If \( f \) denotes the ratio of the number of nuclei decayed \( N_d \) to the number of nuclei at \( t = 0 \) \( N_0 \) then for a collection of radioactive nuclei, the rate of change of \( f \) with respect to time is given as:

\[
[\lambda \text{ is the radioactive decay constant}]
\]

Options:

1. \( -\lambda e^{-\lambda t} \)

2. \( \lambda e^{-\lambda t} \)

3. \( \lambda (1 - e^{-\lambda t}) \)

4. \( -\lambda (1 - e^{-\lambda t}) \)
In Young’s double slit experiment, if the source of light changes from orange to blue then:

1. the intensity of the minima will increase.
2. the distance between consecutive fringes will increase.
3. the distance between consecutive fringes will decrease.
4. the central bright fringe will become a dark fringe.
Question Type: MCQ Is Question Mandatory: No

Correct Marks: 4 Wrong Marks: 1

The relative permittivity of distilled water is 81. The velocity of light in it will be:

(Given μᵣ = 1)

Options:

1. $3.33 \times 10^7$ m/s

2. $4.33 \times 10^7$ m/s

3. $5.33 \times 10^7$ m/s
4. \( 2.33 \times 10^7 \text{ m/s} \)

**Question Type**: MCQ  
**Is Question Mandatory**: No  
**Correct Marks**: 4  
**Wrong Marks**: 1

**Options**:

1. \( 3.33 \times 10^7 \text{ m/s} \)
2. \( 4.33 \times 10^7 \text{ m/s} \)
3. \( 5.33 \times 10^7 \text{ m/s} \)
4. \( 2.33 \times 10^7 \text{ m/s} \)
A capacitor of capacitance $C = 1 \mu F$ is suddenly connected to a battery of 100 volt through a resistance $R = 100 \Omega$. The time taken for the capacitor to be charged to get 50 V is:

[Take $\ln 2 = 0.69$]

**Options:**

1. $0.69 \times 10^{-4} \text{ s}$
2. $0.30 \times 10^{-4} \text{ s}$
3. $1.44 \times 10^{-4} \text{ s}$
4. $3.33 \times 10^{-4} \text{ s}$
A 0.07 H inductor and a 12 Ω resistor are connected in series to a 220 V, 50 Hz ac source. The approximate current in the circuit and the phase angle between current and source voltage are respectively. [Take π as \( \frac{22}{7} \)]
2. $0.88 \text{ A and } \tan^{-1}\left(\frac{11}{6}\right)$

3. $88 \text{ A and } \tan^{-1}\left(\frac{11}{6}\right)$

4. $8.8 \text{ A and } \tan^{-1}\left(\frac{6}{11}\right)$
A light cylindrical vessel is kept on a horizontal surface. Area of base is $A$. A hole of cross-sectional area $a$ is made just at its bottom side. The minimum coefficient of friction necessary to prevent sliding the vessel due to the impact force of the emerging liquid is ($a << A$):

$$\tan^{-1}\left(\frac{6}{11}\right) \approx 8.8 \, \text{A}$$

Options:

1. $\frac{a}{A}$

2. $\frac{2a}{A}$

3. $\frac{A}{2a}$

4. None of these
Question Type : MCQ Is Question Mandatory : No

Correct Marks : 4 Wrong Marks : 1

Options :

1. \( \frac{a}{A} \)
2. \( \frac{2a}{A} \)
3. \( \frac{A}{2a} \)
4. \( \text{ان مسّ كلاً كلاً} \)

Question Type : MCQ Is Question Mandatory : No

Correct Marks : 4 Wrong Marks : 1
In the given figure, a battery of emf E is connected across a conductor PQ of length ‘l’ and different area of cross-sections having radii \( r_1 \) and \( r_2 \) (\( r_2 < r_1 \)).

Choose the correct option as one moves from P to Q:

**Options:**

1. Drift velocity of electron increases.

2. Electron current decreases.

3. Electric field decreases.

4. All of these

**Question Type:** MCQ  **Is Question Mandatory:** No

**Correct Marks:** 4  **Wrong Marks:** 1
Two capacitors of capacities 2C and C are joined in parallel and charged up to potential V. The battery is removed and the capacitor of capacity C is filled completely with a medium of dielectric constant K. The potential difference across the capacitors will now be:
Options:
1. \( \frac{V}{K} \)
2. \( \frac{3V}{K} \)
3. \( \frac{V}{K + 2} \)
4. \( \frac{3V}{K + 2} \)

Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1

Options:
1. \( \frac{V}{K} \)
2. \( \frac{3V}{K} \)
3. \( \frac{V}{K + 2} \)
In the reported figure, a capacitor is formed by placing a compound dielectric between the plates of parallel plate capacitor. The expression for the capacity of the said capacitor will be: (Given area of plate = A)

\[
\frac{3V}{K + 2}
\]

Options:

1. \(\frac{25}{6} \frac{K\varepsilon_0 A}{d}\)

2. \(\frac{15}{34} \frac{K\varepsilon_0 A}{d}\)

3. \(\frac{9}{6} \frac{K\varepsilon_0 A}{d}\)

4. \(\frac{15}{6} \frac{K\varepsilon_0 A}{d}\)
Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1

Options:

1. \( \frac{25}{6} K\varepsilon_0 A \)  
2. \( \frac{15}{34} K\varepsilon_0 A \)  
3. \( \frac{9}{6} K\varepsilon_0 A \)  
4. \( \frac{15}{6} K\varepsilon_0 A \)
A particle starts executing simple harmonic motion (SHM) of amplitude ‘a’ and total energy 

E. At any instant, its kinetic energy is \( \frac{3E}{4} \) then its displacement ‘\( y \)’ is given by:

Options:

1. \( y = \frac{a}{\sqrt{2}} \)

2. \( y = \frac{a}{2} \)

3. \( y = \frac{a \sqrt{3}}{2} \)

4. \( y = a \)
3. \( y = \frac{a\sqrt{3}}{2} \)

4. \( y = a \)

Question Type: MCQ Is Question Mandatory: No

Correct Marks: 4 Wrong Marks: 1

Two identical tennis balls each having mass ‘m’ and charge ‘q’ are suspended from a fixed point by threads of length ‘l’. What is the equilibrium separation when each thread makes a small angle ‘θ’ with the vertical?

Options:

1. \( x = \left( \frac{q^2 l^2}{2\pi\varepsilon_0 m^2 g} \right)^{\frac{1}{3}} \)

2. \( x = \left( \frac{q^2 l}{2\pi\varepsilon_0 mg} \right)^{\frac{1}{3}} \)

3. \( x = \left( \frac{q^2 l}{2\pi\varepsilon_0 mg} \right)^{\frac{1}{2}} \)

4. \( x = \left( \frac{q^2 l^2}{2\pi\varepsilon_0 m^2 g^2} \right)^{\frac{1}{3}} \)
Question Type: MCQ Is Question Mandatory: No

Correct Marks: 4 Wrong Marks: 1

Options:

1. \( x = \left( \frac{q^2 l^2}{2\pi \varepsilon_0 mg} \right)^{\frac{1}{3}} \)

2. \( x = \left( \frac{q^2 l}{2\pi \varepsilon_0 m^2 g} \right)^{\frac{1}{3}} \)

3. \( x = \left( \frac{q^2 l}{2\pi \varepsilon_0 mg} \right)^{\frac{1}{2}} \)

4. \( x = \left( \frac{q^2 l^2}{2\pi \varepsilon_0 m^2 g^2} \right)^{\frac{1}{3}} \)
In the reported figure, there is a cyclic process ABCDA on a sample of 1 mol of a diatomic gas. The temperature of the gas during the process A → B and C → D are $T_1$ and $T_2$ ($T_1 > T_2$) respectively.

Choose the correct option out of the following for work done if processes BC and DA are adiabatic.

**Options:**

1. $W_{BC} + W_{DA} > 0$

2. $W_{AB} < W_{CD}$

3. $W_{AB} = W_{DC}$

4. $W_{AD} = W_{BC}$
A body takes 4 min. to cool from 61°C to 59°C. If the temperature of the surroundings is 30°C, the time taken by the body to cool from 51°C to 49°C is:
Options:

1. 3 min.
2. 4 min.
3. 6 min.
4. 8 min.

Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1

Options:

1. 3 min.
2. 4 min.
3. 6 min.
4. 8 min.

Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1
The number of molecules in one litre of an ideal gas at 300 K and 2 atmospheric pressure with mean kinetic energy $2 \times 10^{-9} \text{ J}$ per molecule is:

Options:

1. $0.75 \times 10^{11}$
2. $1.5 \times 10^{11}$
3. $3 \times 10^{11}$
4. $6 \times 10^{11}$

Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1
Assertion A: If A, B, C, D are four points on a semi-circular arc with centre at ‘O’ such that $|\overrightarrow{AB}| = |\overrightarrow{BC}| = |\overrightarrow{CD}|$, then

$$\overrightarrow{AB} + \overrightarrow{AC} + \overrightarrow{AD} = 4\overrightarrow{AO} + \overrightarrow{OB} + \overrightarrow{OC}$$

Reason R: Polygon law of vector addition yields

$$\overrightarrow{AB} + \overrightarrow{BC} + \overrightarrow{CD} = \overrightarrow{AD} = 2\overrightarrow{AO}$$

In the light of the above statements, choose the most appropriate answer from the options given below:

Options:

1. Both A and R are correct and R is the correct explanation of A.
2. Both A and R are correct but R is not the correct explanation of A.
3. A is correct but R is not correct.
4. A is not correct but R is correct.
\[ |\overrightarrow{AB}| = |\overrightarrow{BC}| = |\overrightarrow{CD}| \]

**Options:**

1. R सही है। अगर A, R और A दोनों सही हैं, तो R सही हो सकता है।
2. दोनों R सही नहीं। अगर एक ही तस्करी के भागों में R सही है, तो दोनों नहीं हो सकते।
3. दोनों R गलत नहीं हैं।
4. दोनों R सही हैं।

*Question Type: MCQ Is Question Mandatory: No*

*Correct Marks: 4 Wrong Marks: 1*
The figure shows two solid discs with radius R and r respectively. If mass per unit area is same for both, what is the ratio of MI of bigger disc around axis AB (which is \( \perp \) to the plane of the disc and passing through its centre) to MI of smaller disc around one of its diameters lying on its plane? Given ‘M’ is the mass of the larger disc. (MI stands for moment of inertia)

Options:

1. \( 2R^2 : r^2 \)
2. \( R^2 : r^2 \)
3. \( 2R^4 : r^4 \)
4. \( 2r^4 : R^4 \)
Options:

1. $2R^2 : r^2$
2. $R^2 : r^2$
3. $2R^4 : r^4$
4. $2r^4 : R^4$

Question Type: MCQ Is Question Mandatory: No

Correct Marks: 4 Wrong Marks: 1
<table>
<thead>
<tr>
<th>List - I</th>
<th>List - II</th>
</tr>
</thead>
<tbody>
<tr>
<td>(a) MI of the rod (length L, Mass M, about an axis ⊥ to the rod</td>
<td>(i) $8 \frac{ML^2}{3}$</td>
</tr>
<tr>
<td>passing through the midpoint)</td>
<td></td>
</tr>
<tr>
<td>(b) MI of the rod (length L, Mass 2M, about an axis ⊥ to the rod</td>
<td>(ii) $\frac{ML^2}{3}$</td>
</tr>
<tr>
<td>passing through one of its end)</td>
<td></td>
</tr>
<tr>
<td>(c) MI of the rod (length 2L, Mass M, about an axis ⊥ to the rod</td>
<td>(iii) $\frac{ML^2}{12}$</td>
</tr>
<tr>
<td>passing through its midpoint)</td>
<td></td>
</tr>
<tr>
<td>(d) MI of the rod (length 2L, Mass 2M, about an axis ⊥ to the rod</td>
<td>(iv) $2 \frac{ML^2}{3}$</td>
</tr>
<tr>
<td>passing through one of its end)</td>
<td></td>
</tr>
</tbody>
</table>

Choose the **correct** answer from the options given below:

**Options:**

1. (a)-(iii), (b)-(iv), (c)-(i), (d)-(ii)

2. (a)-(iii), (b)-(iv), (c)-(ii), (d)-(i)

3. (a)-(ii), (b)-(i), (c)-(iii), (d)-(iv)

4. (a)-(ii), (b)-(iii), (c)-(i), (d)-(iv)

**Question Type:** MCQ  **Is Question Mandatory:** No

**Correct Marks:** 4  **Wrong Marks:** 1
8 ML²/3  (i) ایک سلیول کا جوہری گوشت (لیپلی)، لیکن میں اورانس کو میں اطراف (a) جہاں کے دو پائین افزودنے کا لیپلی تازہ ہو جاتا ہے۔

ML²/3  (ii) ایک سلیول کا جوہری گوشت (لیپلی)، لیکن 2 میں اورانس کو میں اطراف (b) جہاں کے دو پائین افزودنے کا لیپلی تازہ ہو جاتا ہے۔

ML²/12  (iii) ایک سلیول کا جوہری گوشت (لیپلی)، لیکن 2 2 میں اورانس کو میں اطراف (c) جہاں کے دو پائین افزودنے کا لیپلی تازہ ہو جاتا ہے۔

2 ML²/3  (iv) ایک سلیول کا جوہری گوشت (لیپلی)، لیکن 2 2 میں اورانس کو میں اطراف (d) جہاں کے دو پائین افزودنے کا لیپلی تازہ ہو جاتا ہے۔

Options :
1. (a)-(iii), (b)-(iv), (c)-(i), (d)-(ii)
2. (a)-(iii), (b)-(iv), (c)-(ii), (d)-(i)
3. (a)-(ii), (b)-(i), (c)-(iii), (d)-(iv)
4. (a)-(ii), (b)-(iii), (c)-(i), (d)-(iv)
Three objects A, B and C are kept in a straight line on a frictionless horizontal surface. The masses of A, B and C are m, 2m and 2m respectively. A moves towards B with a speed of 9 m/s and makes an elastic collision with it. Thereafter B makes a completely inelastic collision with C. All motions occur along same straight line. The final speed of C is:

Options:
1. 6 m/s
2. 3 m/s
3. 4 m/s
4. 9 m/s
A ball is thrown up with a certain velocity so that it reaches a height \( h \). Find the ratio of the two different times of the ball reaching \( \frac{h}{3} \) in both the directions.

Options:

1. \( \frac{\sqrt{3} - \sqrt{2}}{\sqrt{3} + \sqrt{2}} \)
2. \( \frac{\sqrt{3} - 1}{\sqrt{3} + 1} \)
3. \( \frac{1}{3} \)
4. \( \frac{\sqrt{2} - 1}{\sqrt{2} + 1} \)
The question is in Hindi. It is about a geometric problem involving a triangle. The correct answer is provided in the options, which are given as mathematical expressions. The options are:

1. $\frac{\sqrt{3} - \sqrt{2}}{\sqrt{3} + \sqrt{2}}$
2. $\frac{\sqrt{3} - 1}{\sqrt{3} + 1}$
3. $\frac{1}{3}$
4. $\frac{\sqrt{2} - 1}{\sqrt{2} + 1}$
Assertion A: If in five complete rotations of the circular scale, the distance travelled on main scale of the screw gauge is 5 mm and there are 50 total divisions on circular scale, then least count is 0.001 cm.

Reason R: Least Count = \[
\frac{\text{Pitch}}{\text{Total divisions on circular scale}}
\]

In the light of the above statements, choose the most appropriate answer from the options given below:

Options:
1. Both A and R are correct and R is the correct explanation of A.
2. Both A and R are correct and R is NOT the correct explanation of A.
3. A is correct but R is not correct.
4. A is not correct but R is correct.

Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1
Options:

1. اور A ر دو لا گی چیز اور R کی جت وضاحت کرتی ہے۔

2. اور A ر دو لا گی چیز اور R کی جت وضاحت کرتی ہے۔

3. صحیح ہے۔ صحیح ہے۔

4. صحیح ہے۔ صحیح ہے۔

Physics Section B

Section Id: 864351825
Section Number: 2
Section type: Online
Mandatory or Optional: Mandatory
Number of Questions: 10
Number of Questions to be attempted: 5
Section Marks: 20
Enable Mark as Answered Mark for Review and Clear Response: Yes
Sub-Section Number: 1
Sub-Section Id: 8643511052
Question Shuffling Allowed: Yes
Question Type: SA
Suppose two planets (spherical in shape) of radii R and 2R, but mass M and 9M respectively have a centre to centre separation 8R as shown in the figure. A satellite of mass ‘m’ is projected from the surface of the planet of mass ‘M’ directly towards the centre of the second planet. The minimum speed ‘v’ required for the satellite to reach the surface of the second planet is \( \sqrt{\frac{aGM}{R}} \) then the value of ‘a’ is _______.

[Given: The two planets are fixed in their position]
In a uniform magnetic field, the magnetic needle has a magnetic moment $9.85 \times 10^{-2}$ A/m² and moment of inertia $5 \times 10^{-6}$ kg m². If it performs 10 complete oscillations in 5 seconds then the magnitude of the magnetic field is _______ mT. [Take $\pi^2$ as 9.85]
Response Type: Numeric
Evaluation Required For SA: Yes
Show Word Count: Yes
Answers Type: Equal
Text Areas: PlainText Possible

Answers:
1

Question Type: SA
Correct Marks: 4 Wrong Marks: 0

Response Type: Numeric
Evaluation Required For SA: Yes
Show Word Count: Yes
Answers Type: Equal
Text Areas: PlainText Possible

Answers:
1

Question Type: SA
Correct Marks: 4 Wrong Marks: 0
A stone of mass 20 g is projected from a rubber catapult of length 0.1 m and area of cross section $10^{-6} \text{ m}^2$ stretched by an amount 0.04 m. The velocity of the projected stone is _______ m/s.

($\text{Young's modulus of rubber} = 0.5 \times 10^9 \text{ N/m}^2$)

**Response Type**: Numeric

**Evaluation Required For SA**: Yes

**Show Word Count**: Yes

**Answers Type**: Equal

**Text Areas**: PlainText Possible

**Answers**:

1
A transistor is connected in common emitter circuit configuration, the collector supply voltage is 10 V and the voltage drop across a resistor of 1000 Ω in the collector circuit is 0.6 V. If the current gain factor (β) is 24, then the base current is ________ μA. (Round off to the Nearest Integer)

Response Type : Numeric
Evaluation Required For SA : Yes
Show Word Count : Yes
Answers Type : Equal
Text Areas : PlainText Possible
Answers :

1

Question Type : SA
Correct Marks : 4 Wrong Marks : 0

Response Type : Numeric
Evaluation Required For SA : Yes
Show Word Count : Yes
Answers Type : Equal
Text Areas : PlainText Possible
Answers :

1

Question Type : SA
A prism of refractive index $n_1$ and another prism of refractive index $n_2$ are stuck together (as shown in the figure). $n_1$ and $n_2$ depend on $\lambda$, the wavelength of light, according to the relation

$$n_1 = 1.2 + \frac{10.8 \times 10^{-14}}{\lambda^2} \text{ and } n_2 = 1.45 + \frac{1.8 \times 10^{-14}}{\lambda^2}$$

The wavelength for which rays incident at any angle on the interface BC pass through without bending at that interface will be ________ nm.
Response Type: Numeric

Evaluation Required For SA: Yes

Show Word Count: Yes

Answers Type: Equal

Text Areas: PlainText Possible

Answers:

1

Question Type: SA

Correct Marks: 4 Wrong Marks: 0

A particle of mass $9.1 \times 10^{-31}$ kg travels in a medium with a speed of $10^6$ m/s and a photon of a radiation of linear momentum $10^{-27}$ kg m/s travels in vacuum. The wavelength of photon is _______ times the wavelength of the particle.
A radioactive sample has an average life of 30 ms and is decaying. A capacitor of capacitance 200 \( \mu \text{F} \) is first charged and later connected with resistor \( R \). If the ratio of charge on capacitor to the activity of radioactive sample is fixed with respect to time then the value of \( R \) should be ________ \( \Omega \).
Evaluation Required For SA : Yes

Show Word Count : Yes

Answers Type : Equal

Text Areas : PlainText Possible

Answers :

1

Question Type : SA

Correct Marks : 4 Wrong Marks : 0

In Bohr’s atomic model, the electron is assumed to revolve in a circular orbit of radius 0.5 Å. If the speed of electron is $2.2 \times 10^6$ m/s, then the current associated with the electron will be

$\frac{22}{7} \times 10^{-2}$ mA. [Take $\pi$ as $\frac{22}{7}$]
Response Type: Numeric
Evaluation Required For SA: Yes
Show Word Count: Yes
Answers Type: Equal
Text Areas: PlainText Possible
Answers: 1

Question Type: SA
Correct Marks: 4 Wrong Marks: 0

$2.2 \times 10^6 \times \frac{22/2}{7} \text{ m/s}$

Response Type: Numeric
Evaluation Required For SA: Yes
Show Word Count: Yes
Answers Type: Equal
Text Areas: PlainText Possible
Answers: 1

Question Type: SA
Correct Marks: 4 Wrong Marks: 0
Consider an electrical circuit containing a two way switch ‘S’. Initially S is open and then T₁ is connected to T₂. As the current in R = 6 Ω attains a maximum value of steady state level, T₁ is disconnected from T₂ and immediately connected to T₃. Potential drop across r = 3 Ω resistor immediately after T₁ is connected to T₃ is ________ V. (Round off to the Nearest Integer)

Response Type: Numeric
Evaluation Required For SA: Yes
Show Word Count: Yes
Answers Type: Equal
Text Areas: PlainText Possible

Answers:

1

Question Type: SA
Correct Marks: 4 Wrong Marks: 0
The amplitude of upper and lower side bands of A.M. wave where a carrier signal with frequency 11.21 MHz, peak voltage 15 V is amplitude modulated by a 7.7 kHz sine wave of 5 V amplitude are \( \frac{a}{10} \) V and \( \frac{b}{10} \) V respectively. Then the value of \( \frac{a}{b} \) is ________.
Chemistry Section A

Section Id : 864351826
Section Number : 3
Section type : Online
Mandatory or Optional : Mandatory
The parameters of the unit cell of a substance are $a=2.5$, $b=3.0$, $c=4.0$, $\alpha=90^\circ$, $\beta=120^\circ$, $\gamma=90^\circ$. The crystal system of the substance is:

Options:

1. Triclinic
2. Hexagonal
3. Orthorhombic
4. Monoclinic
Given below are two statements:

Statement I: Rutherford’s gold foil experiment cannot explain the line spectrum of hydrogen atom.

Statement II: Bohr’s model of hydrogen atom contradicts Heisenberg’s uncertainty principle.

In the light of the above statements, choose the most appropriate answer from the options given below:

Options:
1. Both statement I and statement II are true.

2. Both statement I and statement II are false.

3. Statement I is true but statement II is false.

4. Statement I is false but statement II is true.

Question Type : MCQ Is Question Mandatory : No
Correct Marks : 4 Wrong Marks : 1

Options :

1. दोनों सत्य हैं - I और II सत्य हैं

2. दोनों सत्य नहीं - I और II गलत हैं

3. सत्य है - I और गलत है - II

4. गलत है - I और सत्य है - II
For a reaction of order \( n \), the unit of the rate constant is:

Options:

1. \( \text{mol}^{1-n} \text{L}^{1-n} \text{s}^{-1} \)

2. \( \text{mol}^{1-n} \text{L}^{1-n} \text{s} \)

3. \( \text{mol}^{1-n} \text{L}^{2n} \text{s}^{-1} \)

4. \( \text{mol}^{1-n} \text{L}^{n-1} \text{s}^{-1} \)
Match List - I with List - II:

<table>
<thead>
<tr>
<th>List - I</th>
<th>List - II</th>
</tr>
</thead>
<tbody>
<tr>
<td>(a) NaOH</td>
<td>(i) Acidic</td>
</tr>
<tr>
<td>(b) Be(OH)_2</td>
<td>(ii) Basic</td>
</tr>
<tr>
<td>(c) Ca(OH)_2</td>
<td>(iii) Amphoteric</td>
</tr>
<tr>
<td>(d) B(OH)_3</td>
<td></td>
</tr>
<tr>
<td>(e) Al(OH)_3</td>
<td></td>
</tr>
</tbody>
</table>

Choose the most appropriate answer from the options given below:

Options:

1. (a)-(ii), (b)-(i), (c)-(ii), (d)-(iii), (e)-(iii)
2. (a)-(ii), (b)-(ii), (c)-(iii), (d)-(i), (e)-(iii)
3. (a)-(ii), (b)-(iii), (c)-(ii), (d)-(i), (e)-(iii)
4. (a)-(ii), (b)-(ii), (c)-(iii), (d)-(ii), (e)-(iii)
The statement that is INCORRECT about Ellingham diagram is:

Options:
1. provides idea about reduction of metal oxide.

2. provides idea about the reaction rate.

3. provides idea about free energy change.

4. provides idea about changes in the phases during the reaction.
The product obtained from the electrolytic oxidation of acidified sulphate solutions, is:

Options:
1. $\text{HO}_2\text{SOSO}_3\text{H}$
2. $\text{HO}_2\text{SOSO}_2\text{H}$
3. $\text{HO}_3\text{SOOSO}_3\text{H}$
4. $\text{HSO}_4^-$

Question Type: MCQ  Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1

The product obtained from the electrolytic oxidation of acidified sulphate solutions, is:

Options:
1. $\text{HO}_3\text{SOOSO}_3\text{H}$
2. $\text{HO}_2\text{SOSO}_2\text{H}$
3. $\text{HO}_3\text{SOOSO}_3\text{H}$
4. $\text{HSO}_4^-$

Question Type: MCQ  Is Question Mandatory: No
Given below are two statements: One is labelled as Assertion A and the other is labelled as Reason R.

**Assertion A:** Lithium halides are somewhat covalent in nature.

**Reason R:** Lithium possess high polarisation capability.

In the light of the above statements, choose the most appropriate answer from the options given below:

**Options:**

1. Both A and R are true and R is the correct explanation of A
2. Both A and R are true but R is NOT the correct explanation of A
3. A is true but R is false
4. A is false but R is true
The oxidation states of ‘P’ in \( \text{H}_4\text{P}_2\text{O}_7 \), \( \text{H}_4\text{P}_2\text{O}_5 \) and \( \text{H}_4\text{P}_2\text{O}_6 \), respectively, are:

Options:

1. 6, 4 and 5
2. 5, 4 and 3
3. 5, 3 and 4
4. 7, 5 and 6
Correct Marks : 4 Wrong Marks : 1

\[ \text{Options :} \]

1. 4, 6
2. 3, 4, 5
3. 3, 5
4. 5, 7

**Question Type : MCQ Is Question Mandatory : No**

Correct Marks : 4 Wrong Marks : 1

The type of hybridisation and magnetic property of the complex \([\text{MnCl}_6]^{3-}\), respectively, are:

**Options :**

1. \(d^2sp^3\) and paramagnetic
2. \(sp^3d^2\) and diamagnetic
3. \(sp^3d^2\) and paramagnetic
4. \(d^2sp^3\) and diamagnetic
**Question Type : MCQ Is Question Mandatory : No**

**Correct Marks : 4 Wrong Marks : 1**

The number of geometrical isomers found in the metal complexes [PtCl₂(NH₃)₂], [Ni(CO)₄], [Ru(H₂O)₃Cl₃] and [CoCl₂(NH₃)₄]⁺ respectively, are:

**Options :**

1. 1, 1, 1, 1
2. 2, 0, 2, 2
3. 2, 1, 2, 1
4. 2, 1, 2, 2
Question Type : MCQ Is Question Mandatory : No

Correct Marks : 4 Wrong Marks : 1

\[ \text{[CoCl}_2\text{(NH}_3\text{)}_4]^{+} \quad \text{[Ru(H}_2\text{O})_3\text{Cl}_3]^- \quad \text{[Ni(CO)}_4\text{]} \quad \text{[PtCl}_2\text{(NH}_3\text{)}_2] \quad \text{(complexes)} \]

Options :

1. 1, 1, 1, 1
2. 2, 0, 2, 2
3. 2, 1, 2, 1
4. 2, 1, 2, 2

Question Type : MCQ Is Question Mandatory : No

Correct Marks : 4 Wrong Marks : 1

Which one of the following statements is NOT correct?

Options :

1. The dissolved oxygen concentration below 6 ppm inhibits fish growth
2. Eutrophication indicates that water body is polluted
3. Eutrophication leads to increase in the oxygen level in water
4. Eutrophication leads to anaerobic conditions

Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1
Options:
1. "Eutrophication" (Eutrophication)
2. "(anaerobic)" (anaerobic)
3. Seliwanoff’s test
4. Barfoed test
3. Tollen’s test

4. Iodine test

Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1
Options:
1. (Seliwanoff’s test)
2. (Barfoed test)
3. (Tollen’s test)
4. (Iodine test)

Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1
Staggered and eclipsed conformers of ethane are:
Options:
1. Rotamers
2. Mirror images

3. Enantiomers

4. Polymers

Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1
Options:

1. (Rotamers)
2. (Mirror images)
3. (Enantiomers)
4. (Polymers)
The correct order of stability of given carbocations is:

Options:
1. D > B > C > A
2. A > C > B > D
3. C > A > D > B
4. D > B > A > C

Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1
2. A > C > B > D

3. C > A > D > B

4. D > B > A > C

Presence of which reagent will affect the reversibility of the following reaction, and change it to an irreversible reaction:

\[
\text{CH}_4 + I_2 \xrightleftharpoons{\text{Reversible}}^{\text{hv}} \text{CH}_3I + HI
\]

Options:

1. Concentrated HIO$_3$

2. HOCI

3. Liquid NH$_3$

4. Dilute HNO$_2$
Which one of the following compounds will give orange precipitate when treated with 2,4-dinitrophenyl hydrazine?

Options:

1. ![Chemical Structure](image1.png)
2. 

3. 

4. 

Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1

Options:

1. 

(premitate) 2,4-dinitrophenyl hydrazine  نیلا کا کان سیم کرکب (2,4-dinitrophenyl hydrazine) گینما؟

ولی؟
2. 

3. 

4. 

Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1

Consider the above reaction and identify the Product P:

Options:
1. 

2. 

3. 

4. 

Question Type: MCQ Is Question Mandatory: No

Correct Marks: 4 Wrong Marks: 1
Options:

1. [Chemical structure image]

2. [Chemical structure image]

3. [Chemical structure image]

4. [Chemical structure image]
Given below are two statements:

Statement I: Aniline is less basic than acetamide.

Statement II: In aniline, the lone pair of electrons on nitrogen atom is delocalised over benzene ring due to resonance and hence less available to a proton.

Choose the most appropriate option:

Options:

1. Both statement I and statement II are true.

2. Both statement I and statement II are false.

3. Statement I is true but statement II is false.

4. Statement I is false but statement II is true.
Options:

1. Statement I is correct and Statement II is incorrect.
2. Statement II is incorrect and Statement I is correct.
3. Both statements are correct.
4. Both statements are incorrect.

Question Type: MCQ
Is Question Mandatory: No
Correct Marks: 4
Wrong Marks: 1
**Match List - I with List - II:**

<table>
<thead>
<tr>
<th>List - I</th>
<th>List - II</th>
</tr>
</thead>
<tbody>
<tr>
<td>(Drug)</td>
<td>(Class of Drug)</td>
</tr>
<tr>
<td>(a) Furacin</td>
<td>(i) Antibiotic</td>
</tr>
<tr>
<td>(b) Arsphenamine</td>
<td>(ii) Tranquilizers</td>
</tr>
<tr>
<td>(c) Dimetone</td>
<td>(iii) Antiseptic</td>
</tr>
<tr>
<td>(d) Valium</td>
<td>(iv) Synthetic antihistamines</td>
</tr>
</tbody>
</table>

Choose the most appropriate match:

Options:

1. (a)-(iii), (b)-(i), (c)-(iv), (d)-(ii)

2. (a)-(i), (b)-(iii), (c)-(iv), (d)-(ii)

3. (a)-(ii), (b)-(i), (c)-(iii), (d)-(iv)

4. (a)-(iii), (b)-(iv), (c)-(ii), (d)-(i)
Options:

1. (a)-(iii), (b)-(i), (c)-(iv), (d)-(ii)

2. (a)-(i), (b)-(iii), (c)-(iv), (d)-(ii)

3. (a)-(ii), (b)-(i), (c)-(iii), (d)-(iv)

4. (a)-(iii), (b)-(iv), (c)-(ii), (d)-(i)

Question Type: MCQ
Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1
The compound ‘A’ is a complementary base of ________ in DNA strands.

Options:
1. Guanine
2. Adenine
3. Cytosine
4. Uracil

Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1
Options:

1. Guanine
2. Adenine
3. Cytosine
4. Uracil
The density of NaOH solution is 1.2 g cm$^{-3}$. The molality of this solution is _______ m.

(Round off to the Nearest Integer)


Density of H$_2$O: 1.0 g cm$^{-3}$]

Response Type: Numeric

Evaluation Required For SA: Yes

Show Word Count: Yes

Answers Type: Equal

Text Areas: Plaintext Possible

Answers:

1
The difference between bond orders of CO and NO$^2-$ is $\frac{x}{2}$ where $x=\ldots$. (Round off to the Nearest Integer)
Question Type : SA

Correct Marks : 4 Wrong Marks : 0

For water at 100°C and 1 bar,

\[ \Delta_vap H - \Delta_vap U = \_\times 10^2 \text{ J mol}^{-1}. \] (Round off to the Nearest Integer)

[Use : \( R = 8.31 \text{ J mol}^{-1} \text{ K}^{-1} \)]

[Assume volume of \( H_2O(l) \) is much smaller than volume of \( H_2O(g) \). Assume \( H_2O(g) \) can be treated as an ideal gas]

Response Type : Numeric

Evaluation Required For SA : Yes

Show Word Count : Yes

Answers Type : Equal

Text Areas : PlainText Possible

Answers :

1

Question Type : SA

Correct Marks : 4 Wrong Marks : 0

For water at 100°C and 1 bar,

\[ x = \frac{\text{NO}^2}{\text{CO}} \]
\Delta \text{vap} H - \Delta \text{vap} U = \, ______ \times 10^2 \text{ J mol}^{-1} \, \text{ at} \, 100^\circ \text{C} \, \text{ and} \, 1 \text{ bar} \\

\left[ R = 8.31 \text{ J mol}^{-1} \text{ K}^{-1} \right] \\
\left[ \text{Use} : \, R = 8.31 \text{ J mol}^{-1} \text{ K}^{-1} \right]

\text{Response Type : Numeric}

Evaluation Required For SA : Yes

Show Word Count : Yes

Answers Type : Equal

Answers :

1

Question Type : SA

Correct Marks : 4 Wrong Marks : 0

1.46 \text{ g} \, \text{ of a biopolymer dissolved in a 100 mL water at} \, 300 \, \text{K} \, \text{exerted an osmotic pressure of} \, 2.42 \times 10^{-3} \, \text{ bar.}

The molar mass of the biopolymer is \, \, ______ \times 10^4 \text{ g mol}^{-1}. \, (\text{Round off to the Nearest Integer})

\left[ \text{Use} : \, R = 0.083 \, \text{ L bar mol}^{-1} \text{ K}^{-1} \right]

Response Type : Numeric

Evaluation Required For SA : Yes

Show Word Count : Yes

Answers Type : Equal
1

1

1
Question Type : SA
Correct Marks : 4 Wrong Marks : 0

\[ \text{PCl}_5 \rightleftharpoons \text{PCl}_3 + \text{Cl}_2 \quad K_c = 1.844 \]

3.0 molar PCl₅ 1 L 380 K 10⁻³ × \( \times 10^{-3} \)

Response Type : Numeric
Evaluation Required For SA : Yes

Question Type : SA
Correct Marks : 4 Wrong Marks : 0

The conductivity of a weak acid HA of concentration 0.001 mol L⁻¹ is 2.0 × 10⁻⁵ S cm⁻¹. If \( \Lambda_m^0 (HA) = 190 \text{ S cm}^2 \text{ mol}^{-1} \), the ionization constant (\( K_a \)) of HA is equal to _______ × 10⁻⁶. (Round off to the Nearest Integer)

Response Type : Numeric
Evaluation Required For SA : Yes
Show Word Count: Yes

Answers Type: Equal

Text Areas: PlainText Possible

Answers:

1

Question Type: SA

Correct Marks: 4 Wrong Marks: 0

\[ \text{conductivity} = 2.0 \times 10^{-5} \text{ S cm}^{-1} \]

\[ \text{mol L}^{-1} \]

\[ K_a = \_ \times 10^{-6} \]

\[ \Lambda_m^0 (\text{HA}) = 190 \text{ S cm}^{2} \text{ mol}^{-1} \]

Response Type: Numeric

Evaluation Required For SA: Yes

Show Word Count: Yes

Answers Type: Equal

Text Areas: PlainText Possible

Answers:

1

Question Type: SA

Correct Marks: 4 Wrong Marks: 0

CO₂ gas adsorbs on charcoal following Freundlich adsorption isotherm. For a given amount of charcoal, the mass of CO₂ adsorbed becomes 64 times when the pressure of CO₂ is doubled.

The value of \( n \) in the Freundlich isotherm equation is \( \_ \times 10^{-2} \). (Round off to the Nearest Integer)

Response Type: Numeric
The number of geometrical isomers possible in triaminetrinitrocobalt (III) is $X$ and in trioxalatochromate (III) is $Y$. Then the value of $X+Y$ is ________.
Question Type: SA

Correct Marks: 4 Wrong Marks: 0

In gaseous triethyl amine the “–C=N–C–” bond angle is ________ degree.

Response Type: Numeric

Evaluation Required For SA: Yes

Show Word Count: Yes

Answers Type: Equal

Text Areas: PlainText Possible

Answers:

1
An organic compound is subjected to chlorination to get compound A using 5.0 g of chlorine. When 0.5 g of compound A is reacted with AgNO₃ [Carius Method], the percentage of chlorine in compound A is _______ when it forms 0.3849 g of AgCl. (Round off to the Nearest Integer)

(Atomic masses of Ag and Cl are 107.87 and 35.5 respectively)
1

Question Type: SA
Correct Marks: 4 Wrong Marks: 0

Mathematics Section A
Let P and Q be two distinct points on a circle which has center at \(C(2, 3)\) and which passes through origin O. If \(OC\) is perpendicular to both the line segments \(CP\) and \(CQ\), then the set \(\{P, Q\}\) is equal to:

**Options:**

1. \(\{(2 + 2\sqrt{2}, 3 + \sqrt{5}), (2 - 2\sqrt{2}, 3 - \sqrt{5})\}\)

2. \(\{(2 + 2\sqrt{2}, 3 - \sqrt{5}), (2 - 2\sqrt{2}, 3 + \sqrt{5})\}\)

3. \(\{(-1, 5), (5, 1)\}\)

4. \(\{(4, 0), (0, 6)\}\)
Options:

1. \[ \{(2 + 2\sqrt{2}, 3 + \sqrt{5}), (2 - 2\sqrt{2}, 3 - \sqrt{5})\} \]

2. \[ \{(2 + 2\sqrt{2}, 3 - \sqrt{5}), (2 - 2\sqrt{2}, 3 + \sqrt{5})\} \]

3. \[ \{(-1, 5), (5, 1)\} \]

4. \[ \{(4, 0), (0, 6)\} \]

Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1

Let \( \vec{a} = \hat{i} + \hat{j} + 2\hat{k} \) and \( \vec{b} = -\hat{i} + 2\hat{j} + 3\hat{k} \). Then the vector product

\[ (\vec{a} + \vec{b}) \times \left( (\vec{a} \times (\vec{a} - \vec{b}) \times \vec{b}) \right) \]

is equal to:

Options:

1. \[ 5\left(30 \hat{i} - 5 \hat{j} + 7 \hat{k}\right) \]

2. \[ 7\left(30 \hat{i} - 5 \hat{j} + 7 \hat{k}\right) \]

3. \[ 5\left(34 \hat{i} - 5 \hat{j} + 3 \hat{k}\right) \]

4. \[ 7\left(34 \hat{i} - 5 \hat{j} + 3 \hat{k}\right) \]
Question Type : MCQ Is Question Mandatory : No

Correct Marks : 4 Wrong Marks : 1

(vector product) \( \vec{b} = -\hat{i} + 2\hat{j} + 3\hat{k} \) \( \vec{a} = \hat{i} + \hat{j} + 2\hat{k} \)

Options :

1. \( 5\left(30\hat{i} - 5\hat{j} + 7\hat{k}\right) \)
2. \( 7\left(30\hat{i} - 5\hat{j} + 7\hat{k}\right) \)
3. \( 5\left(34\hat{i} - 5\hat{j} + 3\hat{k}\right) \)
4. \( 7\left(34\hat{i} - 5\hat{j} + 3\hat{k}\right) \)

Question Type : MCQ Is Question Mandatory : No

Correct Marks : 4 Wrong Marks : 1

If the coefficients of \( x^7 \) in \( \left(x^2 + \frac{1}{bx}\right)^{11} \) and \( x^{-7} \) in \( \left(x - \frac{1}{bx^2}\right)^{11}, \ b \neq 0 \), are equal, then the value of \( b \) is equal to:

Options :

1. \(-1\)
2.

3. \(-2\)

4. 1

Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1

\[\text{(coefficients)} x^{-7} b \neq 0 , \left( x - \frac{1}{b x^2} \right)^{11} \text{ के गुणनांक} + \ b \neq 0 , \left( x^2 + \frac{1}{bx} \right)^{11} \text{ गुणनांक} \]

Options:
1. \(-1\)
2. 2
3. \(-2\)
4. 1
If the area of the bounded region

\[ R = \left\{ (x, y) : \max\{0, \log_e x\} \leq y \leq 2^x, \frac{1}{2} \leq x \leq 2 \right\} \]

is, \( \alpha (\log_2) - 1 + \beta (\log_2) + \gamma \), then the value of \( (\alpha + \beta - 2\gamma)^2 \) is equal to:

Options:
1. 1
2. 2
3. 4
4. 8
Let \( A = \begin{bmatrix} 1 & 2 \\ -1 & 4 \end{bmatrix} \). If \( A^{-1} = \alpha I + \beta A \), \( \alpha, \beta \in \mathbb{R} \), \( I \) is a \( 2 \times 2 \) identity matrix, then \( 4(\alpha - \beta) \) is equal to:

Options:
1. 2
2. 4
3. 5
4. \( \frac{8}{3} \)
Two tangents are drawn from the point \(P(-1, 1)\) to the circle \(x^2+y^2-2x-6y+6=0\). If these tangents touch the circle at points \(A\) and \(B\), and if \(D\) is a point on the circle such that length of the segments \(AB\) and \(AD\) are equal, then the area of the triangle \(ABD\) is equal to:

Options:

1. \(2\)
2. \(4\)
3. \((3\sqrt{2} + 2)\)
4. \(3(\sqrt{2} - 1)\)
Let \( C \) be the set of all complex numbers. Let

\[ S_1 = \{ z \in C \mid |z - 3 - 2i|^2 = 8 \}, \]

\[ S_2 = \{ z \in C \mid \text{Re}(z) \geq 5 \} \]

and

\[ S_3 = \{ z \in C \mid |z - \overline{z}| \geq 8 \}. \]

Then the number of elements in \( S_1 \cap S_2 \cap S_3 \) is equal to:

Options:

1. 0

2. 1
3. Infinite

Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1

Options:
1. 0
2. 1
3. 2
4. لا يوجد
Let the plane passing through the point \((-1, 0, -2)\) and perpendicular to each of the planes 
\[2x + y - z = 2\]  
and 
\[x - y - z = 3\]  
be \(ax + by + cz + 8 = 0\). Then the value of \(a + b + c\) is equal to:

Options:
1. 5
2. 3
3. 4
4. 8

Question Type: MCQ  Is Question Mandatory: No
Correct Marks: 4  Wrong Marks: 1

Options:
1. 5
2. 3
3. 4
4. 8

Question Type: MCQ  Is Question Mandatory: No
Let $\alpha, \beta$ be two roots of the equation $x^2 + (20)^{1/4} x + (5)^{1/2} = 0$. Then $\alpha^8 + \beta^8$ is equal to:

Options:
1. 100
2. 10
3. 50
4. 160

Correct Marks: 4 Wrong Marks: 1

Question Type: MCQ Is Question Mandatory: No

Correct Marks: 4 Wrong Marks: 1

Let $\alpha, \beta$ be two roots of the equation $x^2 + (20)^{1/4} x + (5)^{1/2} = 0$. Then $\alpha^8 + \beta^8$ is equal to:

Options:
1. 100
2. 10
3. 50
4. 160

Question Type: MCQ Is Question Mandatory: No

Correct Marks: 4 Wrong Marks: 1
Let \( f : \left( -\frac{\pi}{4}, \frac{\pi}{4} \right) \to \mathbb{R} \) be defined as

\[
f(x) = \begin{cases} 
(1 + |\sin x|)^{\frac{3a}{|\sin x|}}, & -\frac{\pi}{4} < x < 0 \\
b, & x = 0 \\
e^{\cot 4x/\cot 2x}, & 0 < x < \frac{\pi}{4}
\end{cases}
\]

If \( f \) is continuous at \( x = 0 \), then the value of \( 6a + b^2 \) is equal to:

Options:
1. \( 1 + e \)
2. \( 1 - e \)
3. \( e \)
4. \( e - 1 \)
\[ f(x) = \begin{cases} 
3a
(1 + |\sin x|) & -\frac{\pi}{4} < x < 0 \\
b & x = 0 \\
6a + b^2 & 0 < x < \frac{\pi}{4} 
\end{cases} \]

Let
\[ A = \{(x, y) \in \mathbb{R} \times \mathbb{R} \mid 2x^2 + 2y^2 - 2x - 2y = 1\}, \]
\[ B = \{(x, y) \in \mathbb{R} \times \mathbb{R} \mid 4x^2 + 4y^2 - 16y + 7 = 0\} \text{ and} \]
\[ C = \{(x, y) \in \mathbb{R} \times \mathbb{R} \mid x^2 + y^2 - 4x - 2y + 5 \leq r^2\}. \]

Then the minimum value of \(|r|\) such that \(A \cup B \subseteq C\) is equal to:

Options:
1. 1 + e
2. 1 - e
3. e
4. e - 1
1. \( \frac{3 + \sqrt{10}}{2} \)

2. \( 1 + \sqrt{5} \)

3. \( \frac{2 + \sqrt{10}}{2} \)

4. \( \frac{3 + 2\sqrt{5}}{2} \)

Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1

Consider the sets:

\[ A = \{(x, y) \in \mathbb{R} \times \mathbb{R} \mid 2x^2 + 2y^2 - 2x - 2y = 1\}, \]

\[ B = \{(x, y) \in \mathbb{R} \times \mathbb{R} \mid 4x^2 + 4y^2 - 16y + 7 = 0\}, \]

\[ C = \{(x, y) \in \mathbb{R} \times \mathbb{R} \mid x^2 + y^2 - 4x - 2y + 5 \leq r^2\}. \]

It's asked to find the value of \( r \) such that \( A \cup B \subseteq C \).

Options:

1. \( \frac{3 + \sqrt{10}}{2} \)

2. \( 1 + \sqrt{5} \)
3. \( \frac{2 + \sqrt{10}}{2} \)

4. \( \frac{3 + 2\sqrt{5}}{2} \)

Question Type: MCQ Is Question Mandatory: No

Correct Marks: 4 Wrong Marks: 1

If the mean and variance of the following data:
6, 10, 7, 13, a, 12, b, 12
are 9 and \( \frac{37}{4} \) respectively, then \((a - b)^2\) is equal to:

Options:
1. 16
2. 12
3. 24
4. 32

Question Type: MCQ Is Question Mandatory: No

Correct Marks: 4 Wrong Marks: 1

\[ \frac{3}{4} \text{ ارائه مُشكلة مُقبال} \]
Let \( y = y(x) \) be solution of the differential equation \( \log_e \left( \frac{dy}{dx} \right) = 3x + 4y \), with \( y(0) = 0 \).

If \( y \left( -\frac{2}{3} \log_e 2 \right) = \alpha \log_e 2 \), then the value of \( \alpha \) is equal to:

Options:

1. \(- \frac{1}{4}\)
2. \(\frac{1}{4}\)
3. 2
4. \(- \frac{1}{2}\)
Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1

\[ y = y(x) \quad \text{given that} \quad y(0) = 0 \quad \text{and} \quad \log_e \left( \frac{dy}{dx} \right) = 3x + 4y \]

\[ y \left( -\frac{2}{3} \log_e 2 \right) = a \log_e 2 \]

Options:
1. \(-\frac{1}{4}\)
2. \(\frac{1}{4}\)
3. 2
4. \(-\frac{1}{2}\)

Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1

If \(\sin \theta + \cos \theta = \frac{1}{2}\), then \(16(\sin(2\theta) + \cos(4\theta) + \sin(6\theta))\) is equal to:

Options:
1. 23
2. \(-23\)

3. \(27\)

4. \(-27\)

Question Type : MCQ Is Question Mandatory : No

Correct Marks : 4 Wrong Marks : 1

\[
\sin\theta + \cos\theta = \frac{1}{2}
\]

Options :
1. 23
2. \(-23\)
3. 27
4. \(-27\)

Question Type : MCQ Is Question Mandatory : No

Correct Marks : 4 Wrong Marks : 1

The probability that a randomly selected 2-digit number belongs to the set \(\{ n \in \mathbb{N} : (2^n - 2) \text{ is a multiple of 3}\}\) is equal to :

Options :

\[
\frac{1}{2}
\]

1.
2. \( \frac{1}{3} \)

3. \( \frac{2}{3} \)

4. \( \frac{1}{6} \)

**Question Type:** MCQ  
**Is Question Mandatory:** No

**Correct Marks:** 4  
**Wrong Marks:** 1

\[ \text{Let } n \in \mathbb{N} : (2^n - 2) \text{ is a multiple of 3} \]

\[ \text{Find the number of 2-digit solutions.} \]

**Options:**
1. \( \frac{1}{2} \)
2. \( \frac{1}{3} \)
3. \( \frac{2}{3} \)
4. \( \frac{1}{6} \)
A ray of light through (2, 1) is reflected at a point P on the y-axis and then passes through the point (5, 3). If this reflected ray is the directrix of an ellipse with eccentricity $\frac{1}{3}$ and the distance of the nearer focus from this directrix is $\frac{8}{\sqrt{53}}$, then the equation of the other directrix can be:

Options:

1. $2x - 7y - 39 = 0$ or $2x - 7y - 7 = 0$
2. $11x + 7y + 8 = 0$ or $11x + 7y - 15 = 0$
3. $2x - 7y + 29 = 0$ or $2x - 7y - 7 = 0$
4. $11x - 7y - 8 = 0$ or $11x + 7y + 15 = 0$
1. $2x - 7y - 39 = 0$ or $2x - 7y - 7 = 0$

2. $11x + 7y + 8 = 0$ or $11x + 7y - 15 = 0$

3. $2x - 7y + 29 = 0$ or $2x - 7y - 7 = 0$

4. $11x - 7y - 8 = 0$ or $11x + 7y + 15 = 0$

The compound statement $(P \lor Q) \land (\neg P) \implies Q$ is equivalent to:

Options:

1. $\neg (P \implies Q)$

2. $P \land \neg Q$

3. $\neg (P \implies Q) \iff P \land \neg Q$

4. $P \lor Q$

The compound statement $(P \lor Q) \land (\neg P) \implies Q$ (compound statement) is:

Options:

1. $\neg (P \implies Q)$
2. \( P \land \neg Q \)

3. \( \neg(P \Rightarrow Q) \iff P \land \neg Q \)

4. \( P \lor Q \)

Let \( f : \mathbb{R} \to \mathbb{R} \) be a function such that \( f(2) = 4 \) and \( f'(2) = 1 \). Then, the value of
\[
\lim_{x \to 2} \frac{x^2 f(2) - 4 f(x)}{x - 2}
\]
is equal to:

Options:
1. 4
2. 8
3. 12
4. 16
The value of \( \lim_{n \to \infty} \frac{1}{n} \sum_{j=1}^{n} \frac{(2j - 1) + 8n}{(2j - 1) + 4n} \) is equal to:
4. \[ 3 + 2 \log_e \left( \frac{2}{3} \right) \]

Question Type: MCQ Is Question Mandatory: No
Correct Marks: 4 Wrong Marks: 1
Options:
1. \[ 5 + \log_e \left( \frac{3}{2} \right) \]
2. \[ 1 + 2 \log_e \left( \frac{3}{2} \right) \]
3. \[ 2 - \log_e \left( \frac{2}{3} \right) \]
4. \[ 3 + 2 \log_e \left( \frac{2}{3} \right) \]
The value of the definite integral
\[ \int_{-\frac{\pi}{4}}^{\frac{\pi}{4}} \frac{dx}{(1 + e^{x \cos x})(\sin^4 x + \cos^4 x)} \]
is equal to:

Options:
1. \(\frac{\pi}{2\sqrt{2}}\)
2. \(-\frac{\pi}{4}\)
3. \(-\frac{\pi}{2}\)
4. \(\frac{\pi}{\sqrt{2}}\)
2. $\frac{\pi}{4}$

3. $\frac{\pi}{2}$

4. $\frac{\pi}{\sqrt{2}}$
Let a plane $P$ pass through the point $(3, 7, -7)$ and contain the line,

\[
\frac{x - 2}{-3} = \frac{y - 3}{2} = \frac{z + 2}{1}.
\]

If distance of the plane $P$ from the origin is $d$, then $d^2$ is equal to 

\[\text{__________}.\]

**Response Type**: Numeric

**Evaluation Required For SA**: Yes

**Show Word Count**: Yes

**Answers Type**: Equal Text

**Areas**: PlainText Possible

**Answers**: 

1

**Question Type**: SA

**Correct Marks**: 4 **Wrong Marks**: 0

\[\text{Given that the plane}\ P \text{ passes through the point (3, 7, -7) and contains the line,}

\[\frac{x - 2}{-3} = \frac{y - 3}{2} = \frac{z + 2}{1},\]

\text{the distance of the plane from the origin is} \ d, \ \text{then} \ d^2 \text{ is equal to} \]

\[\text{__________}.\]

**Response Type**: Numeric

**Evaluation Required For SA**: Yes

**Show Word Count**: Yes

**Answers Type**: Equal Text

**Areas**: PlainText Possible

**Answers**: 

1

**Question Type**: SA
Let \( f(x) = \begin{vmatrix} \sin^2 x & -2 + \cos^2 x & \cos 2x \\ 2 + \sin^2 x & \cos^2 x & \cos 2x \\ \sin^2 x & \cos^2 x & 1 + \cos 2x \end{vmatrix} \), \( x \in [0, \pi] \).

Then the maximum value of \( f(x) \) is equal to _________.

Response Type: Numeric

Evaluation Required For SA: Yes

Show Word Count: Yes

Answers Type: Equal

Text Areas: PlainText Possible

Answers:

1

Question Type: SA

Correct Marks: 4 Wrong Marks: 0

\[ f(x) = \begin{vmatrix} \sin^2 x & -2 + \cos^2 x & \cos 2x \\ 2 + \sin^2 x & \cos^2 x & \cos 2x \\ \sin^2 x & \cos^2 x & 1 + \cos 2x \end{vmatrix} \]

(_maximum) (maximum) \( f(x) \) کل سب سے زیادہ

Response Type: Numeric

Evaluation Required For SA: Yes

Show Word Count: Yes

Answers Type: Equal

Text Areas: PlainText
Let $F : [3, 5] \rightarrow \mathbb{R}$ be a twice differentiable function on $(3, 5)$ such that

$$F(x) = e^{-x} \int_{3}^{x} (3t^2 + 2t + 4F(t)) \, dt.$$ 

If $F'(4) = \frac{\alpha e^\beta - 224}{(e^\beta - 4)^2}$, then $\alpha + \beta$ is equal to ________.

**Question Type**: SA

**Correct Marks**: 4 **Wrong Marks**: 0

**Response Type**: Numeric

**Evaluation Required For SA**: Yes

**Show Word Count**: Yes

**Answers Type**: Equal

**Text Areas**: PlainText Possible

**Answers**: 1

$F(x) = e^{-x} \int_{3}^{x} (3t^2 + 2t + 4F(t)) \, dt.$
Let \( \vec{a} = \hat{i} + \hat{j} + \hat{k} \), \( \vec{b} \) and \( \vec{c} = \hat{j} - \hat{k} \) be three vectors such that \( \vec{a} \times \vec{b} = \vec{c} \) and \( \vec{a} \cdot \vec{b} = 1 \). If the length of projection vector of the vector \( \vec{b} \) on the vector \( \vec{a} \times \vec{c} \) is \( l \), then the value of \( 3l^2 \) is equal to ________.

**Question Type**: SA

**Correct Marks**: 4 **Wrong Marks**: 0

**Correct Marks**: 4 **Wrong Marks**: 0
Let the domain of the function

\[ f(x) = \log_4 \left( \log_5 \left( \log_3 \left( 18x - x^2 - 77 \right) \right) \right) \] be (a, b).

Then the value of the integral

\[ \int_a^b \frac{\sin^3 x}{(\sin^3 x + \sin^3 (a + b - x))} \, dx \]

is equal to \( \boxed{1} \).
Question Type : SA
Correct Marks : 4 Wrong Marks : 0

1. Evaluate the integral: 
\[ \int_{a}^{b} \frac{\sin^3 x}{\sin^3 x + \sin^3 (a - b - x)} \, dx \]

Response Type : Numeric
Evaluation Required For SA : Yes
Show Word Count : Yes
Answers Type : Equal

Answers: 
1

Question Type : SA
Correct Marks : 4 Wrong Marks : 0

1. If \( \log_3 2, \log_3 (2^x - 5), \log_3 \left( \frac{2^x - 7}{2} \right) \) are in an arithmetic progression, then the value of \( x \) is equal to ________.

Response Type : Numeric
Evaluation Required For SA : Yes
Show Word Count : Yes
Answers Type : Equal

Answers: 

Question Type: SA

Correct Marks: 4 Wrong Marks: 0

For real numbers $\alpha$ and $\beta$, consider the following system of linear equations:

\[x + y - z = 2, \quad x + 2y + \alpha z = 1, \quad 2x - y + z = \beta.\]

If the system has infinite solutions, then $\alpha + \beta$ is equal to \[\text{__________}.\]

Response Type: Numeric

Evaluation Required For SA: Yes

Show Word Count: Yes

Answers Type: Equal

Text Areas: PlainText Possible

Answers:

1
Question Type : SA
Correct Marks : 4 Wrong Marks : 0

Let \( S = \{1, 2, 3, 4, 5, 6, 7\} \). Then the number of possible functions \( f : S \to S \) such that
\[ f(m \cdot n) = f(m) \cdot f(n) \]
for every \( m, n \in S \) and \( m \cdot n \in S \) is equal to ________.

Response Type : Numeric
Evaluation Required For SA : Yes
Show Word Count : Yes
Answers Type : Equal
Text Areas : PlainText Possible

Answers :

1
Question Type : SA

Correct Marks : 4 Wrong Marks : 0

If \( y = y(x), \quad y \in \left[ 0, \frac{\pi}{2} \right] \) is the solution of the differential equation

\[ \sec y \frac{dy}{dx} - \sin(x + y) - \sin(x - y) = 0, \] with \( y(0) = 0 \), then \( 5y'\left(\frac{\pi}{2}\right) \) is equal to ________.
Let $f: [0, 3] \to \mathbb{R}$ be defined by

$$f(x) = \min\{|x - \lfloor x \rfloor|, 1 + \lfloor x \rfloor - x|$$

where $\lfloor x \rfloor$ is the greatest integer less than or equal to $x$.

Let $P$ denote the set containing all $x \in [0, 3]$ where $f$ is discontinuous, and $Q$ denote the set containing all $x \in (0, 3)$ where $f$ is not differentiable. Then the sum of number of elements in $P$ and $Q$ is equal to _______.

Response Type: Numeric

Evaluation Required For SA: Yes
Show Word Count: Yes

Answers Type: Equal

Text Areas: PlainText Possible

Answers:

1

Question Type: SA

Correct Marks: 4 Wrong Marks: 0

$$f(x) = \min\{x - [x], 1 + [x] - x\} \quad x \in [0, 3] \to \mathbb{R}$$

Find the domain for which the function

$$f(x)$$

is continuous. Note that the function is not differentiable at points where:

$$x \in (0, 3)$$

Hence, the answer is 

$$Q, P$$

Response Type: Numeric

Evaluation Required For SA: Yes

Show Word Count: Yes

Answers Type: Equal Text

Areas: PlainText Possible

Answers:

1