ALGEBRAIC EQUATIONS

Algebraic equations are polynomial equations. In examination, generally equations of 1 degree, 2 degree or 3 degrees are asked.

Linear Equation

Polynomial equations with degree 1 i.e., ax + c = 0 are called as linear equations. Some examples of linear equations are as follows –

$$2x + 3y = 4$$

$$x + y + z = 10$$

Q1. In this question two equations numbered I and II are given. You have to solve both the equations and find out the relation between x and y.

I.
$$5x = 7y + 21$$

II.
$$11x + 4y + 109 = 0$$

Solution:

I.
$$2x + 3y = 13$$

II.
$$3x + 2y = 12$$

(3 × Equation 2) - (2 × Equation 1) gives us

$$\Rightarrow$$
 5x = 10

$$\Rightarrow$$
 x = 2

Putting value of x in equation 1, we get y

= 3

Hence, x < y.

Q2. In the given question, two equations numbered I and II are given. You have to solve both the equations and mark the appropriate answer-

I.
$$4x + 5y = 14$$

II.
$$2x + 3y = 5$$

Solution:

$$4x + 5y = 14$$
 (1)

$$2x + 3y = 5$$
 (2)

On multiplying equation (2) by 2.

$$4x + 6y = 10$$
 (3)

Subtracting equation (1) from equation (3),

$$y = -4$$

x = 1 (on putting value of y in the above equation)

Quadratic Equation

Polynomial equations with degree 2 i.e., $ax^2 + bx + c = 0$ are called quadratic equations. Some examples of quadratic equations are as follows –

$$x^2 + 2x + 3 = 0$$

$$y^2 - 3y + 4 = 0$$

Methods to solve quadratic equation

1) Factorisation method

In it quadratic equation $ax^2 + bx + c = 0$ is factorized as $(x - \infty)(x - \beta) = 0$ and then equation is solved to get $x = \infty$ or $x = \beta$.

Q3. Solve quadratic equation

$$x^2 - 2x - 15 = 0$$

Solution:

$$x^2 - 2x - 15 = 0$$

$$\Rightarrow$$
 x² - 5x + 3x - 15 = 0

$$\Rightarrow$$
 x (x - 5) + 3(x - 5) = 0

$$\Rightarrow$$
 (x + 3) (x - 5) = 0

$$\Rightarrow$$
 x + 3 = 0 or x - 5 = 0

$$\Rightarrow$$
 x = -3 or x = 5

2) Sridharachrya's method

In it quadratic equation $ax^2 + bx + c = 0$ is solved by using formula

$$= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Which gives us
$$x = \frac{-b + \sqrt{b^2 - 4ac}}{2a}$$
 or $\frac{-b - \sqrt{b^2 - 4ac}}{2a}$

Q4. Solve quadratic equation $x^2 - 2x - 15 = 0$

Solution:

$$X1 = \frac{-b + \sqrt{b^2 - 4ac}}{2a} = 5$$

$$X2 = \frac{-b - \sqrt{b^2 - 4ac}}{2a} = -3$$

Q5. In the following question two equations are given. You have to solve both the equations and find the relation between x and y.

I.
$$x^2 = 625$$

II.
$$y = \sqrt{625}$$

Solution:

We will solve both the equations separately. x^2

$$\Rightarrow$$
 x = +25 or -25 (we will consider two values of x because of x^2) y =

 \Rightarrow y = 25 (The square root is used to refer to only the positive square root i.e.

$$\{\sqrt{x^2} = |x|\}.$$

∴
$$x \le y$$

Q6. In the given question, two equations numbered I and II are given. You have to solve both the equations and find the relation between m and n.

I) m =
$$\sqrt{324}$$

II)
$$n^2 - 16n - 36 = 0$$

Solution:

| Value of m | Value of n | Result |
|------------|------------|--------|
| 18 | 18 | m = n |
| 18 | -2 | m > n |

$$m = \sqrt{324}$$

$$\Rightarrow$$
 m = 18

$$n^2 - 16n - 36 = 0$$

$$\Rightarrow$$
 n² - 18n + 2n - 36 = 0

$$\Rightarrow$$
 n (n - 18) + 2(n - 18) = 0

$$\Rightarrow$$
 (n - 18) (n + 2) = 0

$$\Rightarrow$$
 n = (18, - 2)

Hence, $m \ge n$.

Cubic Equation

Polynomial equations with degree 3 i.e., $ax^3 + bx^2 + cx + d = 0$ are called as cubic equations. Some examples of cubic equations are as follows –

$$x^3 + 2x^2 + 3x + 4 = 0$$

$$2x^3 + 12x^2 + 30x + 48 = 0$$

$$X = \sqrt[3]{625}$$

Q7. In the given question, two equations numbered I and II are given. You have to solve both the equations and mark the appropriate answer

$$X = \sqrt[3]{15625}$$

$$y^2 = 625$$

Solution:

$$X = \sqrt[3]{15625} = 25$$

$$Y \leq X$$