]
\[ n = 5 \]
\[ \therefore 5d \]

Question: Compound A is used as an oxidising agent to amphoteric in nature. It is part of the lead storage battery compound A is
Options:
(a) \( PbO \)
(b) \( Pb₃O₄ \)
(c) \( 2PbO, PbO₂ \)
(d) \( PbO₂ \)
Answer: (d)
Solution: In lead storage battery, \( PbO₂ \) is the oxidising agent that is amphoteric in nature as it reacts with both acids and bases So A is \( PbO₂ \)
**Question:** What is the major product of the following reaction?

\[
\begin{align*}
\text{CH}_2\text{CH}_3 & \quad \text{Br}_2/\text{hv} \\
\text{CN} & \\
\end{align*}
\]

**Options:**

(a) 
\[
\begin{align*}
\text{CH}_2\text{CH}_2\text{Br} & \\
\text{CN} & \\
\end{align*}
\]

(b) 
\[
\begin{align*}
\text{CHBrCH}_3 & \\
\text{CN} & \\
\end{align*}
\]

(c) 
\[
\begin{align*}
\text{Br} & \quad \text{CH}_2\text{CH}_3 \\
\text{CN} & \\
\end{align*}
\]

(d) 
\[
\begin{align*}
\text{Br} & \quad \text{CH}_2\text{CH}_3 \\
\text{CN} & \\
\end{align*}
\]

**Answer:** (b)

**Solution:**

It is free-radical substitution reaction of alkanes, so bromination takes place of benzylic carbon.
**Question:** Statement – I: Chloroform and aniline is separated by simple distillation.
Statement – II : When we separate water and aniline by steam distillation aniline boils below its boiling point.

**Options:**
(a) Statement I is true, Statement II is false
(b) Statement I is false, Statement II is true
(c) Statement I, II both are true
(d) Statement I, II both are false

**Answer:** (c)

**Solution:** Simple distillation may be used when the boiling points of two liquids are significantly different from each other or to separate liquids from solids or nonvolatile components. In simple distillation, a mixture is heated to change the most volatile component from a liquid into vapor.

**Question:** Which statement is false?

**Options:**
(a) Kjeldal method is used for estimation of nitrogen.
(b) Carius tube is used for estimation of sulphur
(c) Carius tube is used for estimation of nitrogen
(d) Phosphoric acid is precipitated by adding magnesia mixture on yields $Mg_2P_2O_7$

**Answer:** (c)

**Solution:** Carius method is used for quantitative estimation of halogen, sulphur and phosphorous.
Question: $x - y = 0, 2x + y = 6, x + 2y = 3$, triangle formed by these lines is

Options:
(a) right angled
(b) equilateral
(c) isosceles
(d) none

Answer: (c)

Solution:

\[ AB = \sqrt{1+4} = \sqrt{5} \]
\[ BC = \sqrt{2} \]
\[ AC = \sqrt{5} \]

Hence it is isosceles

Question: \[ \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{\cos^2 x}{1 + 3^3} \, dx = ? \]

Options:
(a)
(b)
(c)
(d)

Answer: ()

Solution:
\[ I = \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{\cos^2 x}{1+3^x} \, dx \quad \text{....(i)} \]

\[ I = \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{\cos^2 x}{1+3^{-x}} \, dx \]

\[
\text{[using } \int_{a}^{b} f(x) \, dx = \int_{a}^{b} f(a + b - x) \, dx \text{]}
\]

\[ I = \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{3^x \cos^2 x \, dx}{3^x + 1} \quad \text{....(ii)} \]

(i) + (ii)

\[ 2I = \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \cos^2 x \, dx = 2\int_{0}^{\frac{\pi}{2}} -\cos^2 x \, dx \]

\[ I = \int_{0}^{\frac{\pi}{2}} \cos^2 x \, dx \quad \text{....(iii)} \]

\[ I = \int_{0}^{\frac{\pi}{2}} \sin^2 x \, dx \quad \text{....(iii)} \]

(iii) + (iv)

\[ 2I = \int_{0}^{\frac{\pi}{2}} 1 \, dx = \frac{\pi}{2} \]

\[ I = \frac{\pi}{4} \]

**Question:** The sum of the infinite values of \( 1 + \frac{2}{3} + \frac{7}{3^2} + \frac{12}{3^3} \ldots \infty \)

**Options:**
(a) 
(b) 
(c) 
(d) 
**Answer:** ()

**Solution:**
\[ S = 1 + \frac{2}{3} + \frac{7}{3^2} + \frac{12}{3^3} + \ldots + \infty \]  
... (i)

\[ \frac{1}{3} S = \frac{1}{3} + \frac{2}{3^2} + \frac{7}{3^3} + \ldots + \infty \]  
... (ii)

(i) − (ii)

\[ \frac{2}{3} S = 1 + \frac{1}{3} + \frac{5}{3^2} + \frac{5}{3^3} + \ldots \]

\[ = \frac{4}{3} + \frac{\frac{5}{3^2}}{1 - \frac{1}{3}} \]

\[ \frac{2}{3} S = \frac{4}{3} + \frac{5}{3^2} + \frac{5}{3^3} + \ldots \]

\[ \Rightarrow S = 2 + \frac{5}{4} = \frac{13}{4} \]

**Question:** Growth of bacteria is directly proportional to number of bacteria. At \( t = 0 \), number of bacteria = 1000 and after 2 hours population is increased by 20%. After this population becomes 2000 where \( t = \frac{k}{\ln\left(\frac{6}{5}\right)} \). Find value of \( \left(\frac{k}{\ln 2}\right)^2 \).

**Options:**
(a) 4 
(b) 8 
(c) 16 
(d) 32 

**Answer:** (a)

**Solution:**

Let, number of bacteria = \( N \)

\[ \frac{dN}{dt} \propto N \]

\[ \frac{dN}{dt} = aN \]

\[ \int \frac{dN}{N} = a \int dt \]

\[ \log N = at + C \]

At \( t = 0 \), \( N = 1000 \) \( \Rightarrow C = \log 1000 \)

At \( t = 2 \), \( N = 1200 \) \( \Rightarrow C = \log 1000 \)

\[ \Rightarrow \log 1200 = 2a + \log 1000 \]
\[2a = \log\left(\frac{1200}{1000}\right)\]
\[a = \frac{1}{2} \log\left(\frac{6}{5}\right)\]

At \(t = \frac{k}{\ln\left(\frac{6}{5}\right)}\), \(N = 2000\)

\[\Rightarrow \log 2000 = \frac{1}{2} \log\left(\frac{6}{5}\right) \cdot \frac{k}{\log\left(\frac{6}{5}\right)} + 1000\]

\[\Rightarrow \log\left(\frac{2000}{1000}\right) = \frac{k}{2}\]

\[\Rightarrow \frac{k}{\log 2} = 2\]

\[\Rightarrow \left(\frac{k}{\log 2}\right)^2 = 4\]

**Question:** If \(|f(x) - f(y)| \leq (x - y)^2\) \(\forall x, y \in R\) and \(f(0) = 1\), then

**Options:**

(a) \(f(x) < 0 \forall x \in R\)
(b) \(f(x) > 0 \forall x \in R\)
(c) \(f(x) = 0 \forall x \in R\)
(d) 

**Answer:** (c)

**Solution:**

\[|f(x) - f(y)| \leq (x - y)^2\]

\[\Rightarrow |f(x+h) - f(x)| \leq (x+h-x)^2\]

\[|f(x+h) - f(x)| \leq h^2\]

\[h^2 \leq f(x+h) - f(x) \leq h^2\]

\[h \leq \frac{f(x+h) - f(x)}{h} \leq h\]

\[\Rightarrow \lim_{h \to 0} (-h) \leq \lim_{h \to 0} \frac{f(x+h) - f(x)}{h} \leq \lim_{h \to 0} h\]
\[
\Rightarrow 0 \leq f'(x) \leq 0 \\
\Rightarrow f'(x) = 0 \\
\Rightarrow f(x) = \text{constant}
\]

\[
\therefore f(0) = 1 \\
\therefore f(x) = 1 \quad \forall x \in R
\]

**Question:** A coin is flipped ‘n’ times. Probability of seven heads is equal to probability of nine heads. What is probability of getting exactly 2 heads

**Options:**
(a) \( \frac{15}{2^{13}} \)
(b) \( \frac{15}{2^{16}} \)
(c) \( \frac{15}{2^{12}} \)
(d) none

**Answer:** (a)

**Solution:**
Let \( n \) be total no. of tosses

\( x \)-number of times head occurs

\[
\therefore p = \frac{1}{2} = q
\]

\( P(7) = P(9) \)

\[
\binom{n}{7} \left( \frac{1}{2} \right)^7 \left( \frac{1}{2} \right)^{n-7} = \binom{n}{9} \left( \frac{1}{2} \right)^9 \left( \frac{1}{2} \right)^{n-9}
\]

\[
\therefore C_7 = C_9
\]

\[
\Rightarrow n = 7 + 9 = 16
\]

\[
P(2) = \binom{16}{2} \left( \frac{1}{2} \right)^2 \left( \frac{1}{2} \right)^{14} = \frac{16 \times 15}{2 \times 2^{16}} = \frac{15}{2^{13}}
\]

**Question:** How many 7 digit numbers can be made using 1, 2, 3 such that its sum of digits is 10

**Options:**
(a) 77
(b) 76
(c) 78
(d) 80
Answer: (a)
Solution:
2 ways of having sum 10 using these digits
{3, 2, 1, 1, 1, 1, 1} or {2, 2, 2, 1, 1, 1, 1}

\[
\frac{7!}{5!} + \frac{7!}{3!4!}
\]
\[
= 42 + \frac{7 \times 6 \times 5}{6}
\]
\[
= 42 + 35
\]
\[
= 77
\]

Question: The value of \( \sum_{n=1}^{100} e^{x-[x]} dx = \)

Options:
(a) \(100(e-1)\)
(b) \(100e\)
(c) \(100(1+e)\)
(d) \(100(1-e)\)

Answer: (a)
Solution:
\[
\int_{0}^{T} f(x) dx = n \int_{0}^{T} f(x) dx
\]

Here \(x-[x] = \{x\}\)

\(\{x\}\) has period 1

\(I = \int_{0}^{100} e^{x} dx\)

\[
= \int_{0}^{1} e^x + \int_{1}^{2} e^{x-1}
\]

\[
= 100 \left[ e^x \right]_{0}^{1} = 100 \left[ e^1 - e^0 \right]
\]
\[
= 100(e - 1)
\]
\[
= 100(e - 1)
\]
**Question:** OA = 1, OB = 13 Find area of Δ PQB

**Options:**
(a) $24\sqrt{3}$
(b) $24\sqrt{2}$
(c) $26\sqrt{3}$
(d) $26\sqrt{2}$

**Answer:** (a)

**Solution:**

\[ x^2 + 5.5^2 = 6.5^2 \]
\[ x^2 = 12 \]
\[ x = 2\sqrt{3} \]

Area $\Delta PQB = \frac{1}{2} \times 12 \times 2 \times 2\sqrt{3}$
\[ = 24\sqrt{3} \]

**Question:** $3\cos x + 2\sin x = k + 1$ then set integral values of $k$.

**Options:**
(a)
(b)
(c) (d)
Answer: ()
Solution:
\[-\sqrt{3^2 + 2^2} \leq k + 1 \leq \sqrt{3^2 + 2^2}\]
\[\sqrt{13} - 1 \leq k \leq \sqrt{13} - 1\]
So, integral values of k are
-4, -3, -2, -1, 0, 1, 2

Question:
\[\frac{\sin^{-1}(x)}{a} = \frac{\cos^{-1}(x)}{b} = \frac{\tan^{-1}(y)}{c}\]
value of \[\frac{\pi c}{a + b}\]
Options:
(a) \[\frac{1 - y}{1 + y}\]
(b) \[\frac{1 - y^2}{1 + y^2}\]
(c) \[\frac{2y}{1 + y^2}\]
(d) 
Answer: (b)
Solution:
\[\frac{\sin^{-1} x}{a} = \frac{\cos^{-1} x}{b} = \frac{\tan^{-1} y}{c}\]
\[\Rightarrow \frac{\sin^{-1} x + \cos^{-1} x}{a + b} = \frac{\tan^{-1} y}{c}\]
\[\Rightarrow \frac{\tan^{-1} y}{x} = \frac{\pi}{2(a + b)}\]
\[\Rightarrow 2 \tan^{-1} y = \frac{\pi c}{(a + b)}\]
\[\Rightarrow \cos \left(\frac{\pi c}{a + b}\right) = \cos \left(2 \tan^{-1} y\right)\]
\[= \frac{1 - \tan^2 \left(\tan^{-1} y\right)}{1 + \tan^2 \left(\tan^{-1} y\right)}\]
\[= \frac{1 - y^2}{1 + y^2}\]
Question: \( e^{\sin y} \cos y \frac{dy}{dx} + e^{\sin y} \cos x = \cos x \)

Options:
(a)
(b)
(c)
(d)

Answer: ()
Solution:

\[
e^{\sin y} \cos y \frac{dy}{dx} + e^{\sin y} \cos x = \cos x
\]

Put \( e^{\sin y} = t \) \( \Rightarrow \) \( e^{\sin y} \cos \frac{dy}{dx} = \frac{dt}{dx} \)

So, \( \frac{dt}{dx} + t \cos x = \cos x \)

\[ I.F = e^{\int \cos x \, dx} = e^{\sin x} \]

Hence, solution is

\[ t(e^{\sin x}) = \int \cos x \cdot e^{\sin x} \, dx + c \]

\[ e^{\sin y} e^{\sin x} = e^{\sin x} + c \]

\[ e^{\sin y} = 1 + ce^{-\sin x} \]

Question: \( \lim_{h \to 0} \frac{\sqrt{3} \sin \left( \frac{h + \frac{\pi}{6}}{6} \right) - \cos \left( h + \frac{\pi}{6} \right)}{h \left( \sqrt{3} \cosh - \sinh \right)} \)

Options:
(a)
(b)
(c)
(d)

Answer: ()
Solution:

\[
\lim_{h \to 0} \frac{\frac{\sqrt{3}}{2} \sin \left( h + \frac{\pi}{6} \right) - \frac{1}{2} \cos \left( h + \frac{\pi}{6} \right)}{h \left( \frac{\sqrt{3}}{2} \cosh - \frac{1}{2} \sinh \right)}
\]

\[
\lim_{h \to 0} \frac{\cos \left( h + \frac{\pi}{6} \right) - \sin \left( h + \frac{\pi}{6} \right)}{h \left( \sin \frac{\pi}{3} \cos h - \cos \frac{\pi}{3} \sin h \right)}
\]
\[
\lim_{h \to 0} 2 \cdot \frac{\sin \left( h + \frac{\pi}{6} - \frac{\pi}{6} \right)}{h \cdot \sin \left( \frac{\pi}{3} - h \right)}
\]

\[
\lim_{h \to 0} \frac{2 \cdot 1}{\sin \frac{\pi}{3}} = \frac{2 \cdot \frac{1}{\sqrt{3}}}{2} = \frac{4}{\sqrt{3}}
\]

**Question:** Find maximum value of term independent of ‘t’ in \( \left( \frac{\frac{1}{t}x^3 + \left(1-x\right)^{\frac{1}{10}}}{} \right)^t \), \( x \in (0, 1) \)

**Options:**
(a)
(b)
(c)
(d)

**Answer:** ()

**Solution:**
\[
{^{10}}C_r \left( \frac{1}{t}x^3 \right)^{10-r} \left(1-r\right)^{\frac{r}{t}} t^{-r}
\]

For term Independent of t

\[10 - 2r = 0\]

\[r = 5\]

\[T_6 = {^{10}}C_5 \frac{x^1 \times \left(1-x\right)^{\frac{1}{2}}}{t^5}\]

Let \( T_6 = f(x) = {^{10}}C_5 x \sqrt{1-x} \)

\[f'(x) = {^{10}}C_5 \left( \sqrt{1-x} - \frac{x}{2\sqrt{1-x}} \right)\]

\[f''(x) = {^{10}}C_5 \left( \frac{2 - 2x - x}{2\sqrt{1-x}} \right)\]

\[f''(x) = 0 \Rightarrow x = \frac{2}{3}\]

\[T_6 = {^{10}}C_5 \frac{2}{3} \left( \frac{1}{3} \right)\]

**Question:** \( \int_{\frac{\pi}{6}}^{\frac{\pi}{3}} |\sin 2x| \, dx = ? \)

**Answer:** 2.00

**Solution:**
Let \( 2x = t \)
\[ \Rightarrow dx = \frac{dt}{2} \]

\[ x = 0, t = 0 \]
\[ x = \pi, t = 2\pi \]

\[ I = \int_{0}^{2\pi} |\sin t| \frac{dt}{2} \]

\[ \Rightarrow \int_{0}^{2\pi} |\sin t| dt = 4 \int_{0}^{\pi/2} \sin t dt \]

\[ = 4.1 \]
\[ I = \frac{4}{2} = 2 \]

**Question:** If A is a \( 2 \times 2 \) symmetric matrix with integer elements. \( tr(A^2) = 1. \) Find the number of such matrices of A

**Answer:** 4.00

**Solution:**

\[ A = \begin{bmatrix} a & b \\ b & c \end{bmatrix} \]

\[ A^2 = \begin{bmatrix} a & b \\ b & c \end{bmatrix} \begin{bmatrix} a & b \\ b & c \end{bmatrix} = \begin{bmatrix} a^2 + b^2 & ab + bc \\ ab + bc & b^2 + c^2 \end{bmatrix} \]

\[ tr(A^2) = 1 \]

\[ \Rightarrow a^2 + b^2 + b^2 + c^2 = 1 \]
\[ a^2 + c^2 + 2b^2 = 1 \]

\[ \therefore a, b, c \in I \]

\[ \therefore b = 0 \]

\[ \Rightarrow a^2 + c^2 = 1 \]

Now, \( (a, c) \) can be \((1, 0), (-1, 0), (0, 1), (0, -1)\)

Hence, number of such matrices \( A = 4 \)
Question: The value of
\[
\begin{vmatrix}
(a+1)(a+2) & a+2 & 1 \\
(a+2)(a+3) & a+3 & 1 \\
(a+3)(a+4) & a+4 & 1 \\
\end{vmatrix}
\]

Answer: -2.00

Solution:

\[
R_3 \rightarrow R_3 - R_2, R_2 \rightarrow R_2 - R_1
\]

\[
\begin{vmatrix}
(a+1)(a+2) & a+2 & 1 \\
2(a+2) & 1 & 0 \\
2(a+3) & 1 & 0 \\
\end{vmatrix}
\]

\[
= 2a + 4 - 2a - 6 = -2
\]

Question: Find area bounded by \(y = |x - 1| - 2\) with x-axis

Answer: 4.00

Solution:
Area \( = \frac{1}{2} \times 2 \times 4 = 4 \)

**Question:** Find number of solutions of \( \sqrt{3} \cos^2 x = (\sqrt{3} - 1) \cos x + 1; \ x \in \left[ 0, \frac{\pi}{2} \right] \)

**Answer:** 1.00

**Solution:**
\[
\sqrt{3} \cos^2 x = (\sqrt{3} - 1) \cos x + 1
\]
\[
\sqrt{3} \cos^2 x - (\sqrt{3} - 1) \cos x - 1 = 0
\]
\[
(\sqrt{3} \cos x + 1)(\cos x - 1) = 0
\]

\[\cos x = 1 \quad \text{or} \quad \cos x = -\frac{1}{\sqrt{3}} \quad \text{(rejected)}\]

\[\Rightarrow \cos x = 1 \quad \therefore \ x \in \left[ 0, \frac{\pi}{2} \right] \]

\[x = 0\]

Hence, number of solution is 1

**Question:** If \( \alpha, \beta, \gamma \) are roots of \( x^3 - 2x^2 + 2x - 1 = 0 \). Find \( \alpha^{162} + \beta^{162} + \gamma^{162} \)

**Answer:** 3.00

**Solution:**
\[(x - 1)(x^2 - x + 1) = 0\]
\[\alpha = 1, \ \beta = -\omega, \ \gamma = -\omega^2\]
\[1^{162} + (-\omega)^{162} + (-\omega^2)^{162} = 1 + 1 + 1 = 3\]