

30/01/2023

Evening



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## Memory Based Answers & Solutions

Time : 3 hrs.

*for*

M.M. : 300

## JEE (Main)-2023 (Online) Phase-1

(Physics, Chemistry and Mathematics)

### IMPORTANT INSTRUCTIONS:

- (1) The test is of **3 hours** duration.
- (2) The Test Booklet consists of 90 questions. The maximum marks are 300.
- (3) There are **three** parts in the question paper consisting of **Physics, Chemistry** and **Mathematics** having 30 questions in each part of equal weightage. Each part (subject) has two sections.
  - (i) **Section-A:** This section contains 20 multiple choice questions which have only one correct answer. Each question carries **4 marks** for correct answer and **-1 mark** for wrong answer.
  - (ii) **Section-B:** This section contains 10 questions. In Section-B, attempt any **five questions out of 10**. The answer to each of the questions is a numerical value. Each question carries **4 marks** for correct answer and **-1 mark** for wrong answer. For Section-B, the answer should be rounded off to the nearest integer.

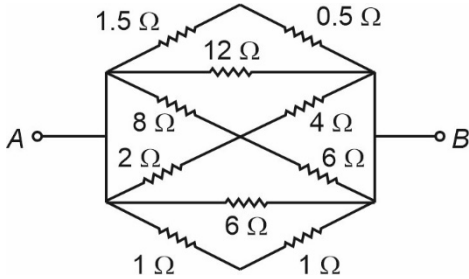
**PHYSICS**

**SECTION - A**

**Multiple Choice Questions:** This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

**Choose the correct answer:**

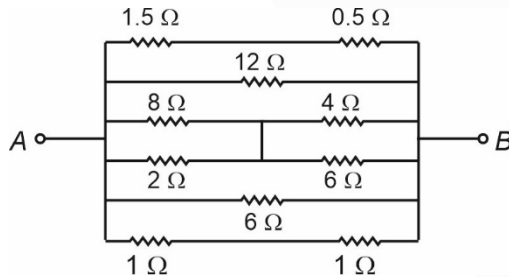
1. In the given circuit the resistance between terminals A and B is equal to



- (1) 2 Ω                                      (2)  $\frac{3}{2}$  Ω  
(3)  $\frac{2}{3}$  Ω                                      (4) 6 Ω

**Answer (3)**

**Sol.** The circuit can be redrawn as



So the net resistance across A and B is

$$\frac{1}{R_{net}} = \frac{1}{2} + \frac{1}{12} + \frac{1}{4} + \frac{1}{6} + \frac{1}{2}$$

$$\frac{1}{R_{net}} = \frac{6+1+3+2+6}{12}$$

$$R_{net} = \left(\frac{2}{3}\right) \Omega$$

2. A car travels 4 km distance with a speed of 3 km/h and next 4 km with a speed of 5 km/h. Find average speed of car.

- (1)  $\frac{15}{2}$  km/h                                      (2)  $\frac{15}{4}$  km/h  
(3) 15 km/h                                      (4) 10 km/h

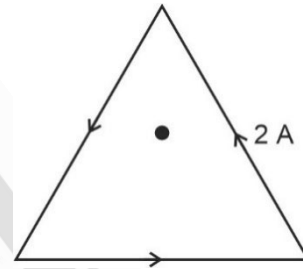
**Answer (2)**

**Sol.**  $v_{avg} = \frac{\text{Distance}}{\text{Time}}$

$$= \frac{4+4}{\frac{4}{3} + \frac{4}{5}} \text{ km/h}$$

$$= \frac{15}{4} \text{ km/h}$$

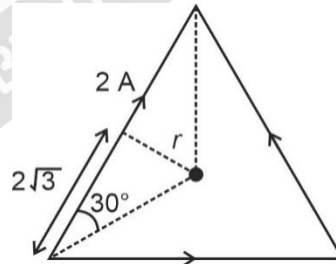
3. A current 2 A is flowing through the sides of an equilateral triangular loop of side  $4\sqrt{3}$  m as shown. Find the magnetic field induction at the centroid of the triangle.



- (1)  $3\sqrt{3} \times 10^{-7}$  T                                      (2)  $\sqrt{3} \times 10^{-7}$  T  
(3)  $2\sqrt{3} \times 10^{-7}$  T                                      (4)  $5\sqrt{3} \times 10^{-7}$  T

**Answer (1)**

**Sol.**



$$\frac{r}{2\sqrt{3}} = \tan 30^\circ$$

$$r = 2 \text{ m}$$

Magnetic field at centroid

$$= 3 \times \frac{\mu_0 I}{4\pi r} (\sin 60^\circ + \sin 60^\circ)$$

$$= 3 \times \frac{\mu_0}{4\pi} \times \frac{2}{2} \left[ \frac{\sqrt{3}}{2} + \frac{\sqrt{3}}{2} \right]$$

$$= 3\sqrt{3} \times \frac{\mu_0}{4\pi} \text{ T}$$

$$= 3\sqrt{3} \times 10^{-7} \text{ T}$$

4. A particle is released at a height equal to radius of the earth above the surface of the earth. Its velocity when it hits the surface of earth is equal to ( $M_e$  : mass of earth,  $R_e$  : Radius of earth)

(1)  $v = \sqrt{\frac{2GM_e}{R_e}}$       (2)  $v = \sqrt{\frac{GM_e}{2R_e}}$   
 (3)  $v = \sqrt{\frac{GM_e}{R_e}}$       (4)  $v = \sqrt{\frac{2GM_e}{3R_e}}$

**Answer (3)**

**Sol.** Using energy conservation.

$$-\frac{GMm}{2R_e} = -\frac{GMm}{R_e} + \frac{1}{2}mv^2$$

$$v = \sqrt{\frac{GM_e}{R_e}}$$

5. A faulty scale reads  $5^\circ\text{C}$  at melting point and  $95^\circ\text{C}$  at steam point.

Find original temperature if this faulty scale reads  $41^\circ\text{C}$ .

- (1)  $40^\circ\text{C}$       (2)  $41^\circ\text{C}$   
 (3)  $36^\circ\text{C}$       (4)  $45^\circ\text{C}$

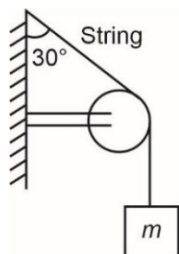
**Answer (1)**

**Sol.**  $\frac{41-5}{95-5} = \frac{x-0}{100-0}$

$$\Rightarrow 9x = 360$$

$$\Rightarrow x = 40$$

6. A block stays in equilibrium as shown:



Find the tension in the string if  $m = \sqrt{3}$  kg

- (1)  $\sqrt{3}g$  N      (2)  $3g$  N  
 (3)  $\frac{g}{2}$  N      (4)  $\frac{g}{\sqrt{3}}$  N

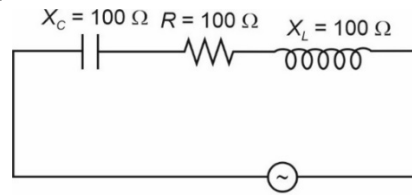
**Answer (1)**

**Sol.** Since block in equilibrium

$$\Rightarrow T = mg$$

$$\Rightarrow T = \sqrt{3}g$$

7. In the AC circuit shown in the figure the value of  $I_{\text{rms}}$  is equal to



$$V = 200\sqrt{2} \sin(\omega t)$$

- (1) 2A      (2)  $2\sqrt{2}$ A  
 (3) 4A      (4)  $\sqrt{2}$ A

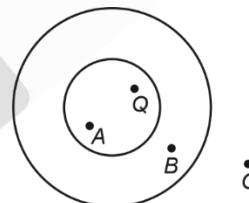
**Answer (1)**

**Sol.**  $Z = \sqrt{R^2 + (X_L - X_C)^2}$   
 $= \sqrt{100^2 + (100 - 100)^2} = 100 \Omega$

So,  $i_0 = \frac{200\sqrt{2}}{100} = 2\sqrt{2}$

So,  $i_{\text{rms}} = \frac{i_0}{\sqrt{2}} = 2\text{A}$

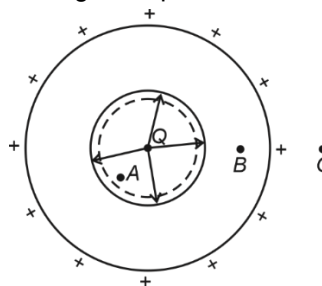
8. A point charge  $Q$  is placed inside the cavity made in uniform conducting solid sphere as shown.  $E_A$ ,  $E_B$  and  $E_C$  are electric field magnitudes at points  $A$ ,  $B$  and  $C$  respectively, Then



- (1)  $E_A = 0, E_B = 0$  and  $E_C \neq 0$   
 (2)  $E_A \neq 0, E_B = 0$  and  $E_C \neq 0$   
 (3)  $E_A \neq 0, E_B \neq 0$  and  $E_C = 0$   
 (4)  $E_A \neq 0, E_B \neq 0$  and  $E_C \neq 0$

**Answer (2)**

**Sol.** Taking  $Q$  as positive

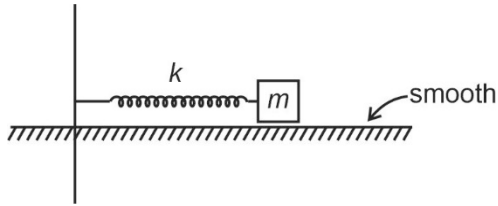


$E_A \neq 0$  (electric field due to both  $Q$  and induced charge on the inner surface of cavity)

$E_B = 0$  (No field line inside conductor)

$E_C \neq 0$  (electric field due to charge induced on outer surface of conductor).

9. In the shown mass-spring system when it is set into oscillations along the spring, it has angular frequency  $\omega_1$ , when  $m = 1$  kg and  $\omega_2$  if  $m = 2$  kg. Then value of  $\frac{\omega_1}{\omega_2}$  is equal to



- (1) 1                                      (2)  $\sqrt{2}$   
 (3)  $\frac{1}{\sqrt{2}}$                                 (4) 2

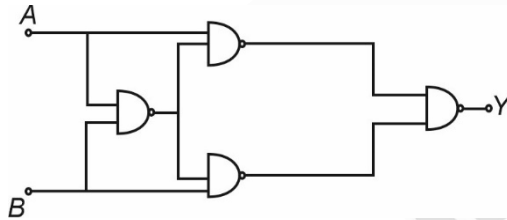
**Answer (2)**

**Sol.**  $\omega_1 = \sqrt{\frac{k}{m}} = \sqrt{\frac{k}{1}}$

$\omega_2 = \sqrt{\frac{k}{m}} = \sqrt{\frac{k}{2}}$

So  $\frac{\omega_1}{\omega_2} = \sqrt{\frac{k}{k/2}} = \sqrt{2}$

10. For the given logic circuit which of the following truth table is correct?



- (1) 

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0

                                      (2) 

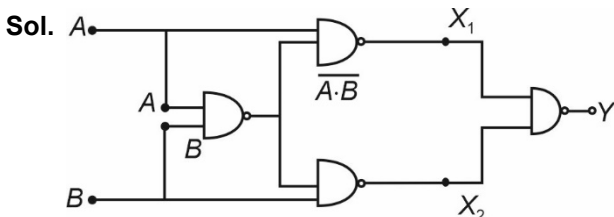
A	B	Y
0	0	1
0	1	0
1	0	0
1	1	1
- (3) 

A	B	Y
0	0	1
0	1	1
1	0	1
1	0	0

                                      (4) 

A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

**Answer (1)**



$$\begin{aligned} X_1 &= A \cdot (\overline{A \cdot B}) \cdot B \cdot (\overline{A \cdot B}) \\ &= A \cdot (\overline{AB}) + B \cdot (\overline{AB}) \\ &= A \cdot (\overline{A} + \overline{B}) + B \cdot (\overline{A} + \overline{B}) \\ &= \overline{AB} + \overline{BA} \\ &= \text{XOR gate} \end{aligned}$$

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0

11. A particle of mass  $m$  is moving under a force whose delivered power  $P$  is constant. Initial velocity of particle is zero. Find position of particle at  $t = 4$  s.

- (1)  $x = \frac{16}{3} \sqrt{\frac{2P}{m}}$                                       (2)  $x = \frac{4}{3} \sqrt{\frac{2P}{m}}$   
 (3)  $x = \frac{2}{3} \sqrt{\frac{P}{m}}$                                       (4)  $x = \frac{3}{10} \sqrt{\frac{P}{m}}$

**Answer (1)**

**Sol.**  $P = \frac{W}{t}$   
 $\Rightarrow \frac{1}{2}mv^2 = P \cdot t$   
 $\Rightarrow v = \sqrt{\frac{2Pt}{m}} = \frac{dx}{dt}$   
 $\Rightarrow x = \frac{16}{3} \sqrt{\frac{2P}{m}}$

12. Column-I list few physical quantities and column-II lists their dimensions. Choose the correct option matching the two lists correctly

Column-I	Column-II
(P) Pressure gradient	(A) $[M^1L^2T^{-2}]$
(Q) Energy density	(B) $[M^1L^1T^{-1}]$
(R) Torque	(C) $[M^1L^{-2}T^{-2}]$
(S) Impulse	(D) $[M^1L^{-1}T^{-2}]$
(1) P-C, Q-A, R-B, S-D	(2) P-C, Q-D, R-A, S-B
(3) P-A, Q-D, R-B, S-C	(4) P-A, Q-C, R-B, S-D

**Answer (2)**

**Sol.** [Pressure gradient]  $\Rightarrow \left[ \frac{dp}{dz} \right] = \left[ \frac{ML^{-1}T^{-2}}{L} \right]$   
 $= [ML^{-2}T^{-2}]$

$$[\text{Energy density}] \Rightarrow \left[ \frac{dU}{dV} \right] = \left[ \frac{ML^2T^{-2}}{L^3} \right] = [ML^{-1}T^{-2}]$$

$$[\text{Torque}] \Rightarrow [F] \times [r] = [MLT^{-2}] \times [L] = [ML^2T^{-2}]$$

$$[\text{Impulse}] \Rightarrow [F] [t] = [MLT^{-2}] [T] = [MLT^{-1}]$$

So, P → C, Q → D, R → A, S → B

13. Consider the following assertion & reason:

**Assertion (A):** At sink temperature of  $-273^\circ\text{C}$ , the efficiency of a Carnot engine will be 1.

**Reason (R):** Efficiency of a Carnot engine is given

$$\text{by } \eta = 1 - \frac{T_{\text{sink}}}{T_{\text{Source}}}$$

- (1) (A) is correct, (R) is correct and correctly explains A
- (2) (A) is not correct, (R) is correct
- (3) Both (A) & (R) are incorrect
- (4) Both (A) & (R) are correct, (R) does not explain (A)

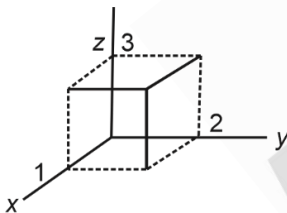
**Answer (1)**

**Sol.**  $\eta = 1 - \frac{T_{\text{sink}}}{T_{\text{Source}}}$

If  $T_{\text{sink}} = 0 \text{ K} \Rightarrow \eta = 1$

14. Electric field in a region is

$$\vec{E} = 2x^2\hat{i} - 4y\hat{j} + 6z\hat{k}$$



Find the charge inside the cuboid shown:

- (1)  $-8\epsilon_0$
- (2)  $36\epsilon_0$
- (3)  $12\epsilon_0$
- (4)  $24\epsilon_0$

**Answer (4)**

**Sol.**  $\phi_{\text{total}} = 2(1)^2[2 \times 3] - 4(2)[1 \times 3] + 6(3)[1 \times 2]$   
 $= 12 - 24 + 36$   
 $= 24$

$$\Rightarrow \frac{q}{\epsilon_0} = 24$$

$$\Rightarrow q = 24\epsilon_0$$

15. Find the ratio of de Broglie wavelength of proton, when it is accelerated across  $v$  and  $3v$  potential difference.

- (1) 3 : 1
- (2)  $1 : \sqrt{3}$
- (3) 1 : 3
- (4)  $\sqrt{3} : 1$

**Answer (4)**

**Sol.** When proton is accelerated by potential difference  $V$ , the linear momentum of proton

$$\frac{p^2}{2m} = eV$$

$$p = \sqrt{2meV} \Rightarrow \lambda_1 = \frac{h}{\sqrt{2meV}}$$

When accelerated by potential difference of  $3V$ , then linear momentum of proton is

$$\frac{p^2}{2m} = 3eV$$

$$p = \sqrt{6meV} \Rightarrow \lambda_2 = \frac{h}{\sqrt{6meV}}$$

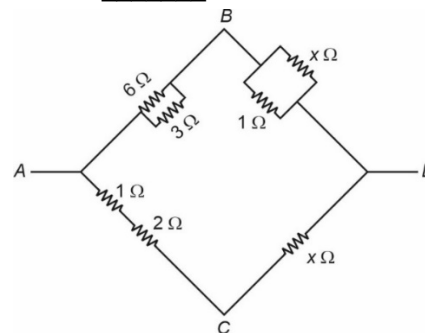
$$\frac{\lambda_1}{\lambda_2} = \sqrt{3}$$

- 16.
- 17.
- 18.
- 19.
- 20.

**SECTION - B**

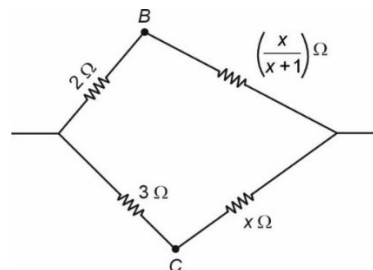
**Numerical Value Type Questions:** This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a **NUMERICAL VALUE**. For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g. 06.25, 07.00, -00.33, -00.30, 30.27, -27.30) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.

21. For the given electrical circuit, the potential difference between points  $B$  and  $C$  is zero. The value of  $x$  is \_\_\_\_\_.



**Answer (00.50)**

**Sol.**



$$V_B = V_C$$

$$\text{then } \frac{2}{3} = \frac{\left(\frac{x}{x+1}\right)}{x}$$

$$\Rightarrow \frac{2}{3} = \frac{1}{x+1}$$

$$x+1 = \frac{3}{2}$$

$$\Rightarrow x = \frac{1}{2} \Omega$$

22. Two waves of same intensity from sources in phase are made to superimpose at a point. If path difference between these two coherent waves is zero then resultant intensity is  $I_0$ . If this path difference is  $\frac{\lambda}{2}$  where  $\lambda$  is wavelength of these waves, then resultant intensity is  $I_1$  and if the path difference is  $\frac{\lambda}{4}$  then resultant intensity is  $I_2$ . Value of  $\frac{I_1 + I_2}{I_0}$  is equal to

**Answer (00.50)**

**Sol.** Let individual intensity from source is  $I$  thus

$$I_0 = I + I + 2\sqrt{I \times I} \cos\left(0 \times \frac{2\pi}{\lambda}\right)$$

$$\Rightarrow I_0 = 4I$$

$$I_1 = I + I + 2\sqrt{I \times I} \cos\left(\frac{\lambda}{2} \times \frac{2\pi}{\lambda}\right)$$

$$\Rightarrow I_1 = 0$$

$$I_2 = I + I + 2\sqrt{I \times I} \cos\left(\frac{\lambda}{4} \times \frac{2\pi}{\lambda}\right)$$

$$\Rightarrow I_2 = 2I$$

$$\text{So, } \frac{I_1 + I_2}{I_0} = \frac{1}{2} \text{ or } 0.5$$

23. A bullet (mass 10 grams) is fired from a gun (mass 10 kg without the bullet) with a speed of 100 m/s.

The recoil speed of gun is  $\frac{x}{10}$  m/s. Find  $x$ .

**Answer (1)**

**Sol.** Conserving momentum

$$10 \times V = \frac{10}{1000} \times 100$$

$$\Rightarrow V = \frac{1}{10} \text{ m/s}$$

24. The ratio of temperature (in K) of hydrogen and oxygen is 2 : 1. The ratio of their average kinetic energy per molecule is

**Answer (02.00)**

**Sol.** Average kinetic energy =  $\frac{f}{2} K_B T$

$$\frac{(\text{Average kinetic energy})_{H_2}}{(\text{Average kinetic energy})_{O_2}} = \frac{T_{H_2}}{T_{O_2}} = \left(\frac{2}{1}\right)$$

25. The relation between velocity ( $v$ ) and position ( $x$ ) of a particle moving along  $x$ -axis is given by  $4v^2 = 50 - x^2$ . The time period of the oscillatory motion of the particle is  $\frac{88}{n}$  seconds.

Find  $n$  [use  $\pi = \frac{22}{7}$ ]

**Answer (07.00)**

**Sol.**  $4v^2 = 50 - x^2$

$$v^2 = \frac{1}{4}(50 - x^2)$$

$$v = \frac{1}{2}\sqrt{50 - x^2}$$

Comparing equation of S.H.M.

$$v = \omega\sqrt{A^2 - x^2}$$

$$A^2 = 50$$

$$A = \sqrt{50} = 5\sqrt{2}$$

$$\omega = \frac{1}{2} = 0.5 \text{ rad/sec}$$

$$T = \frac{2\pi}{\omega} = \frac{2\pi}{0.5} = 4\pi \text{ second}$$

$$\pi = \left(\frac{22}{7}\right)$$

$$T = \frac{88}{7} = \frac{88}{n}$$

So,  $n = 7$

26. Prism  $A$  has angle of prism equal to  $6^\circ$  and its material has refractive index 1.5. It is used in combination with prism  $B$  of refractive index 1.8 to produce dispersion without deviation. Prism angle of prism  $B$  is equal to \_\_\_\_\_ degrees.

**Answer (03.75°)**

**Sol.** For dispersion without deviation

$$A_A(\mu_A - 1) + A_B(\mu_B - 1) = 0$$

$$6(1.5 - 1) + A(1.8 - 1) = 0$$

$$A = -\frac{3}{0.8} = -3.75^\circ$$

27.

28.

29.

30.

## CHEMISTRY

### SECTION – A

**Multiple Choice Questions:** This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which **ONLY ONE** is correct.

**Choose the correct answer :**

1. Maximum no. of  $e^-$  in  $n = 4$  shell
- (1) 72
  - (2) 50
  - (3) 16
  - (4) 32

**Answer (4)**

**Sol.** Maximum number of  $e^- = 2n^2$

$$= 2(4)^2$$

$$= 32$$

2. BOD value of a water sample is 3 ppm. Select the correct option about the given sample of water.
- (1) It is highly polluted water
  - (2) It is clean water
  - (3) Concentration of oxygen in the given sample is very less
  - (4) None of these

**Answer (2)**

**Sol.** The given sample of water is clean water as BOD value of clean water ranges between 3 to 5.

3. Which of the following chloride is more soluble in organic solvent?
- (1) Be
  - (2) K
  - (3) Ca
  - (4) Mg

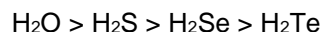
**Answer (1)**

**Sol.** Out of the given elements, the chlorides of K and Ca are largely ionic. So, they will be more soluble in water and less soluble in organic solvents.  $\text{BeCl}_2$  has higher covalent character than  $\text{MgCl}_2$ . Therefore,  $\text{BeCl}_2$  is more soluble in organic solvents than  $\text{MgCl}_2$ .

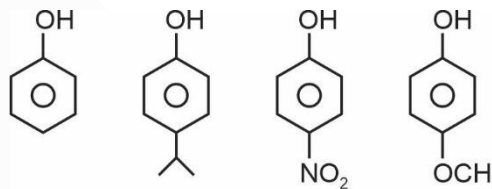
4. The correct order of bond strength  $\text{H}_2\text{O}$ ,  $\text{H}_2\text{S}$ ,  $\text{H}_2\text{Se}$ ,  $\text{H}_2\text{Te}$
- (1)  $\text{H}_2\text{O} > \text{H}_2\text{S} > \text{H}_2\text{Se} > \text{H}_2\text{Te}$
  - (2)  $\text{H}_2\text{S} > \text{H}_2\text{O} > \text{H}_2\text{Se} > \text{H}_2\text{Te}$
  - (3)  $\text{H}_2\text{Te} > \text{H}_2\text{Se} > \text{H}_2\text{S} > \text{H}_2\text{O}$
  - (4)  $\text{H}_2\text{Te} > \text{H}_2\text{S} > \text{H}_2\text{O} > \text{H}_2\text{Se}$

**Answer (1)**

**Sol.** The correct order of bond strength is



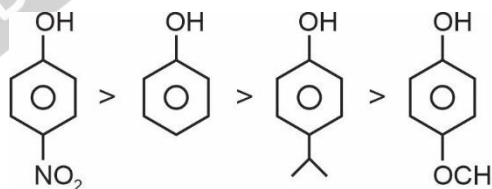
5. The correct order of acidic strength of the following compounds is



- (a)                      (b)                      (c)                      (d)
- (1)  $a > b > c > d$                       (2)  $c > a > b > d$
- (3)  $d > c > b > a$                       (4)  $c > b > a > d$

**Answer (2)**

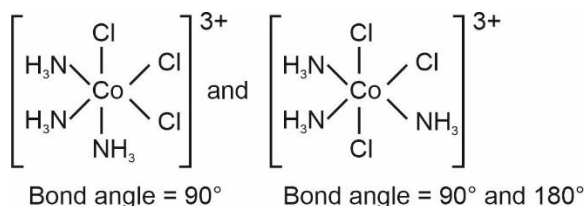
**Sol.** The correct acidic order is



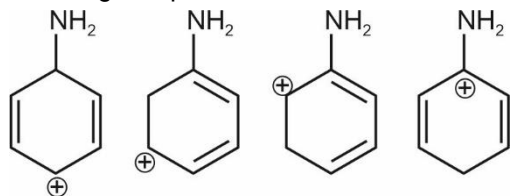
6. What is  $\text{Cl} - \text{Co} - \text{Cl}$  bond angle in  $[\text{Co}(\text{NH}_3)_3\text{Cl}_3]$ ?
- (1)  $120^\circ$  and  $90^\circ$
  - (2)  $90^\circ$  and  $180^\circ$
  - (3)  $90^\circ$
  - (4)  $180^\circ$

**Answer (2)**

**Sol.**



7. The correct decreasing order of stability of the following compounds is

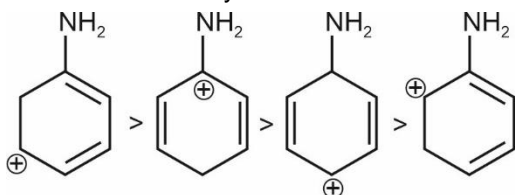


(a) (b) (c) (d)

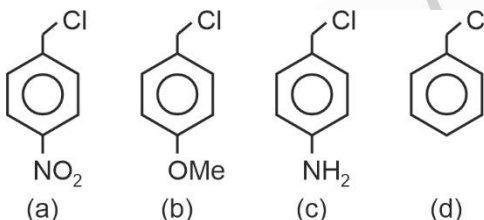
- (1)  $a > b > c > d$   
 (2)  $d > b > c > a$   
 (3)  $b > d > a > c$   
 (4)  $b > a > d > c$

**Answer (3)**

**Sol.** The correct stability order is



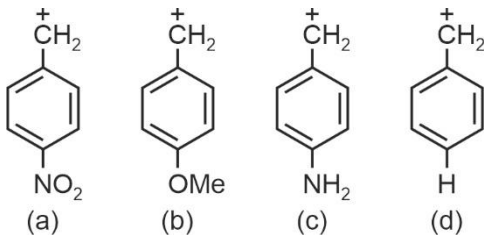
8. Which of the following is correct order of  $S_N1$  reaction?



- (a) (b) (c) (d)
- (1)  $a > b > c > d$  (2)  $c > b > d > a$   
 (3)  $c > a > b > d$  (4)  $d > a > b > c$

**Answer (2)**

**Sol.** The reactivity order of the given aralkyl halides towards  $S_N1$  reaction will be decided by the stability of their corresponding carbocations.



The benzyl carbocation is stabilised by resonance. The presence of  $-NH_2$  group at the p-position promotes the resonance stabilisation due to +R effect. The  $-OMe$  group also promotes but to a lesser extent due to higher electronegativity of O-atom than N-atom. The  $-NO_2$  group opposes the resonance stabilisation due to its  $-R$  effect.

$\therefore$  The correct order is  $c > b > d > a$ .

9. Lead storage battery have 38% (w/w)  $H_2SO_4$ . Find the temperature at which the liquid of battery will freeze

$$(i = 2.67); k_f \text{ of water} = 1.86 \frac{K \cdot kg}{mole}$$

- (1)  $-3.1^\circ C$   
 (2)  $-31^\circ C$   
 (3)  $-0.31^\circ C$   
 (4)  $-0.031^\circ C$

**Answer (2)**

**Sol.**  $\Delta T_f = i k_f m$

$$= (2.67)(1.86)(m)$$

$$m = \frac{38(1000)}{(98)(62)} = 6.25$$

$$\Delta T_f = (2.67)(1.86)(6.25) = 31.06^\circ C$$

$$\text{Freezing point} = -31.06^\circ C$$

10.  $KMnO_4$  oxidises  $I^-$  in acidic & neutral medium in which form – respectively.

- (1)  $IO_3^-, IO_3^-$   
 (2)  $IO_3^-, IO_3^-$   
 (3)  $IO_3^-, I_3^-$   
 (4)  $I_2, IO_3^-$

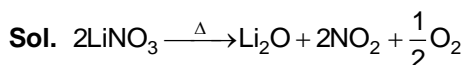
**Answer (4)**

**Sol.**  $I^-$  converts to  $I_2$  in acidic medium and converts to  $IO_3^-$  in neutral medium.

11. Which of the following equation is correct?

- (1)  $LiNO_3 \rightarrow Li + NO_2 + O_2$   
 (2)  $LiNO_3 \rightarrow LiNO_2 + O_2$   
 (3)  $LiNO_3 \rightarrow Li_2O + NO_2 + O_2$   
 (4)  $LiNO_3 \rightarrow Li_2O + N_2O_4 + O_2$

**Answer (3)**





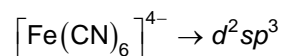
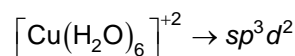
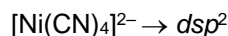
12. The option containing correct match is

(List-I)	(List-II)
A. $\text{Ni}(\text{CO})_4$	(i) $sp^3$
B. $[\text{Ni}(\text{CN})_4]^{2-}$	(ii) $sp^3d^2$
C. $[\text{Cu}(\text{H}_2\text{O})_6]^{+2}$	(iii) $d^2sp^3$
D. $[\text{Fe}(\text{CN})_6]^{4-}$	(iv) $dsp^2$

- (1) A(i), B(iv), C(ii), D(iii)  
 (2) A(iii), B(ii), C(iv), D(i)  
 (3) A(ii), B(iii), C(iv), D(i)  
 (4) A(iv), B(ii), C(i), D(iii)

#### Answer (1)

**Sol.**  $\text{Ni}(\text{CO})_4 \rightarrow sp^3$



13. Statement 1:– Antihistamine prevents the secretion of acid in stomach

Statement 2: – Antiallergic and antacid work on same receptors

- (1) 1 is correct, 2 is incorrect  
 (2) Both are correct  
 (3) 1 is incorrect, 2 is correct  
 (4) Both are incorrect

#### Answer (4)

**Sol.** Antihistamines do not affect the secretion of acid in stomach. Antiallergic and antacid drugs work on different receptors. Therefore, both the statements are incorrect.

14. **Statement-1:** During hall-heroult process mixing of  $\text{CaF}_2$  and  $\text{Na}_3\text{AlF}_6$  decreases the M.P. of  $\text{Al}_2\text{O}_3$ .

**Statement-2:** During electrolytic refining Anode is pure and cathode is impure.

- (1) Both are correct  
 (2) Statement-1 is correct, statement-2 is incorrect  
 (3) Both are incorrect  
 (4) Statement-1 is incorrect, statement-2 is correct

#### Answer (2)

**Sol.** Mixture of  $\text{CaF}_2$  and  $\text{Na}_3\text{AlF}_6$  decreases the melting point of  $\text{Al}_2\text{O}_3$ .

15. Nessler's reagent is

- (1)  $\text{K}_2[\text{HgI}_4]$   
 (2)  $\text{K}_3[\text{HgI}_4]$   
 (3)  $\text{Hg}_2\text{I}_2$   
 (4)  $\text{HgI}_2$

#### Answer (1)

**Sol.** Nessler's reagent is  $\text{K}_2[\text{HgI}_4]$

16. Boric acid is present in solid state while  $\text{BF}_3$  is a gas at room temperature because

- (1) Hydrogen bonding is present in boric acid  
 (2) Boric acid has more molar mass as compared to  $\text{BF}_3$   
 (3)  $\text{BF}_3$  is polymeric in nature  
 (4) Both (2) and (3)

#### Answer (1)

**Sol.** Due to H-bonding, boric acid is solid at room temperature.

17.

18.

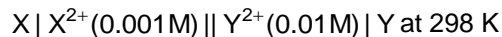
19.

20.

### SECTION - B

**Numerical Value Type Questions:** This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a **NUMERICAL VALUE**. For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g. 06.25, 07.00, -00.33, -00.30, 30.27, -27.30) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.

21. For given  $E_{\text{cell}}$ ,



$$E_{X^{2+}/X}^{\circ} = -0.76$$

$$E_{Y^{2+}/Y}^{\circ} = +0.34$$

$$\frac{2.303 RT}{F} = 0.06$$

If  $E_{\text{cell}} = t$ , find  $5t$  (closest integer).

**Answer (6)**

$$\text{Sol. } E_{\text{cell}} = E_{\text{cell}}^{\circ} - \frac{0.06}{2} \log \frac{10^{-3}}{10^{-2}}$$

$$= 1.10 - 0.03 (-1)$$

$$= 1.10 + 0.03$$

$$t = 1.13 \text{ V}$$

$$5t = 5.65 \text{ V}$$

Nearest integer = 6

22. Find the number of formula units of FeO per unit cell (Round off to the nearest integer)

Given that density =  $4.0 \text{ gm/cm}^3$

$$a = 5 \text{ \AA}$$

$$N_A = 6.0 \times 10^{23}$$

**Answer (04)**

$$\text{Sol. Density} = \frac{ZM}{N_A \times a^3} \Rightarrow Z = \frac{\text{density} \times N_A \times a^3}{M}$$

$$= \frac{4 \times 6.0 \times 10^{23} \times (5 \times 10^{-8})^3}{(56 + 16)}$$

$$= \frac{4 \times 6 \times 125 \times 10^{-1}}{72} = 4.16$$

23. For 1<sup>st</sup> order reaction, 540 s is required for 60% completion, then the time for 90% completion is  $1.35 \times 10^x$ . Find  $x$ .

$$(\log^4 = 0.6)$$

**Answer (3)**

$$\text{Sol. } \frac{t_{90}}{t_{60}} = \frac{\log \frac{100}{100-90}}{\log \left( \frac{100}{100-60} \right)} = \frac{1}{\log \frac{10}{4}} = \frac{1}{1-0.6} = \frac{1}{0.4}$$

$$t_{90} = \frac{540}{0.4} = 1350 \text{ sec}$$

$$1350 = 1.35 \times 10^x$$

$$x = 3$$

24. 1 mole of a gas undergoes adiabatic process given that  $C_V = 20 \text{ JK}^{-1} \text{ mol}^{-1}$ ,  $w = 3 \text{ kJ}$ ,  $T_1 = 27^\circ\text{C}$ ,  $T_2 = ?$  ( $^\circ\text{C}$ )

**Answer (177)**

$$\text{Sol. } w = + nC_V(T_2 - T_1)$$

$$3000 = 1 \times 20 \times (T_2 - 300)$$

$$150 = T_2 - 300$$

$$T_2 = 450 \text{ K}$$

$$\Rightarrow T_2 = 177^\circ\text{C}$$

25. Volume strength of  $\text{H}_2\text{O}_2$  solution is 60 'V', strength of solution is \_\_\_\_\_ g/L.

(Round off to the nearest integer)

**Answer (182)**

**Sol.** Volume strength of  $\text{H}_2\text{O}_2 = 60$  volume

$$\text{Molarity of } \text{H}_2\text{O}_2 \text{ solution} = \frac{60}{11.2} \text{ M}$$

$$\text{Strength of } \text{H}_2\text{O}_2 \text{ solution} = \frac{60 \times 34}{11.2}$$

$$= 182.14 \text{ g/L}$$

$$\approx 182 \text{ g/L}$$

26.

27.

28.

29.

30.

MATHEMATICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.

Choose the correct answer :

- 1. Common tangent is drawn to y^2 = 16x and x^2 + y^2 = 8. Find square of distance between point of contact of common tangent on both the curves. (1) 78 (2) 72 (3) 42 (4) 76

Answer (2)

Sol. y = mx + 4/m

Perpendicular from (0,0)

|4/m|/sqrt(m^2 + 1) = sqrt(8)

=> m = +/- 1

Point of contact on parabola = (a/m^2, 2a/m) = (4, +/-8)

Point of contact in circle = (-2, 2) OR (2, -2)

Distance between (4, 8) & (-2, 2) = sqrt(72)

- 2. Let f(x) = { x/|x|, x != 0; 1, x = 0

g(x) = { sin(x+1)/(x+1), x != -1; 1, x = -1

h(x) = 2[x] + f(x)

([.] denotes greatest integer function)

then limit g(h(x-1)) is

- (1) sin1/1 (2) sin2/2 (3) -1 (4) 2

Answer (2)

Sol. h(x-1) = 2[x-1] + f(x-1)

lt h(x-1) = 2.0 + f(0+) = 1 as x->1+

lt h(x-1) = 2(-1) + f(0-) = -3 as x->1-

RHL

lt g(h(x-1)) = sin2/2 as x->1+

LHL

lt g(h(x-1)) = sin2/2 as x->1-

LHL = RHL

therefore limit g(h(x-1)) = sin2/2

- 3. If |a| = 1, |b| = 2, a . b = 4, c = 2(a x b) - 3b then b . c equals (1) -48 (2) -12 (3) 12 (4) 48

Answer (2)

Sol. c = 2(a x b) - 3b

b . c = -3b . b = -3|b|^2 = -12

- 4. limit n->inf 3/n [4 + (2+1/n)^2 + (2+2/n)^2 + ... + (3-1/n)^2] is (1) 19 (2) 21 (3) -19 (4) 0

Answer (1)

Sol. limit n->inf 3/n sum r=0 to n-1 (2+r/n)^2

= 3 integral 0 to 1 (2+x)^2 dx

= 3 [(2+x)^3 / 3] 0 to 1

= 27 - 8 = 19

5. Let  $f(x) = \sqrt{3-x} + \sqrt{x+2}$ . The range of  $f(x)$  is

- (1)  $[2\sqrt{2}, \sqrt{10}]$                       (2)  $[\sqrt{5}, \sqrt{10}]$   
 (3)  $[\sqrt{2}, \sqrt{7}]$                         (4)  $[\sqrt{7}, \sqrt{10}]$

**Answer (2)**

**Sol.**  $y = \sqrt{3-x} + \sqrt{x+2}$

$$y' = \frac{1}{2\sqrt{3-x}}(-1) + \frac{1}{2\sqrt{x+2}} = 0$$

$$\Rightarrow \sqrt{x+2} = \sqrt{3-x}$$

$$\Rightarrow x = \frac{1}{2}$$

$$\Rightarrow y\left(\frac{1}{2}\right) = \sqrt{\frac{5}{2}} + \sqrt{\frac{5}{2}}$$

$$y_{\max} = \sqrt{10}$$

$y_{\min}$  at  $x = -2$  or  $x = 3$  is  $\sqrt{5}$

$$\therefore y \in [\sqrt{5}, \sqrt{10}]$$

6. The value of  $\tan^{-1}\left(\frac{1}{1+a_1a_2}\right) + \tan^{-1}\left(\frac{1}{1+a_2a_3}\right) + \dots + \tan^{-1}\left(\frac{1}{1+a_{2021}a_{2022}}\right)$

if  $a_1 = 1$  and  $a_i$  are consecutive natural numbers

- (1)  $\frac{\pi}{4} - \cot^{-1}(2021)$   
 (2)  $\frac{\pi}{4} - \cot^{-1}(2022)$   
 (3)  $\frac{\pi}{4} - \tan^{-1}(2021)$   
 (4)  $\frac{\pi}{4} - \tan^{-1}(2022)$

**Answer (2)**

**Sol.**  $\tan^{-1}\left(\frac{a_2 - a_1}{1 + a_1a_2}\right) + \tan^{-1}\left(\frac{a_3 - a_2}{1 + a_2a_3}\right) + \dots +$

$$\tan^{-1}\left(\frac{a_{2022} - a_{2021}}{1 + a_{2021}a_{2022}}\right)$$

$$= (\tan^{-1} a_2 - \tan^{-1} a_1) + (\tan^{-1} a_3 - \tan^{-1} a_2) + \dots +$$

$$(\tan^{-1} a_{2022} - \tan^{-1} a_{2021})$$

$$= \tan^{-1} a_{2022} - \tan^{-1} a_1$$

$$\therefore a_1 = 1, a_2 = 2 \dots a_{2022} = 2022$$

$$= \tan^{-1} 2022 - \tan^{-1} 1$$

$$= \tan^{-1} 2022 - \frac{\pi}{4}$$

$$= \frac{\pi}{2} - \cot^{-1} 2022 - \frac{\pi}{4}$$

$$= \frac{\pi}{4} - \cot^{-1} 2022$$

7. Let  $P = (8\sqrt{3} + 13)^{13}$ ,  $Q = (6\sqrt{2} + 9)^9$  then (where  $[ ]$  represents greatest integer function)

- (1)  $[P] = \text{Odd}, [Q] = \text{Even}$   
 (2)  $[P] = \text{Even}, [Q] = \text{Odd}$   
 (3)  $[P] = \text{Odd}, [Q] = \text{Odd}$   
 (4)  $[P] + [Q] = \text{Even}$

**Answer (4)**

**Sol.** Let  $P = I_1 + f_1, f_1' = (8\sqrt{3} - 13)^{13}$

$$I_1 + f_1 - f_1' = (8\sqrt{3} + 13)^{13} - (8\sqrt{3} - 13)^{13}$$

$$= 2 \left( {}^{13}C_1 (8\sqrt{3})^{12} (13)^1 + {}^{13}C_3 (8\sqrt{3})^{10} (13)^3 \right.$$

$$\left. + {}^{13}C_5 (8\sqrt{3})^8 (13)^5 + \dots + {}^{13}C_{13} (8\sqrt{3})^0 (13)^{13} \right)$$

$$f_1 - f_1' = 0$$

So,  $I_1$  is even

Let  $Q = I_2 + f_2, f_2' = (9 - 6\sqrt{2})^9$

$$I_2 + f_2 - f_2' = (9 + 6\sqrt{2})^9 - (9 - 6\sqrt{2})^9$$

$$= 2 \left[ {}^9C_0 9^9 + {}^9C_2 9^7 (6\sqrt{2})^2 + \dots \right]$$

Again  $f_2 - f_2' = 0$

$$I_2 = \text{even}$$

8. Let  $p$ : I am well.

$q$ : I will not take rest

$r$ : I will not sleep properly, then

"If I am not well then I will not take rest and I will not sleep properly" is logically equivalent to

(1)  $(\sim p \rightarrow q) \vee r$                       (2)  $\sim p \rightarrow (q \wedge r)$

(3)  $(\sim p \wedge q) \rightarrow r$                       (4)  $(\sim p \vee q) \rightarrow r$

**Answer (2)**

Sol.  $\sim p$ : I am not well

$q$ : I will not take rest

$r$ : I will not sleep properly

I will not take rest and I will not sleep properly  $\equiv q \wedge r$

If I am not well then I will not take rest and I will not sleep properly  $\equiv \sim p \rightarrow (q \wedge r)$

9.  $q$  is maximum value of  $p$  lying in interval  $[0, 10]$ , roots of  $x^2 - px + \frac{5p}{d} = 0$  are having rational roots.

Find area of region

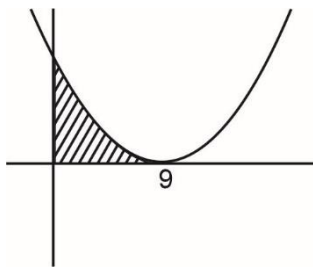
$$S: \{0 \leq y \leq (x - q)^2\}$$

- (1) 243 (2) 723  
(3) 81 (4) 3

Answer (1)

Sol.  $D = p^2 - 5p$  must be a perfect square i.e. possible when  $p = 9$

Region for  $0 \leq y \leq (x - 9)^2$ , in 1<sup>st</sup> quadrant



$$A = \int_0^9 (x-9)^2 dx$$

$$= \frac{(x-9)^3}{3} \Big|_0^9 = 0 + \frac{9^3}{3}$$

$$= 243 \text{ sq. unit}$$

10. If  $\frac{dy}{dx} = -\frac{3x^2 + y^2}{3y^2 + x^2}$ ,  $y(1) = 0$ , then  $f(x)$  is

- (1)  $\log(x+y) + \frac{2xy}{(x+y)^2} = 0$   
 (2)  $\log(x+y) - \frac{2xy}{(x+y)^2} = 0$   
 (3)  $3 = (3y^2 - 2xy + 3x^2)(x+y)^2$   
 (4)  $3 = (3y^2 - 2xy + 3x^2)(x+y)$

Answer (3)

Sol.  $\frac{dy}{dx} = -\frac{3x^2 + y^2}{3y^2 + x^2} = -\frac{3 + \left(\frac{y}{x}\right)^2}{3\left(\frac{y}{x}\right)^2 + 1}$

Let,  $\frac{y}{x} = u$

$$\frac{dy}{dx} = u + x \frac{du}{dx}$$

$$u + x \frac{du}{dx} = \frac{-(3 + u^2)}{3u^2 + 1}$$

$$x \frac{du}{dx} = \frac{-(3 + u^2) - u(3u^2 + 1)}{3u^2 + 1}$$

$$x \frac{du}{dx} = \frac{-[3u^3 + u^2 + u + 3]}{(3u^2 + 1)}$$

$$x \frac{du}{dx} = \frac{-(u+1)(3u^2 - 2u + 3)}{3u^2 + 1}$$

$$\int \frac{3u^2 + 1}{(u+1)(3u^2 - 2u + 3)} du = -\int \frac{dx}{x}$$

$$\int \left[ \frac{1}{u+1} + \frac{1}{4} \frac{(6u-2)}{3u^2 - 2u + 3} \right] du = -\int \frac{dx}{x}$$

$$\frac{1}{2} \ln|(u+1)| + \frac{1}{4} \ln|3u^2 - 2u + 3| = -\ln x + C$$

$$\frac{1}{2} \ln(x+y) - \frac{1}{2} \ln x + \frac{1}{4} \ln(3y^2 - 2xy + 3x^2)$$

$$= -\frac{1}{4} \times 2 \ln x = -\ln x + C$$

$$\ln(x+y)^2 + \ln(3y^2 - 2xy + 3x^2) = C$$

$$(x+y)^2 (3x^2 - 2xy + 3y^2) = C$$

$$y(1) = 0$$

$$\Rightarrow C = 3$$

$$\boxed{(x+y)^2 (3x^2 - 2xy + 3y^2) = 3}$$

11. A bag contains 3 same balls and 3 different balls of three different colours. Two balls are drawn randomly with replacement. The probability they have same colour is  $m$ . Again four balls are drawn one by one with replacement, then probability of getting three same balls is  $n$ . The value of  $m \cdot n$  is

- (1)  $\frac{3}{49}$                       (2)  $\frac{6}{49}$   
 (3)  $\frac{43}{147}$                     (4)  $\frac{8}{81}$

**Answer (4)**

**Sol.** For  $m$

both balls is one of different colours =  $\left(\frac{1}{6} \times \frac{1}{6}\right) \cdot 3$

both balls is from the same balls =  $\frac{1}{2} \times \frac{1}{2}$

$\therefore m = \frac{1}{4} + \frac{1}{12} = \frac{1}{3}$

For  $n$

Same ball is from the different coloured balls

$= 3 \left( 4 \left( \frac{1}{6} \right)^3 \cdot \frac{5}{6} \right)$

Or same ball is from the 3 same balls

$= \left( 4 \left( \frac{1}{2} \right)^3 \cdot \frac{1}{2} \right)$

$\therefore n = \frac{10}{6^3} + \frac{1}{4} = \frac{8}{27}$

$\therefore m \cdot n = \frac{8}{81}$

12.  
13.  
14.  
15.  
16.  
17.  
18.  
19.  
20.

**SECTION - B**

**Numerical Value Type Questions:** This section contains 10 questions. In Section B, attempt any five questions out of 10. The answer to each question is a **NUMERICAL VALUE**. For each question, enter the correct numerical value (in decimal notation, truncated/rounded-off to the second decimal place; e.g. 06.25, 07.00, -00.33, -00.30, 30.27, -27.30) using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.

21. Two A.P.'s are given as under

3, 7, 11, .....

1, 6, 11, 16, .....

Find 8<sup>th</sup> common term that is appearing in both the series

**Answer (151)**

**Sol.** First common term is 11 and common terms will appear in an A.P. having common difference as LCM of (4, 5) = 20

$T_8 = 11 + (8 - 1) \cdot 20$   
 $= 151$

22. Using 1, 2, 2, 2, 3, 3, 5 find number of 7-digit odd numbers that can be formed

**Answer (240)**

**Sol.** ----- 1  $\rightarrow \frac{6!}{2!3!} = 60$

----- 3  $\rightarrow \frac{6!}{3!} = 120$

----- 5  $\rightarrow \frac{6!}{3!2!} = 60$

Total = 240

23. 50<sup>th</sup> root of  $x$  is 12

50<sup>th</sup> root of  $y$  is 18

Remainder when  $x + y$  is divided by 25.

**Answer (23)**

**Sol.**  $12^{50} + 18^{50} = 144^{25} + 324^{25}$   
 $= (25K_1 - 6)^{25} + (25K_2 - 1)^{25}$   
 $= 25\lambda - 6^{25} - 1$

$6^{25} + 1 = (6^5)^5 + 1$   
 $= (7776)^5 + 1$   
 $= (25\lambda_1 + 1)^5 + 1 = 25p + 2$

$\Rightarrow 12^{50} + 18^{50} = 25\lambda - (25p + 2)$

$\Rightarrow$  Remainder = 23

24. Let  $a = \{1, 3, 5, \dots, 99\}$   
and  $b = \{2, 4, 6, \dots, 100\}$

The number of ordered pair  $(a, b)$  such that  $a + b$  when divided by 23 leaves remainder 2 is

**Answer (108)**

**Sol.**  $a + b = 23\lambda + 2$

$\lambda = 0, 1, 2, \dots$

But  $\lambda$  can't be even

$\therefore$  if  $\lambda = 1$   $(a, b) \rightarrow 12$  pairs

$\lambda = 3$   $(a, b) \rightarrow 35$  pairs

$\lambda = 5$   $(a, b) \rightarrow 42$  pairs

$\lambda = 7$   $(a, b) \rightarrow 19$  pairs

$\lambda = 9$   $(a, b) \rightarrow 0$  pairs

$\vdots$

Total =  $12 + 35 + 42 + 19 = 108$  ordered pairs

25. Let a line parallel to  $x + 3y - 2z - 2 = 0 = x - y + 2z$  and passes through  $(2, 3, 1)$ . If distance of point  $(5, 3, 8)$  from the line is  $\alpha$ , then  $3\alpha^2$  is

**Answer (158)**

**Sol.** Let  $\vec{a} = \hat{i} + 3\hat{j} - 2\hat{k}$

$$\vec{b} = \hat{i} - \hat{j} + 2\hat{k}$$

Line will be parallel to  $\vec{a} \times \vec{b}$

$$\vec{a} \times \vec{b} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 3 & -2 \\ 1 & -1 & 2 \end{vmatrix} = \hat{i}(4) - \hat{j}(4) + \hat{k}(-4)$$

$$\Rightarrow \vec{n} = \hat{i} - \hat{j} - \hat{k}$$

$$d = \frac{|(\vec{a}_2 - \vec{a}_1) \times \vec{n}|}{|\vec{n}|}$$

where  $\vec{a}_2 = 5\hat{i} + 3\hat{j} + 8\hat{k}$ ,  $\vec{a}_1 = 2\hat{i} + 3\hat{j} + \hat{k}$

$$\vec{a}_2 - \vec{a}_1 = 3\hat{i} + 7\hat{k}$$

$$(\vec{a}_2 - \vec{a}_1) \times \vec{n} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & 0 & 7 \\ 1 & -1 & -1 \end{vmatrix} = \hat{i}(7) - \hat{j}(-10) + \hat{k}(-3)$$

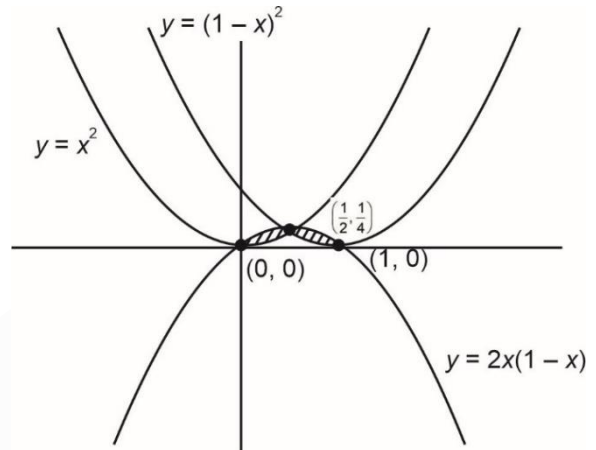
$$d = \frac{\sqrt{100 + 49 + 9}}{\sqrt{3}} = \frac{\sqrt{158}}{\sqrt{3}} = \alpha$$

$$3\alpha^2 = 158$$

26. If area of the region bounded by the curves  $y = x^2$ ,  $y = (1 - x)^2$  and  $y = 2x(1 - x)$  is  $A$ , then find the value of  $540A$ ,

**Answer (135)**

$$\text{Sol. } A = \int_0^1 2x(1-x)dx - \int_0^{\frac{1}{2}} x^2 dx - \int_{\frac{1}{2}}^1 (1-x)^2 dx$$



$$= x^2 - \frac{2x^3}{3} \Big|_0^1 - \frac{x^3}{3} \Big|_0^{\frac{1}{2}} + \frac{(1-x)^3}{3} \Big|_{\frac{1}{2}}^1$$

$$= \frac{1}{4}$$

$$540A = 135$$

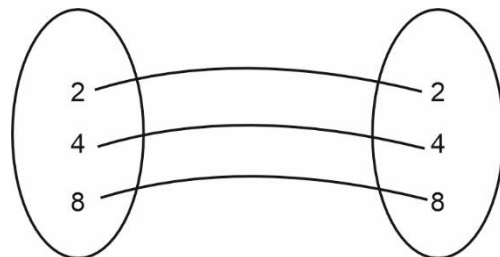
27.  $A = \{2, 4, 6, 8, 10\}$

Find total no. of functions defined on  $A$  such that  $f(m \cdot n) = f(m) \cdot f(n)$ ,  $m, n \in A$

**Answer (25)**

$$\text{Sol. } f(4) = (f(2))^2 = 4$$

$$f(8) = (f(2))^3 = 8$$



For 6 and 10 we have 5 options

$$\text{Total functions} = 5 \times 5 = 25$$

28.

29.

30.

