QUESTION PAPER CODE 65/2/G

EXPECTED ANSWERS/VALUE POINTS

SECTION-A

Marks

1.
$$d.r's \text{ of } \overrightarrow{AB}: 1,-5-a, b-3; d.r's \text{ of } \overrightarrow{BC} \text{ are } -4,16,9-b \text{ or } d.r's \text{ of } \overrightarrow{AC}:-3,11-a,6$$
 ½ m

getting
$$a = -1$$
, $b = 1$, $a + b = 0$

2.
$$\left| \vec{a} \right| \left| \vec{b} \right| \sin \theta = 16 \implies \sin \theta = \frac{16}{20} = \frac{4}{5} \implies \cos \theta = \pm \frac{3}{5}$$

$$\vec{a} \cdot \vec{b} = |\vec{a}| |\vec{b}| \cos \theta = \pm 12$$

3.
$$d = \frac{|9-6|}{\sqrt{2^2 + (-1)^2 + (-2)^2}}$$

$$=1$$
 $\frac{1}{2}$ m

4.
$$3\begin{bmatrix} 2 & 4 \\ 3 & 2 \end{bmatrix} - \begin{bmatrix} -2 & 5 \\ 3 & 4 \end{bmatrix}$$
 ½ m

$$= \begin{bmatrix} 8 & 7 \\ 6 & 2 \end{bmatrix}$$
¹/₂ m

5.
$$y = e^{-x} + ax + b \implies y' = -e^{-x} + a$$

$$y'' = e^{-x}$$
 or $\frac{d^2y}{dx^2} = e^{-x}$

6. Order = 2, degree = 2 (any one correct)
$$\frac{1}{2}$$
 m

$$Sum = 2 + 2 = 4$$

SECTION - B

7. Given
$$\frac{x}{x-y} = \log a - \log (x-y)$$

Differentiating both sides and getting $[: X \neq y]$

$$x - 2y + y \frac{dy}{dx} = 0$$

$$2\frac{1}{2}m$$

$$\Rightarrow \frac{dy}{dx} = \frac{2y - x}{y}$$

$$\Rightarrow \frac{\mathrm{dy}}{\mathrm{dx}} = 2 - \frac{x}{y}$$

8. $I = \int \frac{dx}{x^3 (x^5 + 1)^{\frac{3}{5}}}$ $= \int \frac{dx}{x^3 x^3 (1 + \frac{1}{x^5})^{\frac{3}{5}}}$ India's largest Student Review Platform

$$= \int \frac{dx}{x^3 \cdot x^3 \left(1 + \frac{1}{x^5}\right)^{\frac{3}{5}}} \quad \text{India's large}$$

$$1\frac{1}{2} 1$$

Put
$$1 + \frac{1}{x^5} = 1$$

$$\Rightarrow \frac{dx}{x^6} = -\frac{dt}{5}$$

$$\therefore I = -\frac{1}{5} \int t^{-3/5} dt = -\frac{1}{2} t^{2/5} + C$$

$$= -\frac{1}{2} \left(1 + \frac{1}{x^5} \right)^{\frac{2}{5}} + C$$
 \frac{1}{2} m

9.
$$I = \int_{2}^{4} |x-2| dx + \int_{2}^{4} |x-3| dx + \int_{2}^{4} |x-4| dx$$

$$= \int_{2}^{4} (x-2) dx + \int_{2}^{3} -(x-3) dx + \int_{3}^{4} (x-3) dx + \int_{2}^{4} -(x-4) dx$$

$$= \left[\frac{x^2}{2} - 2x\right]_2^4 - \left[\frac{x^2}{2} - 3x\right]_2^3 + \left[\frac{x^2}{2} - 3x\right]_3^4 - \left[\frac{x^2}{2} - 4x\right]_2^4$$
1 m

$$= 5$$

OR

$$I = \int_{0}^{\frac{\pi}{4}} \frac{\sec x}{1 + 2\sin^{2}x} dx = \int_{0}^{\frac{\pi}{4}} \frac{\cos x}{\cos^{2}x (1 + 2\sin^{2}x)} dx$$

$$I = \int_{0}^{\frac{\pi}{4}} \frac{\sec x}{1 + 2\sin^{2}x} dx = \int_{0}^{\frac{\pi}{4}} \frac{\cos x}{\cos^{2}x (1 + 2\sin^{2}x)} dx$$

$$= \int_{0}^{\frac{\pi}{4}} \frac{\cos x}{(1 - \sin x) (1 + \sin x) (1 + 2\sin^{2}x)} dx$$
1 m

Put $\sin x = t \Rightarrow \cos x \, dx = dt$, when x = 0, t = 0

$$x = \frac{\pi}{4}, \ t = \frac{1}{\sqrt{2}}$$

$$I = \int_{0}^{1/\sqrt{2}} \frac{dt}{(1-t)(1+t)(1+2t^{2})}$$

$$\therefore I = \int_{0}^{1/\sqrt{2}} \frac{dt}{6(1-t)} + \int_{0}^{1/\sqrt{2}} \frac{dt}{6(1+t)} + \int_{0}^{1/\sqrt{2}} \frac{2 dt}{3(1+2t^{2})}$$
1 m

$$= \left[\frac{1}{6}\log\left|\frac{1+t}{1-t}\right| + \frac{\sqrt{2}}{3}\tan^{-1}\left(\sqrt{2}t\right)\right]_0^{\frac{1}{\sqrt{2}}}$$

$$= \frac{1}{6} \log \left| \frac{1 + \frac{1}{\sqrt{2}}}{1 - \frac{1}{\sqrt{2}}} \right| + \frac{\sqrt{2}}{3} \tan^{-1} (1)$$



$$= \frac{1}{3} \log \left| \sqrt{2} + 1 \right| + \frac{\pi}{6\sqrt{2}} \quad or \quad \frac{1}{6} \log \left(3 + 2\sqrt{2} \right) + \frac{\pi}{6\sqrt{2}}$$

10. LHS =
$$\sin \left[\cot^{-1} \left(\frac{2x}{1 - x^2} \right) + 2 \tan^{-1} x \right]$$

$$= \sin \left[\frac{\pi}{2} - \tan^{-1} \left(\frac{2x}{1 - x^2} \right) + 2 \tan^{-1} x \right]$$

$$= \sin \left[\frac{\pi}{2} - 2 \tan^{-1} x + 2 \tan^{-1} x\right]$$

$$=\sin \frac{\pi}{2} = 1 = \text{R.H.S}$$

$$= \sin \frac{\pi}{2} = 1 = \text{R.H.S}$$
OR
$$\tan^{-1} \left(\frac{\frac{x-5}{x-6} + \frac{x+5}{x+6}}{\frac{x-5}{x-6} \cdot \frac{x+5}{x+6}} \right) = \frac{\pi}{4}$$

$$2 \text{ m}$$

$$\Rightarrow \frac{(x-5)(x+6)+(x+5)(x-6)}{x^2-36-x^2+25} = \tan\frac{\pi}{4}$$

$$\Rightarrow 2x^2 = 49$$

$$\Rightarrow x = \pm \frac{7}{\sqrt{2}}$$

11. L.H.S. =
$$\begin{vmatrix} 1+a^2-b^2 & 2ab & -2b \\ 2ab & 1-a^2+b^2 & 2a \\ 2b & -2a & 1-a^2-b^2 \end{vmatrix}$$

$$R_1 \rightarrow R_1 + b \cdot R_3$$
, $R_2 \rightarrow R_2 - a R_3$

$$= \begin{vmatrix} 1+a^2+b^2 & 0 & -b(1+a^2+b^2) \\ 0 & 1+a^2+b^2 & a(1+a^2+b^2) \\ 2b & -2a & 1-a^2-b^2 \end{vmatrix}$$
 1+1 m

$$= (1+a^2+b^2)^2 \begin{vmatrix} 1 & 0 & -b \\ 0 & 1 & a \\ 2b & -2a & 1-a^2-b^2 \end{vmatrix}$$
 1 m

Expanding and getting

$$\Delta = (1 + a^2 + b^2)^3 = R.H.S.$$
 1 m

12.
$$A^{2} = \begin{pmatrix} 6 & -5 & 5 \\ -5 & 6 & -5 \\ 5 & -5 & 6 \end{pmatrix}$$

2.
$$A^{2} = \begin{pmatrix} 6 & -5 & 5 \\ -5 & 6 & -5 \\ 5 & -5 & 6 \end{pmatrix}$$

$$A^{2} - 5A + 4I = \begin{pmatrix} 6 & -5 & 5 \\ -5 & 6 & -5 \\ 5 & -5 & 6 \end{pmatrix} - \begin{pmatrix} 10 & -5 & 5 \\ -5 & 10 & -5 \\ 5 & -5 & 10 \end{pmatrix} + \begin{pmatrix} 4 & 0 & 0 \\ 0 & 4 & 0 \\ 0 & 0 & 4 \end{pmatrix}$$

$$1 \text{ m}$$
Pro multiplying by A^{-1} and getting $A^{-1} = \frac{1}{2}(5I - A)$

Pre multiplying by
$$A^{-1}$$
 and getting $A^{-1} = \frac{1}{4} (5 I - A)$

and
$$A^{-1} = \frac{1}{4} \begin{pmatrix} 3 & 1 & -1 \\ 1 & 3 & 1 \\ -1 & 1 & 3 \end{pmatrix}$$
 1 m

OR

$$A = IA$$

$$\Rightarrow \begin{pmatrix} 0 & 1 & 2 \\ 1 & 2 & 3 \\ 3 & 1 & 0 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} A$$



$$R_1 \leftrightarrow R_2$$

$$\begin{pmatrix} 1 & 2 & 3 \\ 0 & 1 & 2 \\ 3 & 1 & 0 \end{pmatrix} = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix} A$$

$$R_3 \rightarrow R_3 - 3R_1$$

$$\begin{pmatrix} 1 & 2 & 3 \\ 0 & 1 & 2 \\ 0 & -5 & -9 \end{pmatrix} = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & -3 & 1 \end{pmatrix} A$$

$$R_1 \rightarrow R_1 - 2R_2$$
, $R_3 \rightarrow R_3 + 5R_2$

$$\begin{pmatrix} 1 & 0 & -1 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} -2 & 1 & 0 \\ 1 & 0 & 0 \\ 5 & -3 & 1 \end{pmatrix} A$$

$$= \begin{pmatrix} -2 & 1 & 0 \\ 1 & 0 & 0 \\ 5 & -3 & 1 \end{pmatrix} A$$

$$= \begin{pmatrix} -2 & 1 & 0 \\ 1 & 0 & 0 \\ 5 & -3 & 1 \end{pmatrix} A$$

$$= \begin{pmatrix} -2 & 1 & 0 \\ 1 & 0 & 0 \\ 5 & -3 & 1 \end{pmatrix} A$$

$$R_1 \to R_1 + R_3$$
, $R_2 \to R_2 - 2R_3$

$$\begin{pmatrix}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{pmatrix} = \begin{pmatrix}
3 & -2 & 1 \\
-9 & 6 & -2 \\
5 & -3 & 1
\end{pmatrix}$$
 A [operating Row wise to reach at this step] $2\frac{1}{2}$ m

$$A^{-1} = \begin{pmatrix} 3 & -2 & 1 \\ -9 & 6 & -2 \\ 5 & -3 & 1 \end{pmatrix}$$
¹/₂ m

13. A Candidate who has made an attempt to solve the question

to be given 4 marks

14.
$$y = -x^3 \log x$$

$$\frac{\mathrm{dy}}{\mathrm{dx}} = -x^2 \left(1 + 3 \log x\right)$$



$$\frac{d^2y}{dx^2} = -(5x + 6x \log x)$$

OR

$$f(x) = (x-4)](x-6)(x-8)$$
$$= x^3 - 18 x^2 + 104 x - 192$$

= R.H.S.

Being a polynomial function f(x) is continuous

in [4, 10] and differentiable in (4, 10) with

$$f(h) = f(a)$$

f'(x) =
$$3x^2 - 36x + 104$$

$$\exists c \in (4,10) \cdot \text{such that} \quad f'(c) = \frac{f(b) - f(a)}{b - a}$$

$$\Rightarrow 3c^2 - 36c + 104 = 8$$

$$\Rightarrow c = 4, 8$$

$$\therefore c = 8 : \text{ verifies the theoren}$$

1+1 m

1+1 m

1/2 m

$$\Rightarrow$$
 c = 4, 8 md ; c = 4 \notin (4, 10)

$$c = 8$$
: verifies the theoren

Equation of line joining (4, 3, 2) and (1, -1, 0) is 15.

$$\frac{x-4}{-3} = \frac{y-3}{-4} = \frac{z-2}{-2}$$

Equation of line joining (1, 2, -1) and (2, 1, 1) is

$$\frac{x-1}{1} = \frac{y-2}{-1} = \frac{z+1}{2}$$

Let equation of the required line be

$$\frac{x-1}{a} = \frac{y+1}{b} = \frac{z-1}{c} = \lambda$$
(i)



According to the question 3a + 4b + 2c = 0

$$a - b + 2c = 0$$

Solving,
$$\frac{a}{10} = \frac{b}{-4} = \frac{c}{-7} = \mu$$

$$\Rightarrow$$
 a = 10μ , b = -4μ , c = -7μ

Equation of the line is

$$\frac{x-1}{10} = \frac{y+1}{-4} = \frac{z-1}{-7}$$
 [cartesian form]

$$\frac{x-1}{10} = \frac{y+1}{-4} = \frac{z-1}{-7} \text{ [cartesian form]}$$
Vector form, $\vec{r} = (\hat{i} - \hat{j} + \hat{k}) + \lambda (10\hat{i} - 4\hat{j} - 7\hat{k})$

$$16. \qquad H R HW$$

$$A \begin{bmatrix} 3 & 4 & 6 \\ 4 & 5 & 3 \\ C & 6 & 2 & 4 \end{bmatrix} \begin{bmatrix} 2500 \\ 3100 \\ 5100 \end{bmatrix}$$

$$1 \text{ m}$$

$$= \begin{bmatrix} 50500 \\ 40800 \\ 41600 \end{bmatrix}$$
 1 m

Hence money awarded by A = Rs. 50500

money awarded by
$$B = Rs. 40800$$

money awarded by C = Rs. 41600

Respect for elders or Any relevant value 1 m

17.
$$I = \int_{\frac{\pi}{4}}^{\frac{\pi}{2}} e^{2x} \left(\frac{1 - \sin 2x}{1 - \cos 2x} \right) dx$$

$$= \int_{\frac{\pi}{4}}^{\frac{\pi}{2}} e^{2x} \left(\frac{1 - 2\sin\cos x}{2\sin^2 x} \right) dx$$

$$= \int_{\frac{\pi}{4}}^{\frac{\pi}{2}} e^{2x} \left(\frac{1}{2} \operatorname{cosec}^{2} x - \cot x \right) dx$$

Put $2x = t \implies dx = \frac{dt}{2}$

$$\therefore I = \frac{1}{2} \int_{\pi/2}^{\pi} e^{t} \left(\frac{1}{2} \operatorname{cosec}^{2} \frac{t}{2} - \cot \frac{t}{2} \right) dt$$

when
$$x = \frac{\pi}{4}$$
, $t = \frac{\pi}{2}$; $x = \frac{\pi}{2}$, $t = \pi$

$$\therefore I = \frac{1}{2} \int_{\frac{\pi}{2}}^{\pi} e^{t} \left(\frac{1}{2} \csc^{2} \frac{t}{2} - \cot \frac{t}{2}\right) dt$$

$$= -\frac{1}{2} \left[\cot \frac{t}{2} \cdot e^{t}\right]_{\frac{\pi}{2}}^{\pi}$$

1 m

$$=\frac{e^{\pi/2}}{2}$$
¹/₂ m

18. Let
$$\overrightarrow{OA} = 4\hat{i} + 8\hat{j} + 12\hat{k}$$
, $\overrightarrow{OB} = 2\hat{i} + 4\hat{j} + 6\hat{k}$

$$\overrightarrow{OC} = 3\hat{i} + 5\hat{j} + 4\hat{k}, \overrightarrow{OD} = 5\hat{i} + 8\hat{j} + 5\hat{k}$$

$$\overrightarrow{AB} = -2\hat{i} - 4\hat{j} - 6\hat{k}, \ \overrightarrow{AC} = -\hat{i} - 3\hat{j} - 8\hat{k}, \ \overrightarrow{AD} = \hat{i} - 7\hat{k}$$

Now,
$$\begin{bmatrix} \overrightarrow{AB} & \overrightarrow{AC} & \overrightarrow{AD} \end{bmatrix} = \begin{vmatrix} -2 & -4 & -6 \\ -1 & -3 & -8 \\ 1 & 0 & -7 \end{vmatrix} = 0$$
 2 m

 $1\frac{1}{2}$ m

 $1\frac{1}{2}$ m

E₁: Event that transferred ball is black

E₂: Event that transferred ball is Red

E₃: Event that balls drawn are black

$$P(E_1) = \frac{5}{9}, \quad P(E_2) = \frac{4}{9}$$
 1 m

$$P(A/E_1) = \frac{{}^5C_2}{{}^8C_2} = \frac{5}{14}, \quad P(A/E_2) = \frac{{}^4C_2}{{}^8C_2} = \frac{3}{14}$$

$$P(E_1/A) = \frac{P(E_1) \cdot P(A/E_1)}{P(E_1) P(A/E_1) + P(E_2) P(A/E_2)}$$
1/2 m

$$= \frac{\frac{5}{9} \times \frac{5}{14}}{\frac{5}{9} \times \frac{5}{14} + \frac{4}{9} \times \frac{3}{14}}$$

$$= \frac{25}{37}$$

$$SECTION - C$$

$$(y - \sin x) dx + (\tan x) dy = 0 \Rightarrow \frac{dy}{dx} + \cot x y = \cos x$$

$$1 \text{ m}$$
Linear diff. equ. with $P = \cot x$, $Q = \cos x$

$$1.F. = \sin x$$

$$1 \text{ m}$$

=
$$\frac{25}{37}$$
 | Student Review Platform 1/2 m

20.
$$(y-\sin x) dx + (\tan x) dy = 0 \Rightarrow \frac{dy}{dx} + \cot x y = \cos x$$

$$1.F. = \sin x$$

Solution is $y \cdot \sin x = \int \cos x \cdot \sin x \, dx + c$

$$= -\frac{1}{4}\cos 2x + c$$
 2 m

when
$$x = 0$$
, $y = 0 \implies c = \frac{1}{4}$

Particular solution is

$$y \sin x = \frac{1}{4} (-\cos 2x + 1) = \frac{\sin^2 x}{2}$$

$$\Rightarrow y = \frac{1}{2}\sin x$$

21.
$$d \cdot r's$$
 of first line : $k - 5$, 1, $2k + 1$

$$d \cdot r's$$
 of 2nd line : -1 , k, 5

1 m

1 m

$$\therefore$$
 lines are \perp : $-1(k-5)+k(1)+5(2k+1)=0$

$$\Rightarrow k = -1$$

Eqns of lines become
$$\frac{x+3}{-6} = \frac{y-1}{-1} = \frac{z-5}{-1}$$
 and $\frac{x+2}{-1} = \frac{y-2}{-1} = \frac{z}{5}$

Eqn of plane containing these two lines is

$$\begin{vmatrix} x+2 & y-2 & z \\ -6 & 1 & -1 \\ -1 & -1 & 5 \end{vmatrix} = 0$$

$$\Rightarrow 4x+31y+7z=54$$
1 m

2. $(a,b)*(c,d)=(a+c,b+d) \quad \forall \ a,b,c,d \in \mathbb{R}$
Since $a+c \in \mathbb{R}$ and $b+d \in \mathbb{R} \Rightarrow (a+c,b+d) \in \mathbb{R} \times \mathbb{R}$
i.e. '*' is binary operation

$$\Rightarrow$$
 4 x + 31 y + 7z = 54

22.
$$(a,b) * (c,d) = (a+c,b+d) \forall a,b,c,d \in R$$

Since
$$a + c \in R$$
 and $b + d \in R \Rightarrow (a + c, b + d) \in R \times R$
i.e. '*' is binary operation

For commutative

consider
$$(c, d) * (a, b) = (c + a, d + b)$$

$$= (a + c, b + d)$$

$$= (a, b) * (c, d)$$

$$\Rightarrow '*' \text{ is commutative}$$

$$1 \frac{1}{2} \text{ m}$$

For Associative

Let
$$(a, b)$$
, (c, d) , $(e, f) \in R \times R = A$

$$[(a, b) * (c, d)] * (e, f) = (a + c, b + d) * (e, f)$$

$$= (a + c + e, b + d + f) \dots (i)$$

$$= (a + c + e, b + d + f)$$

$$= (a + c + e, b + d + f) \dots (ii)$$

$$= (a + c + e, b + d + f) \dots (ii)$$



(i) & (ii) \Rightarrow '*' is associative

For identity element

Let $(e_1, e_2) \in \mathbb{R} \times \mathbb{R}$ be the identity element (if exists)

then
$$(a, b) * (e_1, e_2) = (a, b) = (e_1, e_2) * (a, b)$$

$$\Rightarrow (e_1, e_2) = (0, 0) \in R \times R$$
1½ m

OR

$$f(x) = x^2 - x; x \in \{-1, 0, 1, 2\}$$

$$f(-1) = 2$$
, $f(0) = 0$, $f(1) = 0$, $f(2) = 2$

$$f = \{(-1, 2), (0, 0), (1, 0), (2, 2)\}$$

 $2 \, \mathrm{m}$

$$g(x) = 2 \left| x - \frac{1}{2} \right| - 1 \quad \forall \ x \in \{-1, 0, 1, 2\}$$

$$g(-1) = 2, \ g(0) = 0, \ g(1) = 0, \ g(2) = 2$$

$$\therefore \ g = \{(-1, 2), (0, 0), (1, 0), (2, 2)\}$$

$$(g \text{ of } (x) = g(f(-1)), \ g(f(0)), \ g(f(1)), \ g(f(2)) \ \forall \ x \in A$$

$$= 2, 0, 0, 2$$

$$\therefore \ g \text{ of } = \{(-1, 2), (0, 0), (1, 0), (2, 2)\}$$
Hence $f = g = g \text{ o } f$

$$g(-1) = 2$$
, $g(0) = 0$, $g(1) = 0$, $g(2) = 2$

$$g = \{(-1, 2), (0, 0), (1, 0), (2, 2)\}$$

$$(g \circ f)(x) = g(f(-1), g(f(0), g(f(1), g(f(2)) \forall x \in A))$$

$$=$$
 2, 0, 0, 2

$$gof = \{(-1,2), (0,0), (1,0), (2,2)\}$$

Given curve cuts the x - axis when y = 023.

 $\frac{1}{2}$ m

when
$$y = 0$$
, $x = 7$, hence point is $(7, 0)$

 $\frac{1}{2}$ m

$$\frac{dy}{dx} = \frac{1 - y(2x - 5)}{x^2 - 5x + 6}$$

 $2\frac{1}{2}$ m

$$\frac{\mathrm{dy}}{\mathrm{dx}}\bigg]_{(7,0)} = \frac{1}{20}$$

 $\frac{1}{2}$ m

Equation of the tangent is $y-0 = \frac{1}{20}(x-7)$

1 m

$$\Rightarrow x - 20y = 7$$

Equation of the normal is
$$y-0 = -20(x-7)$$

$$\Rightarrow 20x + y = -7$$

OR

 $f(x) = \cos^2 x + \sin x, x \in [0, \pi]$

$$f'(x) = \cos x (-2 \sin x + 1)$$

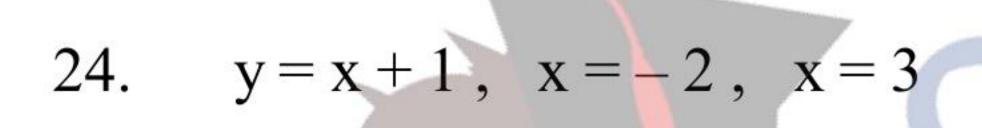
For extremum,
$$f'(x) = 0 \implies x = \frac{\pi}{2}$$
 or $x = \frac{\pi}{6}$, $\frac{5\pi}{6}$

Now
$$f(0) = 1$$
, $f\left(\frac{\pi}{6}\right) = \frac{5}{4}$, $f\left(\frac{\pi}{2}\right) = 1$, $f\left(\frac{5\pi}{6}\right) = \frac{5}{4}$, $f(\pi) = 1$

Absolute max. is
$$\frac{5}{4}$$
 at $x = \frac{\pi}{2}$ and $\frac{5\pi}{6}$

Absolute min. is 1 at x = 0, $\frac{\pi}{6}$ and π

Platfor I m



 \mathbf{X}

-1	India's lais
(-2,0) X' (-2,0)	1,0) 0
	V Y

For correct figure 1 m

1 m

Reqd area =
$$\left| \int_{-2}^{-1} (x+1) dx \right| + \int_{-1}^{3} (x+1) dx$$
 2 m

$$= \left| \left(\frac{x^2}{2} + x \right)_{-2}^{-1} \right| + \left(\frac{x^2}{2} + x \right)_{-1}^{3}$$
 2 m

$$=\frac{17}{2}$$
 sq. units

25. Let x denote no. of heads

here
$$p = \frac{1}{2}, q = \frac{1}{2}$$

1 m

$$P(x=r) = {}^{n}C_{r} \left(\frac{1}{2}\right)^{r} \left(\frac{1}{2}\right)^{n-r}$$

$$= {^{n}C_{r}} \left(\frac{1}{2}\right)^{n}$$

1 m

Now
$$P(x=1) = {}^{n}C_{1}\left(\frac{1}{2}\right)^{n}$$

$$P(x=2) = {}^{n}C_{2} \left(\frac{1}{2}\right)^{n}$$

 $1\frac{1}{2}$ m

$$P(x=3) = {}^{n}C_{3} \left(\frac{1}{2}\right)^{n}$$

According to the question

$$2. {}^{n}C_{2} \left(\frac{1}{2}\right)^{n} = \left({}^{n}C_{1} + {}^{n}C_{3}\right)\left(\frac{1}{2}\right)^{n}$$

2 m

$$\Rightarrow$$
 n = 2 or 7

½ m

n can not be 2 Hence n = 7

26. Let x kg of B₁ and y kg of B₂ is taken

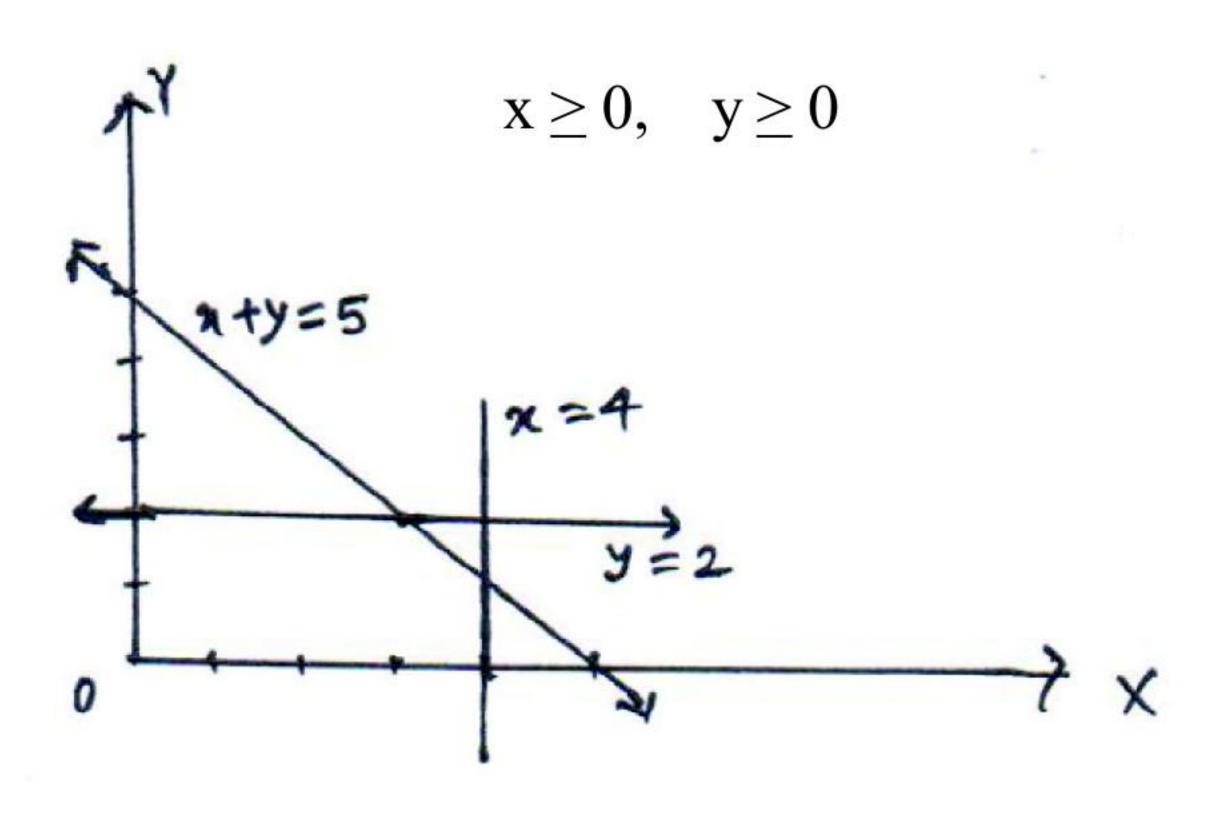
then to minimize
$$Z = 5x + 8y$$

1 m

subject to the following constraints

3 m

$$x + y = 5, \quad x \le 4, \quad y \ge 2$$



Graph

 $2 \, \mathrm{m}$