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65/2 VALUE POINTS

SECTION A

1. $A' = \begin{pmatrix} 1 & 2 & -2 \\ 2 & 1 & 2 \\ 2 & x & -1 \end{pmatrix}$ and getting $x = -2$ $\frac{1}{2} + \frac{1}{2}$

2. Writing $\frac{3ae}{2} = a$ and finding $e = \frac{2}{3}$ $\frac{1}{2} + \frac{1}{2}$

3. $\frac{\pi}{3} - \frac{2\pi}{3} = -\frac{\pi}{3}$ $\frac{1}{2}$ for any one of $\frac{\pi}{3}$ or $\frac{2\pi}{3}$ $\frac{1}{2} + \frac{1}{2}$

4. $[\hat{i} \hat{k} \hat{j}] = \hat{i} \cdot (\hat{k} \times \hat{j}) = -\hat{i} \cdot (\hat{j} \times \hat{k})$ $\frac{1}{2}$

$= -1$ $\frac{1}{2}$

SECTION B

5. $R'(x) = 6x + 36$. 1

$R'(5) = 66$ 1

6. Let $y = \tan^{-1} \left(\frac{\cos x - \sin x}{\cos x + \sin x} \right) = \tan^{-1} \left(\frac{1 - \tan x}{1 + \tan x} \right)$ $\frac{1}{2}$

$= \tan^{-1} \left(\tan \left(\frac{\pi}{4} - x \right) \right)$ $\frac{1}{2}$

$= \frac{\pi}{4} - x$ $\frac{1}{2}$

$\Rightarrow \frac{dy}{dx} = -1$ $\frac{1}{2}$

7. Finding $A^{-1} = \frac{-1}{19} \begin{bmatrix} -2 & -3 \\ -5 & 2 \end{bmatrix}$ 1

$\Rightarrow \frac{-1}{19} \begin{bmatrix} -2 & -3 \\ -5 & 2 \end{bmatrix} = \begin{bmatrix} 2k & 3k \\ 5k & -2k \end{bmatrix}$ $\frac{1}{2}$

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$$\Rightarrow k = \frac{1}{19} \quad \frac{1}{2}$$

8. Put $x = \cos \theta$ in R.H.S

 $\frac{1}{2}$

$$\text{as } \frac{1}{2} \leq x \leq 1, \text{ RHS} = \cos^{-1}(4 \cos^3 \theta - 3 \cos \theta) = \cos^{-1}(\cos 3\theta) = 3\theta \quad \frac{1}{2} + \frac{1}{2}$$

$$= 3 \cos^{-1} x = \text{LHS} \quad \frac{1}{2}$$

9. $P(A/B) = \frac{P(A \cap B)}{P(B)}$ gives $P(A \cap B) = \frac{2}{13}$ 1

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$= \frac{5}{26} + \frac{5}{13} - \frac{2}{13} = \frac{11}{26} \quad 1$$

10. $\vec{a} + \vec{b} + \vec{c} = 0$

$$\vec{a} + \vec{b} = -\vec{c}$$

$$\vec{a}^2 + \vec{b}^2 + 2\vec{a} \cdot \vec{b} = \vec{c}^2$$

$$\Rightarrow \vec{a} \cdot \vec{b} = \frac{|\vec{c}|^2 - |\vec{a}|^2 - |\vec{b}|^2}{2} \quad \frac{1}{2}$$

$$\cos \theta = \frac{\vec{a} \cdot \vec{b}}{|\vec{a}| |\vec{b}|} = \frac{|\vec{c}|^2 - |\vec{a}|^2 - |\vec{b}|^2}{2|\vec{a}| |\vec{b}|} \quad \frac{1}{2}$$

$$= \frac{9^2 - 5^2 - 6^2}{2(5)(6)}$$

$$\cos \theta = \frac{81 - 25 - 36}{60} = \frac{1}{3} \quad \frac{1}{2}$$

$$\theta = \cos^{-1}\left(\frac{1}{3}\right) \quad \frac{1}{2}$$

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$$11. \frac{dy}{dx} = \cos^{-1} a \Rightarrow \int dy = \cos^{-1} a \cdot \int dx \quad \frac{1}{2} + \frac{1}{2}$$

$$y = x \cos^{-1} a + c \quad 1$$

$$12. \frac{3 - 5 \sin x}{\cos^2 x} dx = 3 \int \sec^2 x dx - 5 \int \sec x \tan x dx \quad 1$$

$$= 3 \tan x - 5 \sec x + C \quad \frac{1}{2} + \frac{1}{2}$$

SECTION C

$$13. \frac{dy}{dx} = \frac{y^2 - x^2}{2xy} = \frac{\frac{y^2}{x^2} - 1}{\frac{2y}{x}} \quad 1$$

$$\text{Put } \frac{y}{x} = v \Rightarrow y = vx \text{ and so } \frac{dy}{dx} = v + x \frac{dv}{dx} \quad 1$$

$$v + x \frac{dv}{dx} = \frac{v^2 - 1}{2v} \Rightarrow \frac{xdv}{dx} = -\frac{(1 + v^2)}{2v} \quad \frac{1}{2}$$

$$\int \frac{dx}{x} = -\int \frac{2v dv}{1 + v^2} \Rightarrow \log x = -\log(1 + v^2) + \log C \quad \frac{1}{2} + \frac{1}{2}$$

$$\Rightarrow x(1 + v^2) = C \text{ so } x \left(1 + \frac{y^2}{x^2} \right) = C \text{ or } x^2 + y^2 = Cx \quad \frac{1}{2}$$

OR

$$\frac{dy}{dx} + \frac{2x}{1 + x^2} y = \frac{1}{(1 + x^2)^2} \quad 1$$

$$\text{I.F.} = e^{\int \frac{2x}{1+x^2} dx} = e^{\log(1+x^2)} = (1+x^2) \quad 1$$

$$\text{Solution is } y(1+x^2) = \int \frac{1}{1+x^2} dx = \tan^{-1} x + C \quad 1$$



$$\text{getting } C = -\frac{\pi}{4} \quad \frac{1}{2}$$

$$\therefore y(1+x^2) = \tan^{-1} x - \frac{\pi}{4}$$

$$\text{or } y = \frac{\tan^{-1} x}{1+x^2} - \frac{\pi}{4(1+x^2)} \quad \frac{1}{2}$$

14. Point of intersection = $(1, \sqrt{3})$ 1

$$x^2 + y^2 = 4 \Rightarrow 2x + 2y \frac{dy}{dx} = 0 \quad \frac{dy}{dx} \Big|_{(1, \sqrt{3})} = -\frac{1}{\sqrt{3}} = m_1 \quad \frac{1}{2} + \frac{1}{2}$$

$$(x-2)^2 + y^2 = 4 \Rightarrow 2(x-2) + 2y \frac{dy}{dx} = 0 \Rightarrow \frac{dy}{dx} \Big|_{[1, \sqrt{3}]} = \frac{1}{\sqrt{3}} = m_2 \quad \frac{1}{2} + \frac{1}{2}$$

$$\text{So, } \tan \phi = \frac{\frac{1}{\sqrt{3}} + \frac{1}{\sqrt{3}}}{1 - 1/3} = \sqrt{3} \Rightarrow \phi = \frac{\pi}{3} \quad 1$$

OR

$$f'(x) = -6(x+1)(x+2) \quad 1$$

$$f'(x) = 0 \Rightarrow x = -2, x = -1 \quad \frac{1}{2}$$

$$\Rightarrow \text{Intervals are } (-\infty, -2), (-2, -1) \text{ and } (-1, \infty) \quad \frac{1}{2}$$

$$\text{Getting } f'(x) > 0 \text{ in } (-2, -1) \text{ and } f'(x) < 0 \text{ in } (-\infty, -2) \cup (-1, \infty) \quad 1$$

$$\Rightarrow f(x) \text{ is strictly increasing in } (-2, -1) \quad \left. \begin{array}{l} \\ \text{and strictly decreasing in } (-\infty, -2) \cup (-1, \infty) \end{array} \right\} \quad 1$$

15. Getting $\overline{AB} = (5-4)\hat{i} + (x-4)\hat{j} + (8-4)\hat{k} = \hat{i} + (x-4)\hat{j} + 4\hat{k}$

$$\overline{AC} = \hat{i} + 0\hat{j} - 3\hat{k} \text{ and } \overline{AD} = 3\hat{i} + 3\hat{j} - 2\hat{k} \quad 1 \frac{1}{2}$$



for coplanarity $[\overline{AB} \quad \overline{AC} \quad \overline{AD}] = 0$

$$\Rightarrow \begin{vmatrix} 1 & x-4 & 4 \\ 1 & 0 & -3 \\ 3 & 3 & -2 \end{vmatrix} = 0$$

$$\Rightarrow x = 7$$

 $\frac{1}{2}$ $\frac{1}{2}$ $1\frac{1}{2}$

16. $C_1 \rightarrow C_1 + C_2 + C_3$ gives L.H.S. as

$$\begin{vmatrix} a+b+c & -2a+b & -2a+c \\ a+b+c & 5b & -2b+c \\ a+b+c & -2c+b & 5c \end{vmatrix}$$

1

$$= (a+b+c) \begin{vmatrix} 1 & -2a+b & -2a+c \\ 1 & 5b & -2b+c \\ 1 & -2c+b & 5c \end{vmatrix}$$

 $\frac{1}{2}$

$R_2 \rightarrow R_2 - R_1, R_3 \rightarrow R_3 - R_1$ gives

$$= (a+b+c) \begin{vmatrix} 1 & -2a+b & -2a+c \\ 0 & 2a+4b & 2a-2b \\ 0 & 2a-2c & 4c+2a \end{vmatrix}$$

1

$$= (a+b+c) \begin{vmatrix} 2a+4b & 2a-2b \\ 2a-2c & 4c+2a \end{vmatrix}$$

 $\frac{1}{2}$

$$= 4(a+b+c) \begin{vmatrix} a+2b & a-b \\ a-c & 2c+a \end{vmatrix} = 4(a+b+c) 3(ab+bc+ac)$$

 $\frac{1}{2} + \frac{1}{2}$

$$= 12(a+b+c)(ab+bc+ac)$$

17. $\begin{vmatrix} x_2 - x_1 & y_2 - y_1 & z_2 - z_1 \\ a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \end{vmatrix} = \begin{vmatrix} 1 & 2 & 2 \\ 2 & 3 & 4 \\ 3 & 4 & 5 \end{vmatrix} = 1$

1+1

$$\sqrt{(b_1c_2 - b_2c_1)^2 + (a_2c_1 - a_1c_2)^2 + (a_1b_2 - a_2b_1)^2} = \sqrt{1+4+1} = \sqrt{6}$$

 $1 + \frac{1}{2}$ 

$$d = \frac{1}{\sqrt{6}} \quad \frac{1}{2}$$

$$18. \quad x = \frac{\sin y}{\cos(a+y)} \text{ gives } \frac{dx}{dy} = \frac{\cos(a+y)\cos y + \sin y \sin(a+y)}{\cos^2(a+y)} \quad \frac{1}{2} + 1$$

$$\Rightarrow \frac{dy}{dx} = \frac{\cos^2(a+y)}{\cos(a+y-y)} = \frac{\cos^2(a+y)}{\cos a} \quad 1 + \frac{1}{2}$$

$$\text{Hence } \frac{dy}{dx} = \cos a \text{ when } x = 0 \text{ i.e. } y = 0 \quad 1$$

$$19. \quad \text{Writing } \frac{dy}{d\theta} = 3a \tan^2 \theta \sec^2 \theta \quad 1$$

$$\frac{dx}{d\theta} = 3a \sec^3 \theta \tan \theta \quad 1$$

$$\frac{dy}{dx} = \frac{\tan \theta}{\sec \theta} = \sin \theta \quad \frac{1}{2}$$

$$\frac{d^2y}{dx^2} = \frac{d}{d\theta} \left(\frac{dy}{dx} \right) \frac{d\theta}{dx} = \cos \theta \times \frac{1}{3a \sec^3 \theta \tan \theta} \quad 1$$

$$\left. \frac{d^2y}{dx^2} \right)_{\theta = \frac{\pi}{3}} = \frac{\frac{1}{2}}{3a \times 8 \times \sqrt{3}} = \frac{1}{48\sqrt{3}a} \quad \frac{1}{2}$$

OR

$$y = e^{\tan^{-1} x}$$

$$\frac{dy}{dx} = e^{\tan^{-1} x} \left(\frac{1}{1+x^2} \right) = \frac{y}{1+x^2} \quad 1 + \frac{1}{2}$$

$$(1+x^2) \frac{dy}{dx} = y \Rightarrow (1+x^2) \frac{d^2y}{dx^2} + 2x \frac{dy}{dx} = \frac{dy}{dx} \quad 1 + 1$$

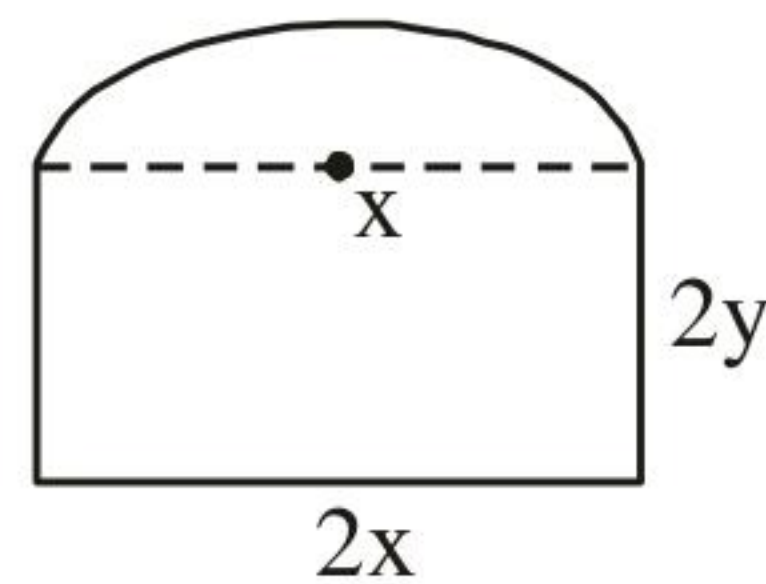
$$\Rightarrow (1+x^2) \frac{d^2y}{dx^2} + (2x-1) \frac{dy}{dx} = 0 \quad \frac{1}{2}$$

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20. Let the dimensions of window be $2x$ and $2y$



$$2x + 4y + \pi x = 10$$

 $\frac{1}{2}$

$$A = 4xy + \frac{1}{2}\pi x^2 = 4x \left(\frac{10 - \pi x - 2x}{4} \right) + \frac{1}{2}\pi x^2$$

1

$$= 10x - \frac{\pi x^2}{2} - 2x^2 \Rightarrow \frac{dA}{dx} = 10 - (\pi + 4)x$$

$$\frac{dA}{dx} = 0 \Rightarrow x = \frac{10}{\pi + 4}$$

 $\frac{1}{2}$

$$\frac{d^2A}{dx^2} = -(\pi + 4) < 0$$

 $\frac{1}{2}$

Getting, $y = \frac{5}{\pi + 4}$, so the dimensions are $\frac{20}{\pi + 4}$ m and $\frac{10}{\pi + 4}$ m

 $\frac{1}{2}$

Any relevant explanation.

1

21. Let E_1 = First group wins, E_2 = Second group wins

1

H = Introduction of new product.

$$P(E_1) = 0.6, P(E_2) = 0.4,$$

 $\frac{1}{2}$

$$P(H/E_2) = 0.3, P(H/E_1) = 0.7$$

 $\frac{1}{2}$

$$\text{Now, } P(E_2/H) = \frac{P(E_2) P(H/E_2)}{P(E_2) P(H/E_2) + P(E_1) P(H/E_1)}$$

 $\frac{1}{2}$

$$= \frac{0.4 \times 0.3}{0.4 \times 0.3 + 0.6 \times 0.7} = \frac{2}{9}$$

 $1 + \frac{1}{2}$ 

22. Let X denote the number of defective bulbs.

 $\frac{1}{2}$

$$X = 0, 1, 2, 3$$

 $\frac{1}{2}$

$$P(X = 0) = \left(\frac{15}{20}\right)^3 = \frac{27}{64}$$

$$P(X = 1) = 3\left(\frac{5}{20}\right)\left(\frac{15}{20}\right)^2 = \frac{27}{64}$$

$$P(X = 2) = 3\left(\frac{5}{20}\right)^2\left(\frac{15}{20}\right) = \frac{9}{64}$$

$$P(X = 3) = \left(\frac{5}{20}\right)^3 = \frac{1}{64}$$

 $\frac{1}{2} \times 4$

$$\text{Mean} = \sum XP(X) = \frac{27}{64} + \frac{18}{64} + \frac{3}{64} = \frac{3}{4}$$

1

23.
$$\frac{4}{(x-2)(x^2+4)} = \frac{A}{x-2} + \frac{Bx+C}{x^2+4}$$

1

$$4 = A(x^2+4) + (Bx+C)(x-2)$$

$$\text{gives } A = \frac{1}{2}, B = -\frac{1}{2}, C = 1$$

 $\frac{1}{2} \times 3$

$$\int \frac{4 dx}{(x-2)(x^2+4)} = \frac{1}{2} \int \frac{dx}{x-2} - \int \frac{(x+2)}{2(x^2+4)} dx$$

$$= \frac{1}{2} \log|x-2| - \frac{1}{4} \log|x^2+4| - \frac{1}{2} \tan^{-1}\left(\frac{x}{2}\right) + C$$

 $\frac{1}{2} + \frac{1}{2} + \frac{1}{2}$

SECTION D

24. Let number of units of type A be x and that of type B be y

$$\text{LPP is Maximize } P = 40x + 50y$$

1

subject to constraints

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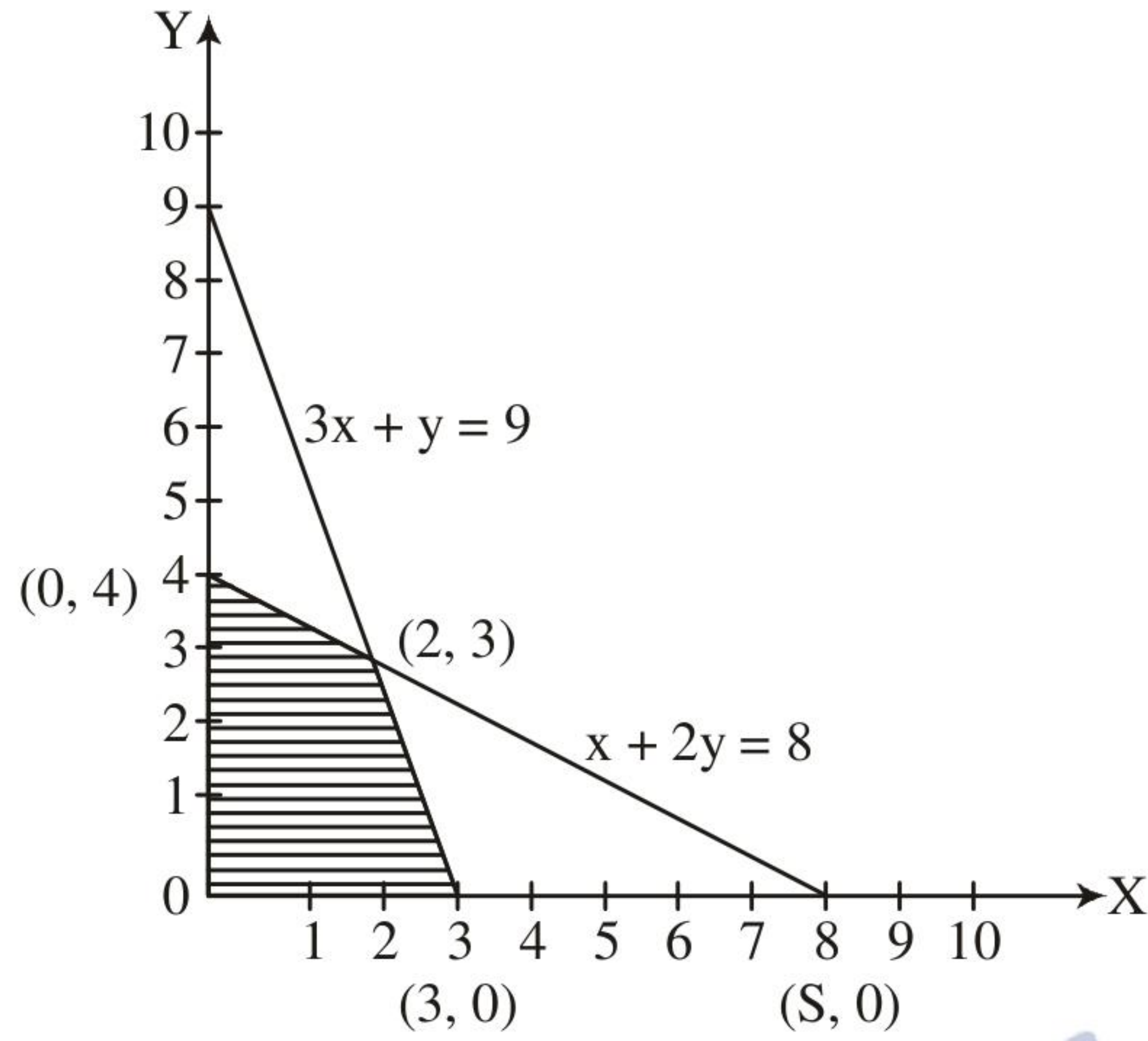


$$3x + y \leq 9$$

2

$$x + 2y \leq 8$$

$$x, y \geq 0$$



2

$$P(3, 0) = 120$$

$$P(2, 3) = 230$$

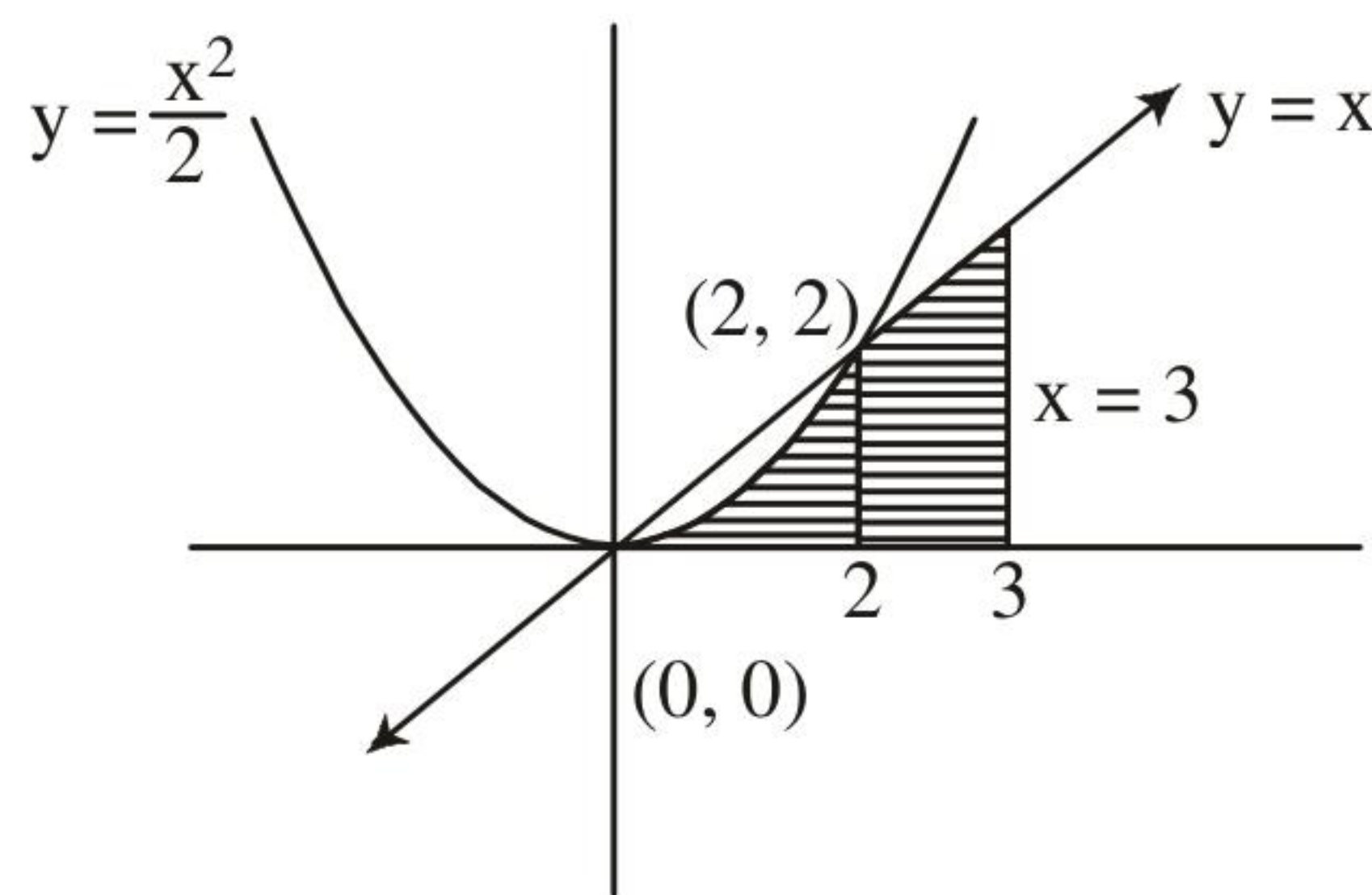
$$P(0, 4) = 200$$

∴ Max profit = ₹ 230 at (2, 3)

So to maximise profit, number of units of A = 2 and number of units of B = 3

1

25.



1

Point of intersection of $x^2 = 2y$ and $y = x$ are (0, 0) and (2, 2).

2

$$\text{Required area} = \int_0^2 \frac{x^2}{2} dx + \int_2^3 x dx$$

2

$$= \frac{8}{6} + \frac{5}{2} = \frac{23}{6}$$

1



26. Since the line is parallel to the two planes.

$$\therefore \text{Direction of line } \vec{b} = (\hat{i} - \hat{j} + 2\hat{k}) \times (3\hat{i} + \hat{j} + \hat{k}) \quad 1$$

$$= -3\hat{i} + 5\hat{j} + 4\hat{k} \quad 1$$

\therefore Equation of required line is

$$\vec{r} = (\hat{i} + 2\hat{j} + 3\hat{k}) + \lambda(-3\hat{i} + 5\hat{j} + 4\hat{k}) \quad \dots(i) \quad 1$$

Any point on line (i) is $(1 - 3\lambda, 2 + 5\lambda, 3 + 4\lambda)$ 1

For this line to intersect the plane $\vec{r} \cdot (2\hat{i} + \hat{j} + \hat{k}) = 4$

$$\text{we have } (1 - 3\lambda)2 + (2 + 5\lambda)1 + (3 + 4\lambda)1 = 4$$

$$\Rightarrow \lambda = -1 \quad 1$$

\therefore Point of intersection is $(4, -3, -1)$ 1

27. $|A| = 5(-1) + 4(1) = -1$ 1

$$\begin{array}{lll} C_{11} = -1 & C_{21} = 8 & C_{31} = -12 \\ C_{12} = 0 & C_{22} = 1 & C_{32} = -2 \\ C_{13} = 1 & C_{23} = -10 & C_{33} = 15 \end{array} \quad 2$$

$$A^{-1} = \begin{bmatrix} 1 & -8 & 12 \\ 0 & -1 & 2 \\ -1 & 10 & -15 \end{bmatrix} \quad 1$$

$$(AB)^{-1} = B^{-1}A^{-1} = \begin{bmatrix} 1 & 3 & 3 \\ 1 & 4 & 3 \\ 1 & 3 & 4 \end{bmatrix} \begin{bmatrix} 1 & -8 & 12 \\ 0 & -1 & 2 \\ -1 & 10 & -15 \end{bmatrix} \quad 1$$

$$= \begin{bmatrix} -2 & 19 & -27 \\ -2 & 18 & -25 \\ -3 & 29 & -42 \end{bmatrix} \quad 1$$

OR

$$\begin{bmatrix} 1 & 2 & -2 \\ -1 & 3 & 0 \\ 0 & -2 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} A \quad 1$$

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$$R_1 \rightarrow R_1 + 2R_3$$

$$\begin{bmatrix} 1 & -2 & 0 \\ -1 & 3 & 0 \\ 0 & -2 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 2 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} A$$

1

$$R_2 \rightarrow R_2 + R_1$$

$$\begin{bmatrix} 1 & -2 & 0 \\ 0 & 1 & 0 \\ 0 & -2 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 2 \\ 1 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix} A$$

1

$$R_3 \rightarrow R_3 + 2R_2$$

$$\begin{bmatrix} 1 & -2 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 2 \\ 1 & 1 & 2 \\ 2 & 2 & 5 \end{bmatrix} A$$

1

$$R_1 \rightarrow R_1 + 2R_2$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 3 & 2 & 6 \\ 1 & 1 & 2 \\ 2 & 2 & 5 \end{bmatrix} A$$

1

$$\text{So, } A^{-1} = \begin{bmatrix} 3 & 2 & 6 \\ 1 & 1 & 2 \\ 2 & 2 & 5 \end{bmatrix}$$

1

$$28. \quad I = \int_0^{\pi/2} \frac{x \sin x \cos x}{\sin^4 x + \cos^4 x} dx$$

$$= \int_0^{\pi/2} \frac{(\pi/2 - x) \sin(\pi/2 - x) \cos(\pi/2 - x)}{\sin^4(\pi/2 - x) + \cos^4(\pi/2 - x)} dx = \int_0^{\pi/2} \frac{(\pi/2 - x) \cos x \sin x}{\cos^4 x + \sin^4 x} dx$$

1

$$2I = \pi/2 \int_0^{\pi/2} \frac{\sin x \cos x}{\sin^4 x + \cos^4 x} dx = \frac{\pi}{2} \int_0^{\pi/2} \frac{\sin x \cos x}{\sin^4 x + (1 - \sin^2 x)^2} dx$$

1

$$\text{Let } \sin^2 x = t \Rightarrow \sin x \cos x dx = \frac{1}{2} dt$$

 $\frac{1}{2}$ 

$$2I = \frac{\pi}{2} \frac{1}{2} \int_0^1 \frac{dt}{t^2 + (1-t)^2} \quad 1$$

$$\Rightarrow I = \frac{\pi}{8} \int_0^1 \frac{dt}{2t^2 - 2t + 1} = \frac{\pi}{16} \int_0^1 \frac{dt}{(t-1/2)^2 + (1/2)^2} \quad 1$$

$$I = \frac{\pi}{16} \frac{2}{1} \cdot \tan^{-1}(2t-1) \Big|_0^1 = \frac{\pi}{8} \cdot \left[\frac{\pi}{4} - \left(-\frac{\pi}{4} \right) \right] = \frac{\pi^2}{16} \quad 1 + \frac{1}{2}$$

OR

$$a = 1, b = 3, h = \frac{2}{n} \Rightarrow nh = 2 \quad 1$$

$$\int_1^3 (3x^2 + 2x + 1) dx = \lim_{h \rightarrow 0} h [f(1) + f(1+h) + f(1+2h) + \dots + f(1+(n-1)h)] \quad 1$$

$$= \lim_{h \rightarrow 0} h [6 + \{3(1+h^2 + 2h) + 2(1+h) + 1\} + \{3(1+4h^2 + 4h) + 2(1+2h) + 1\} + \dots + \{3(1+(n-1)^2h^2 + 2(n-1)h + 2(1+(n-1)h) + 1\}] \quad 1$$

$$= \lim_{h \rightarrow 0} h [6n + 8h(1+2+\dots+(n-1)) + 3h^2(1^2 + 2^2 + \dots + (n-1)^2)] \quad \frac{1}{2}$$

$$= \lim_{h \rightarrow 0} 6nh + \frac{8(nh-h)(nh)}{2} + \frac{3(nh-h)(nh)(2hn-h)}{6} \quad 1 \frac{1}{2}$$

$$= 6(2) + \frac{8(2)(2)}{2} + \frac{3(2-0)(2)(4)}{6} \quad \frac{1}{2}$$

$$= 12 + 16 + 8 = 36 \quad \frac{1}{2}$$

29. $(x-x) = 0$ is divisible by 3 for all $x \in z$. So, $(x, x) \in R$ 1

$\therefore R$ is reflexive.

$(x-y)$ is divisible by 3 implies $(y-x)$ is divisible by 3.

So $(x, y) \in R$ implies $(y, x) \in R, x, y \in z$ 1 $\frac{1}{2}$

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$\Rightarrow R$ is symmetric.

$(x - y)$ is divisible by 3 and $(y - z)$ is divisible by 3.

So $(x - z) = (x - y) + (y - z)$ is divisible by 3.

$$1+1+\frac{1}{2}$$

Hence $(x, z) \in R \Rightarrow R$ is transitive

$\Rightarrow R$ is an equivalence relation

1

OR

*	0	1	2	3	4	5
0	0	1	2	3	4	5
1	1	2	3	4	5	0
2	2	3	4	5	0	1
3	3	4	5	0	1	2
4	4	5	0	1	2	3
5	5	0	1	2	3	4

Table Format 1

Values of each correct row,

$$\frac{1}{2} \times 6 = 3$$

$a * 0 = a + 0 = a \forall a \in A \Rightarrow 0$ is the identify for $*$.

$\frac{1}{2}$

Let $b = 6 - a$ for $a \neq 0$.

$\frac{1}{2}$

Since $a + b = a + 6 - a < 6$

$\Rightarrow a * b = b * a = a + 6 - a - 6 = 0$

$\frac{1}{2}$

Hence $b = 6 - a$ is the inverse of a .

$\frac{1}{2}$

