

## SECTION

## 1

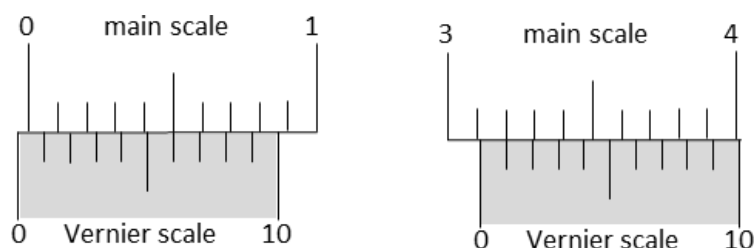
- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.

*Full Marks* : +3 If ONLY the correct option is chosen;

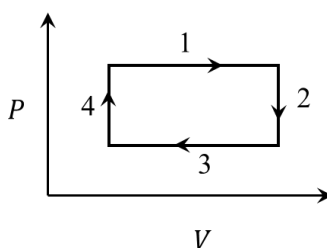
*Zero* : 0 If none of the options is chosen (i.e. the question is

*Negative Marks* : -1 unanswerd); In all other cases.

- Q.1 The smallest division on the main scale of a Vernier calipers is 0.1 cm. Ten divisions of the Vernier scale correspond to nine divisions of the main scale. The figure below on the left shows the reading of this calipers with no gap between its two jaws. The figure on the right shows the reading with a solid sphere held between the jaws. The correct diameter of the sphere is

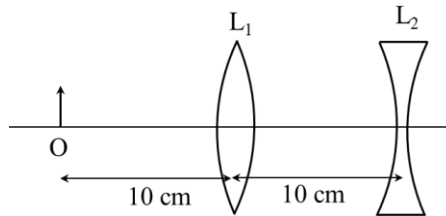


- (A) 3.07 cm      (B) 3.11 cm      (C) 3.15 cm      (D) 3.17 cm
- Q.2 An ideal gas undergoes a four step cycle as shown in the  $P - V$  diagram below. During this cycle, heat is absorbed by the gas in



- (A) steps 1 and 2      (B) steps 1 and 3  
 (C) steps 1 and 4      (D) steps 2 and 4

- Q.3 An extended object is placed at point O, 10 cm in front of a convex lens  $L_1$  and a concave lens  $L_2$  is placed 10 cm behind it, as shown in the figure. The radii of curvature of all the curved surfaces in both the lenses are 20 cm. The refractive index of both the lenses is 1.5. The total magnification of this lens system is



- (A) 0.4                      (B) 0.8                      (C) 1.3                      (D) 1.6
- Q.4 A heavy nucleus  $Q$  of half-life 20 minutes undergoes alpha-decay with probability of 60% and beta-decay with probability of 40%. Initially, the number of  $Q$  nuclei is 1000. The number of alpha-decays of  $Q$  in the first one hour is

- (A) 50                      (B) 75                      (C) 350                      (D) 525

**SECTION  
2**

- This section contains **THREE (03)** question stems.
  - There are **TWO (02)** questions corresponding to each question stem.
  - The answer to each question is a **NUMERICAL VALUE**.
  - For each question, enter the correct numerical value corresponding to the answer in the designated place using the mouse and the on-screen virtual numeric keypad.
  - If the numerical value has more than two decimal places, **truncate/round-off** the value to **TWO** decimal places.
- Answer to each question will be evaluated according to the following marking scheme:
- Full Marks* : +2 If **ONLY** the correct numerical value is entered at the designated  
*Zero* : 0 In all other

**Question Stem for Question Nos. 5 and 6**

**Question Stem**

A projectile is thrown from a point O on the ground at an angle  $45^\circ$  from the vertical and with a speed  $5\sqrt{2}$  m/s. The projectile at the highest point of its trajectory splits into two equal parts. One part falls vertically down to the ground, 0.5 s after the splitting. The other part,  $t$  seconds after the splitting, falls to the ground at a distance  $x$  meters from the point O. The acceleration due to gravity  $g = 10$  m/s<sup>2</sup>.

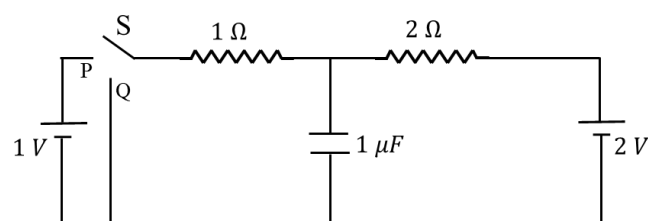
Q.5 The value of  $t$  is \_\_\_\_\_.

Q.6 The value of  $x$  is \_\_\_\_\_.

**Question Stem for Question Nos. 7 and 8**

**Question Stem**

In the circuit shown below, the switch S is connected to position P for a long time so that the charge on the capacitor becomes  $q_1$   $\mu\text{C}$ . Then S is switched to position Q. After a long time, the charge on the capacitor is  $q_2$   $\mu\text{C}$ .



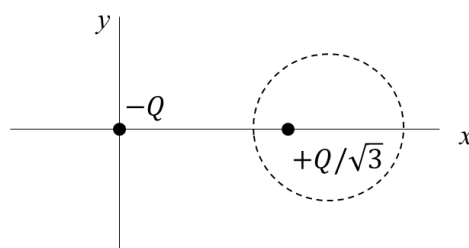
Q.7 The magnitude of  $q_1$  is \_\_\_\_\_.

Q.8 The magnitude of  $q_2$  is \_\_\_\_\_.

### Question Stem for Question Nos. 9 and 10

#### Question Stem

Two point charges  $-Q$  and  $+Q/\sqrt{3}$  are placed in the  $xy$ -plane at the origin  $(0, 0)$  and a point  $(2, 0)$ , respectively, as shown in the figure. This results in an equipotential circle of radius  $R$  and potential  $V = 0$  in the  $xy$ -plane with its center at  $(b, 0)$ . All lengths are measured in meters.



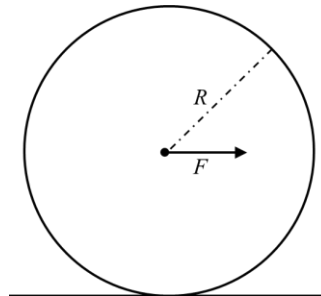
Q.9 The value of  $R$  is \_\_\_\_\_ meter.

Q.10 The value of  $b$  is \_\_\_\_\_ meter.

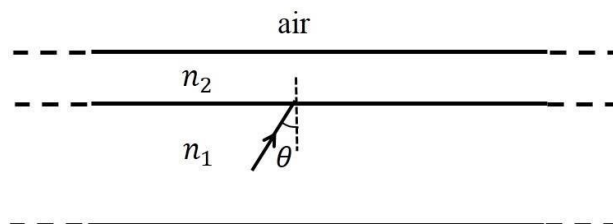
**SECTION 3**

- This section contains **SIX (06)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONE OR MORE THAN ONE** of these four option(s) is (are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:
  - Full Marks* : +4 If only (all) the correct option(s) is(are) chosen;
  - Partial Marks* : +3 If all the four options are correct but **ONLY** three options are chosen;
  - Partial Marks* : +2 If three or more options are correct but **ONLY** two options are chosen, both of which are correct;
  - Partial Marks* : +1 If two or more options are correct but **ONLY** one option is chosen and it is a correct option;
  - Zero Marks* : 0 If unanswerd;
  - Negative Marks* : -2 In all other cases.
- For example, in a question, if (A), (B) and (D) are the **ONLY** three options corresponding to correct answers, then
  - choosing **ONLY** (A), (B) and (D) will get +4 marks;
  - choosing **ONLY** (A) and (B) will get +2 marks;
  - choosing **ONLY** (A) and (D) will get +2 marks;
  - choosing **ONLY** (B) and (D) will get +2 marks;
  - choosing **ONLY** (A) will get +1 mark;
  - choosing **ONLY** (B) will get +1 mark;
  - choosing **ONLY** (D) will get +1 mark;
  - choosing no option(s) (i.e. the question is unanswerd) will get 0 marks
  - and choosing any other option(s) will get -2 marks.

- Q.11 A horizontal force  $F$  is applied at the center of mass of a cylindrical object of mass  $m$  and radius  $R$ , perpendicular to its axis as shown in the figure. The coefficient of friction between the object and the ground is  $\mu$ . The center of mass of the object has an acceleration  $a$ . The acceleration due to gravity is  $g$ . Given that the object rolls without slipping, which of the following statement(s) is(are) correct?



- (A) For the same  $F$ , the value of  $a$  does not depend on whether the cylinder is solid or hollow
- (B) For a solid cylinder, the maximum possible value of  $a$  is  $2\mu g$
- (C) The magnitude of the frictional force on the object due to the ground is always  $\mu mg$
- (D) For a thin-walled hollow cylinder,  $a = \frac{F}{2m}$
- Q.12 A wide slab consisting of two media of refractive indices  $n_1$  and  $n_2$  is placed in air as shown in the figure. A ray of light is incident from medium  $n_1$  to  $n_2$  at an angle  $\theta$ , where  $\sin \theta$  is slightly larger than  $1/n_1$ . Take refractive index of air as 1. Which of the following statement(s) is(are) correct?



- (A) The light ray enters air if  $n_2 = n_1$
- (B) The light ray is finally reflected back into the medium of refractive index  $n_1$  if  $n_2 < n_1$
- (C) The light ray is finally reflected back into the medium of refractive index  $n_1$  if  $n_2 > n_1$
- (D) The light ray is reflected back into the medium of refractive index  $n_1$  if  $n_2 = 1$

Q.13 A particle of mass  $M = 0.2$  kg is initially at rest in the  $xy$ -plane at a point  $(x = -l, y = -h)$ , where  $l = 10$  m and  $h = 1$  m. The particle is accelerated at time  $t = 0$  with a constant acceleration  $a = 10$  m/s<sup>2</sup> along the positive  $x$ -direction. Its angular momentum and torque with respect to the origin, in SI units, are represented by  $\vec{L}$  and  $\vec{\tau}$ , respectively.  $\hat{i}$ ,  $\hat{j}$  and  $\hat{k}$  are unit vectors along the positive  $x$ ,  $y$  and  $z$  directions respectively. If  $\vec{k} = \hat{i} \times \hat{j}$  then which of the following statement(s) is(are) correct?

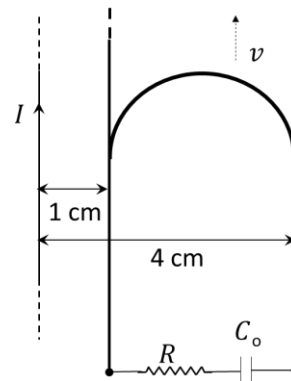
- (A) The particle arrives at the point  $(x = l, y = -h)$  at time  $t = 2$  s
- (B)  $\vec{\tau} = 2 \hat{k}$  when the particle passes through the point  $(x = l, y = -h)$
- (C)  $\vec{L} = 4 \hat{k}$  when the particle passes through the point  $(x = l, y = -h)$
- (D)  $\vec{\tau} = \hat{k}$  when the particle passes through the point  $(x = 0, y = -h)$

Q.14 Which of the following statement(s) is(are) correct about the spectrum of hydrogen atom?

- (A) The ratio of the longest wavelength to the shortest wavelength in Balmer series is  $9/5$
- (B) There is an overlap between the wavelength ranges of Balmer and Paschen series
- (C) The wavelengths of Lyman series are given by  $(1 + \frac{1}{m^2}) \lambda_0$ , where  $\lambda_0$  is the shortest wavelength of Lyman series and  $m$  is an integer
- (D) The wavelength ranges of Lyman and Balmer series do not overlap

Q.15 A long straight wire carries a current,  $I = 2$  ampere. A semi-circular conducting rod is placed beside it on two conducting parallel rails of negligible resistance. Both the rails are parallel to the wire. The wire, the rod and the rails lie in the same horizontal plane, as shown in the figure. Two ends of the semi-circular rod are at distances 1 cm and 4 cm from the wire. At time  $t = 0$ , the rod starts moving on the rails with a speed  $v = 30$  m/s (see the figure).

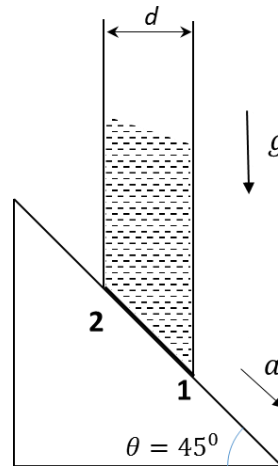
A resistor  $R = 14 \ \Omega$  and a capacitor  $C_0 = 50 \ \mu\text{F}$  are connected in series between the rails. At time  $t = 0$ ,  $C_0$  is uncharged. Which of the following statement(s) is(are) correct? [ $\mu_0 = 4\pi \times 10^{-7}$  SI units. Take  $\ln 2 = 0.7$ ]



- (A) Maximum current through  $R$  is  $1.2 \times 10^{-6}$  ampere  
 (B) Maximum current through  $R$  is  $3.8 \times 10^{-6}$  ampere  
 (C) Maximum charge on capacitor  $C_0$  is  $8.4 \times 10^{-12}$  coulomb  
 (D) Maximum charge on capacitor  $C_0$  is  $2.4 \times 10^{-12}$  coulomb



- Q.16 A cylindrical tube, with its base as shown in the figure, is filled with water. It is moving down with a constant acceleration  $a$  along a fixed inclined plane with angle  $\theta = 45^\circ$ .  $P_1$  and  $P_2$  are pressures at points **1** and **2**, respectively, located at the base of the tube. Let  $\beta = (P_1 - P_2)/(\rho g d)$ , where  $\rho$  is density of water,  $d$  is the inner diameter of the tube and  $g$  is the acceleration due to gravity. Which of the following statement(s) is(are) correct?



- (A)  $\beta = 0$  when  $a = g/\sqrt{2}$                       (B)  $\beta > 0$  when  $a = g/\sqrt{2}$   
 (C)  $\beta = \frac{\sqrt{2}-1}{\sqrt{2}}$  when  $a = g/2$                       (D)  $\beta = \frac{1}{\sqrt{2}}$  when  $a = g/2$

## SECTION

## 4

- This section contains **THREE (03)** questions.
- The answer to each question is a **NON-NEGATIVE INTEGER**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.

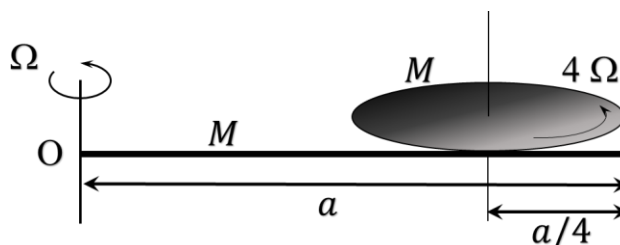
*Full Marks* : +4 If ONLY the correct integer is entered;

*Zero* : 0 In all other cases.

- Q.17 An  $\alpha$ -particle (mass 4 amu) and a singly charged sulfur ion (mass 32 amu) are initially at rest. They are accelerated through a potential  $V$  and then allowed to pass into a region of uniform magnetic field which is normal to the velocities of the particles. Within this region, the  $\alpha$ -particle and the sulfur ion move in circular orbits of radii  $r_\alpha$  and  $r_S$ , respectively. The ratio  $(r_S/r_\alpha)$  is . \_\_\_\_\_

- Q.18 A thin rod of mass  $M$  and length  $a$  is free to rotate in horizontal plane about a fixed vertical axis passing through point O. A thin circular disc of mass  $M$  and of radius  $a/4$  is pivoted on this rod with its center at a distance  $a/4$  from the free end so that it can rotate freely about its vertical axis, as shown in the figure. Assume that both the rod and the disc have uniform density and they remain horizontal during the motion. An outside stationary observer finds the rod rotating with an angular velocity  $\Omega$  and the disc rotating about its vertical axis with angular velocity  $4\Omega$ . The total angular momentum of the system about the point O is  $(\frac{Ma^2\Omega^2}{48})n$ .

The value of  $n$  is\_.



- Q.19 A small object is placed at the center of a large evacuated hollow spherical container. Assume that the container is maintained at 0 K. At time  $t = 0$ , the temperature of the object is 200 K. The temperature of the object becomes 100 K at  $t = t_1$  and 50 K at  $t = t_2$ . Assume the object and the container to be ideal black bodies. The heat capacity of the object does not depend on temperature. The ratio  $(t_2/t_1)$  is\_.

**END OF THE QUESTION PAPER**