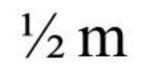
1. 
$$\vec{a} \cdot \vec{b} = 0 \implies x = -6$$

x = 2, y = 9

4.



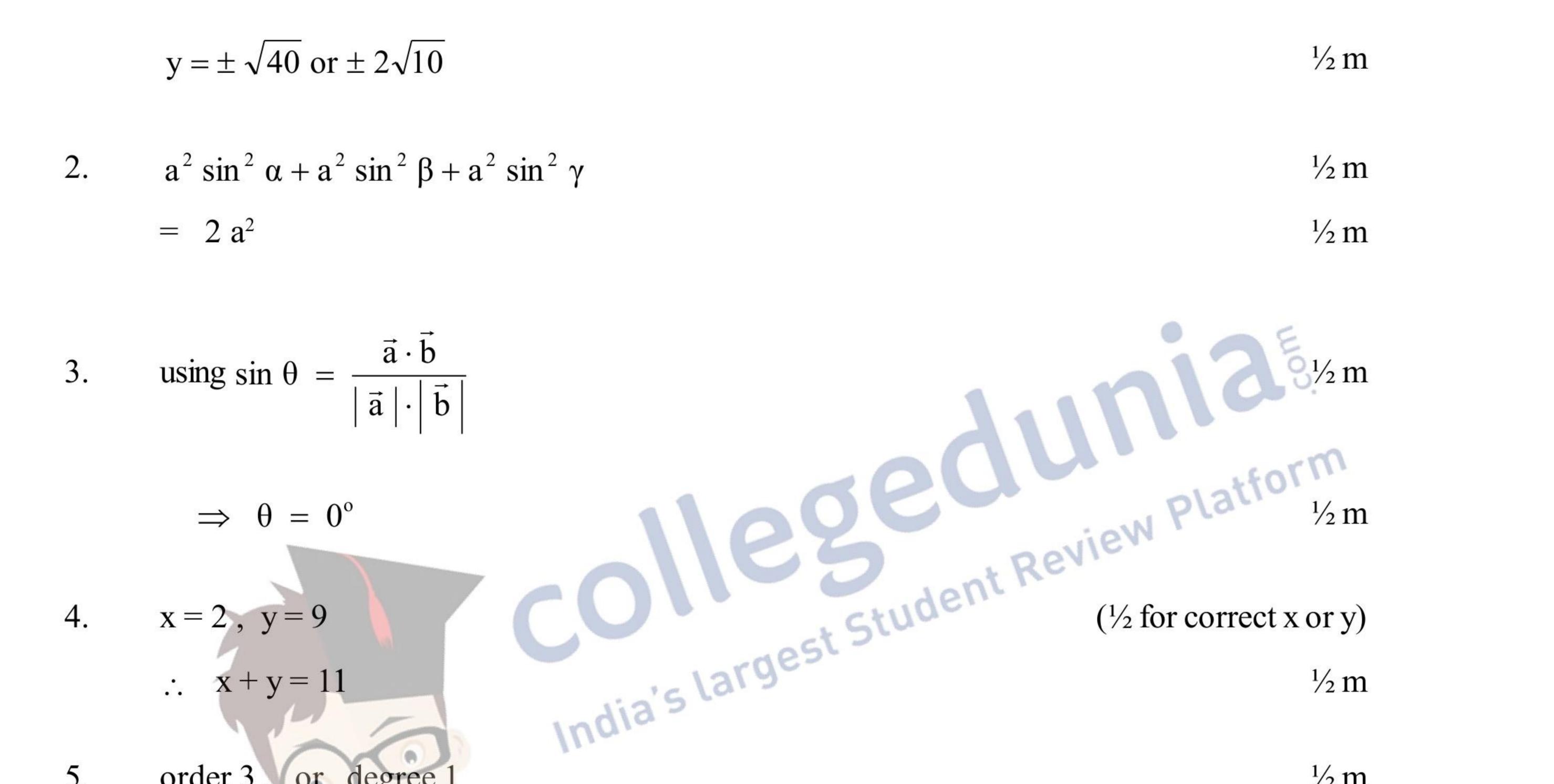
Marks

# **SECTION - A**

#### **EXPECTED ANSWERS/VALUE POINTS**

#### **QUESTION PAPER CODE 65/2/B**

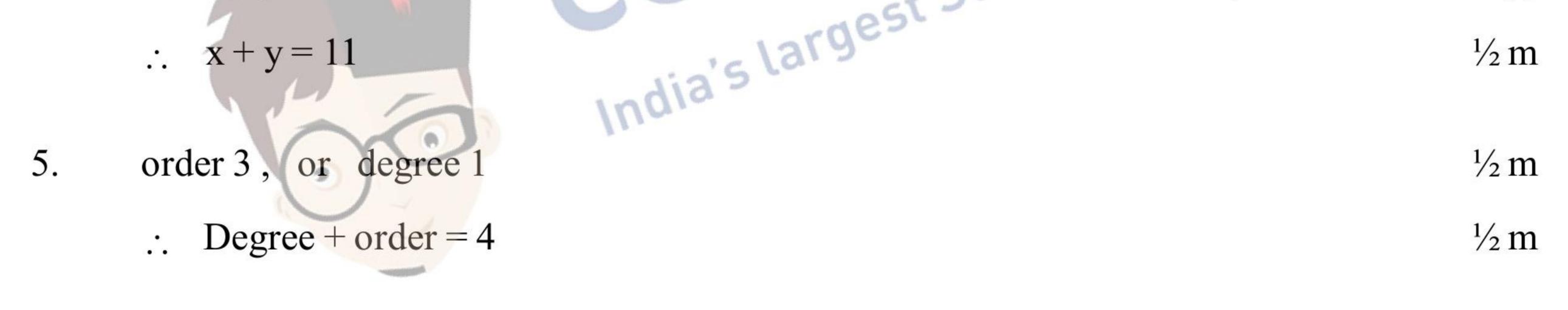
CBSE Class 12 Mathematics Answer Key 2015 (March 18, Set 2 - 65/2/B)



 $\frac{1}{2}$  m

 $\frac{1}{2}$  m

1 m



6. 
$$\frac{dy}{dx} + \frac{y}{x \log x} = \frac{2}{x}$$
 (Standard form)

 $I.F. = \log x$  $\frac{1}{2}$  m

### **SECTION - B**

14

V п.

7. 
$$\frac{y}{x} = \left[\log x - \log (a + b x)\right]$$

$$\Rightarrow \frac{x \frac{dy}{dx} - y}{x^2} = \frac{1}{x} - \frac{b}{a + b x}$$



Differentiating again,

$$x \frac{d^2 y}{dx^2} = \frac{a^2}{(a+b x)^2}$$

1 m

$$x^{3} \cdot \frac{d^{2}y}{dx^{2}} = \left(\frac{ax}{a+bx}\right)^{2} = \left(x\frac{dy}{dx} - y\right)^{2} \text{ (using (i))}$$

$$\frac{1}{2}$$
 m

8. 
$$u = \sec^{-1} \left( \frac{1}{2x^{2} - 1} \right) = 2 \cos^{-1}x \implies \frac{du}{dx} \frac{-2}{\sqrt{1 - x^{2}}}$$

$$v = \sqrt{1 - x^{2}} \implies \frac{dv}{dx} = \frac{-x}{\sqrt{1 - x^{2}}}$$

$$u = \sqrt{1 - x^{2}} \implies \frac{dv}{dx} = \frac{-x}{\sqrt{1 - x^{2}}}$$

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$$u = \sqrt{1 - x^{2}} \implies \frac{1}{\sqrt{1 - x^{2}}} = \frac{1}{\sqrt{1$$

Adding (i) and (ii) 1+1 m

$$2 I = 8 \int_{0}^{\frac{\pi}{2}} 1 \cdot dx = 4 \pi$$

 $\Rightarrow$  I = 2  $\pi$ 

put log x = t 
$$\Rightarrow$$
 x = e<sup>t</sup>  $\Rightarrow$  dx = e<sup>t</sup> dt  
=  $\int e^t \left( \log t + \frac{1}{t^2} \right) dt$ 

\*These answers are meant to be used by evaluators



1 m

15

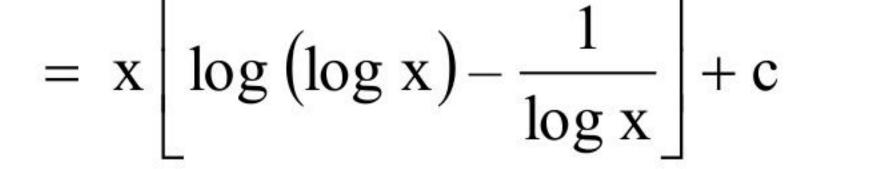
OR

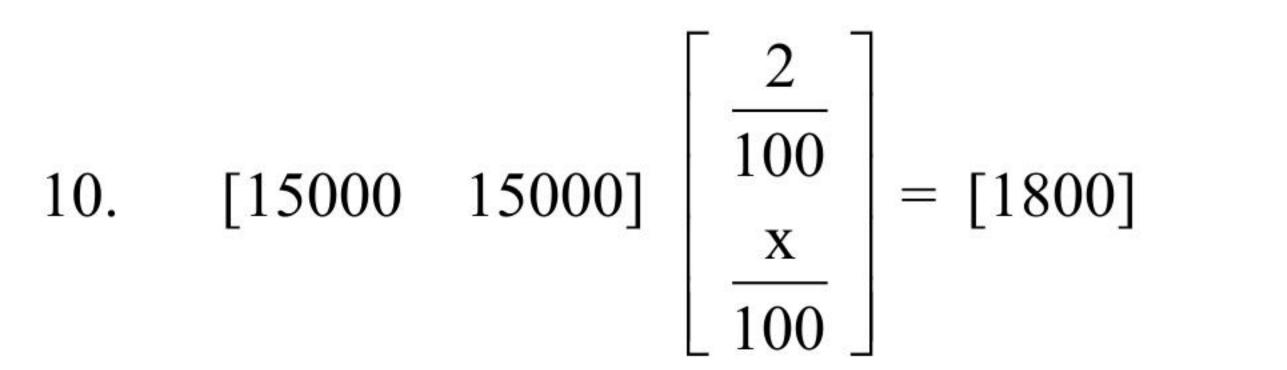
$$= \int e^{t} \left[ \left( \log t - \frac{1}{t} \right) + \left( \frac{1}{t} + \frac{1}{t^{2}} \right) \right] dt$$
$$= e^{t} \left( \log t - \frac{1}{t} \right) + c$$

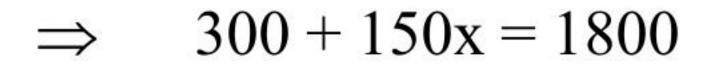
$$1\frac{1}{2}m$$

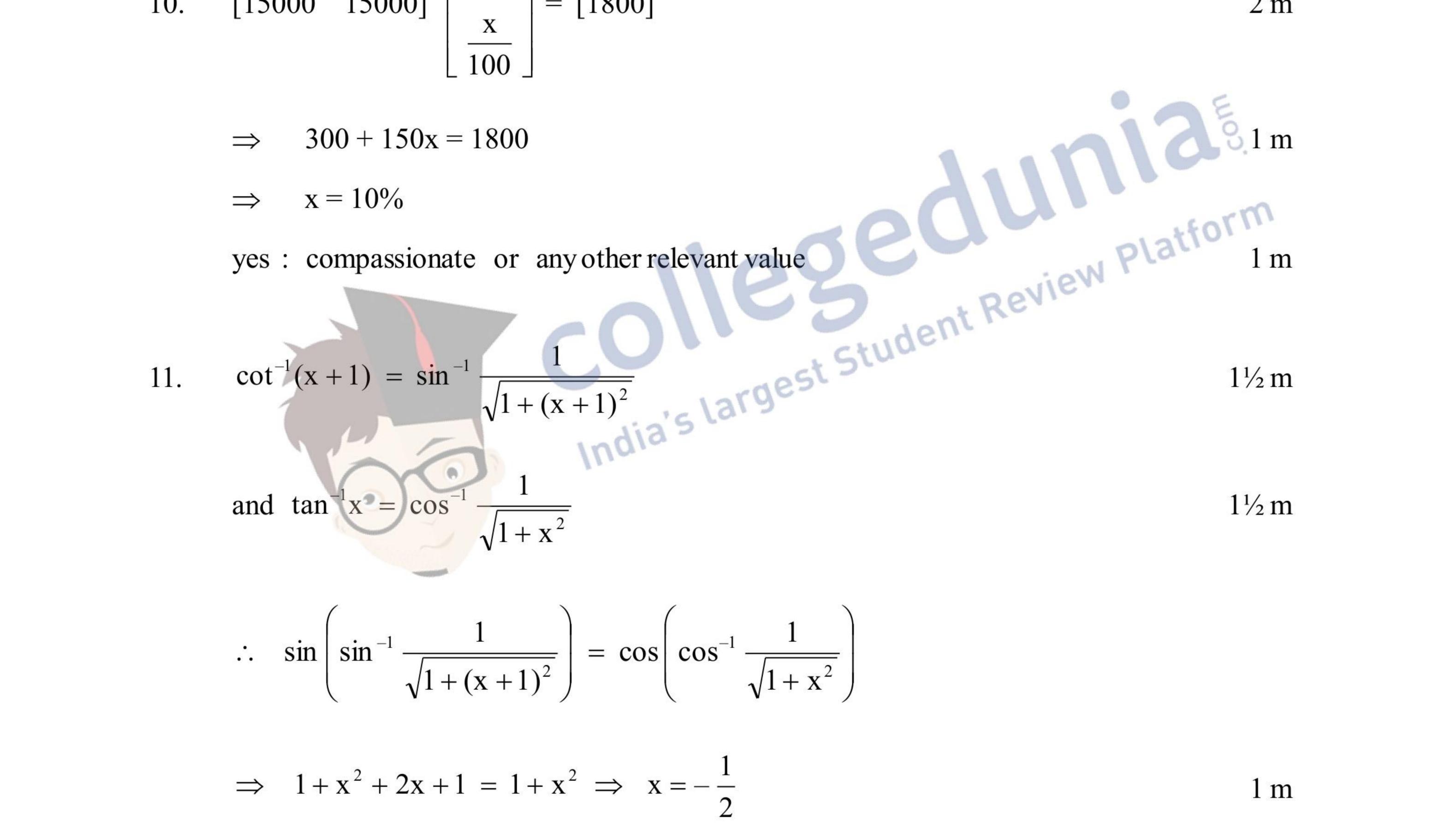
 $\frac{1}{2}$  m

2 m









1 m

16

$$2\sin^{-1}\frac{3}{5} - \tan^{-1}\frac{17}{31}$$

$$= 2 \tan^{-1} \frac{3}{4} - \tan^{-1} \frac{17}{31}$$

1 m



$$= \tan^{-1} \frac{24}{7} - \tan^{-1} \frac{17}{31}$$
$$= \tan^{-1} 1 = \frac{\pi}{4}$$

1+1 m

12.  $C_1 \rightarrow C_1 + C_2 + C_2$ ,

$$12. \quad c_1 \quad c_1 \quad c_2 \quad c_3,$$

$$(a+b+c)\begin{vmatrix} 1 & b & c \\ 1 & c & a \\ 1 & a & b \end{vmatrix} = 0 \qquad 1 m$$

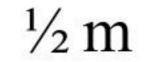
$$R_2 \rightarrow R_2 - R_1, R_3 \rightarrow R_3 - R_1$$

$$\Rightarrow \begin{vmatrix} 1 & b & c \\ 0 & c-b & a-c \\ 0 & a-b & b-c \end{vmatrix} = 0 \quad (\because a+b+c\neq 0)$$

$$\Rightarrow -a^2 - b^2 - c^2 + ab + bc + ca = 0 \qquad 1/2 m$$

17

$$\Rightarrow -\frac{1}{2} [(a-b)^2 + (b-c)^2 + (c-a)^2] = 0$$
  
$$\Rightarrow a = b = c$$



1 m

13.  $\begin{pmatrix} 1 & -1 & 0 \\ 2 & 5 & 3 \\ 0 & 2 & 1 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \cdot \mathbf{A}$ 

$$\mathbf{R}_2 \rightarrow \mathbf{R}_2 - 2 \, \mathbf{R}_1 \, ,$$

 $\begin{pmatrix} 1 & -1 & 0 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \end{pmatrix}$ 

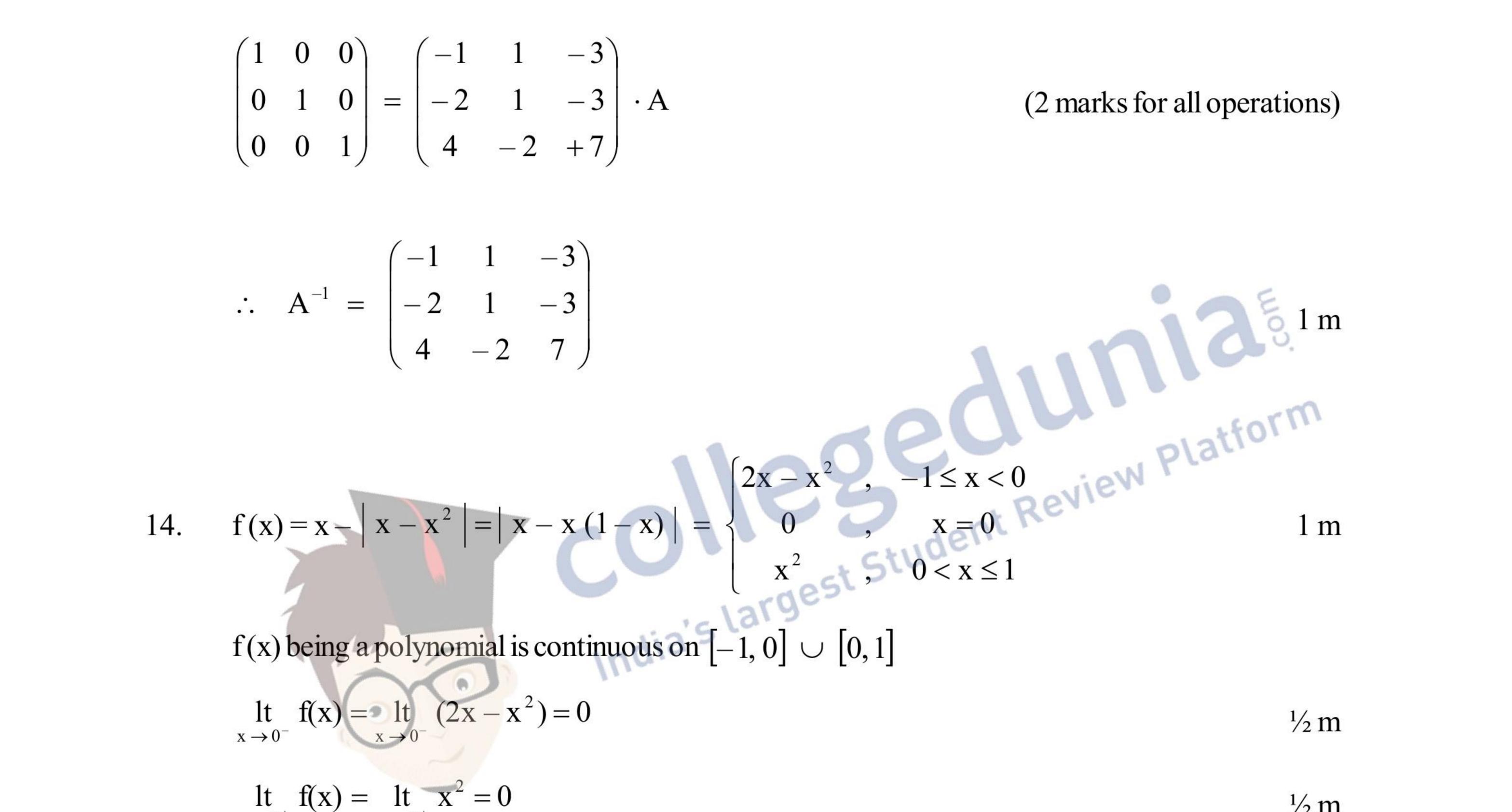
$$\begin{vmatrix} 0 & 7 & 3 \\ 0 & 2 & 1 \end{vmatrix} = \begin{vmatrix} -2 & 1 & 0 \\ 0 & 0 & 1 \end{vmatrix} \cdot \mathbf{A}$$

 $R_2 \rightarrow R_2 - 3R_3$ 



# $R_1 \rightarrow R_1 + R_2, R_3 \rightarrow R_3 - 2R_2$

$$\begin{pmatrix} 1 & -1 & 0 \\ 0 & 1 & 0 \\ 0 & 2 & 1 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ -2 & 1 & -3 \\ 0 & 0 & 1 \end{pmatrix} \cdot \mathbf{A}$$



18

$$\lim_{x \to 0^{-}} f(x) = \lim_{x \to 0^{-}} (2x - x^{2}) = 0$$

$$\lim_{x \to 0^+} f(x) = \lim_{x \to 0^+} x^2 = 0$$

## Also, f(0) = 0

: 
$$\lim_{x \to 0^{-}} f(x) = f(0) = \lim_{x \to 0^{+}} f(x)$$

$$\Rightarrow$$
 There is no point of discontinuity on [-1, 1]

15. 
$$\vec{a}_1 = -\hat{i}, \ \vec{b}_1 = \hat{i} + \frac{1}{2}\hat{j} - \frac{1}{12}\hat{k}$$

$$\frac{1}{2}$$
 m

 $\frac{1}{2}$  m

1 m

1 m

1 m

 $\frac{1}{2}$  m

 $\frac{1}{2}$  m

$$\vec{a}_2 = -2\hat{j} + \hat{k}, \ \vec{b}_2 = \hat{i} + \hat{j} + \frac{1}{6}\hat{k}$$

$$\vec{a}_2 - \vec{a}_1 = \hat{i} - 2\hat{j} + \hat{k}$$
  
 $\vec{b}_1 \times \vec{b}_2 = \frac{1}{6}\hat{i} - \frac{1}{4}\hat{j} + \frac{1}{2}\hat{k}$ 

\*These answers are meant to be used by evaluators

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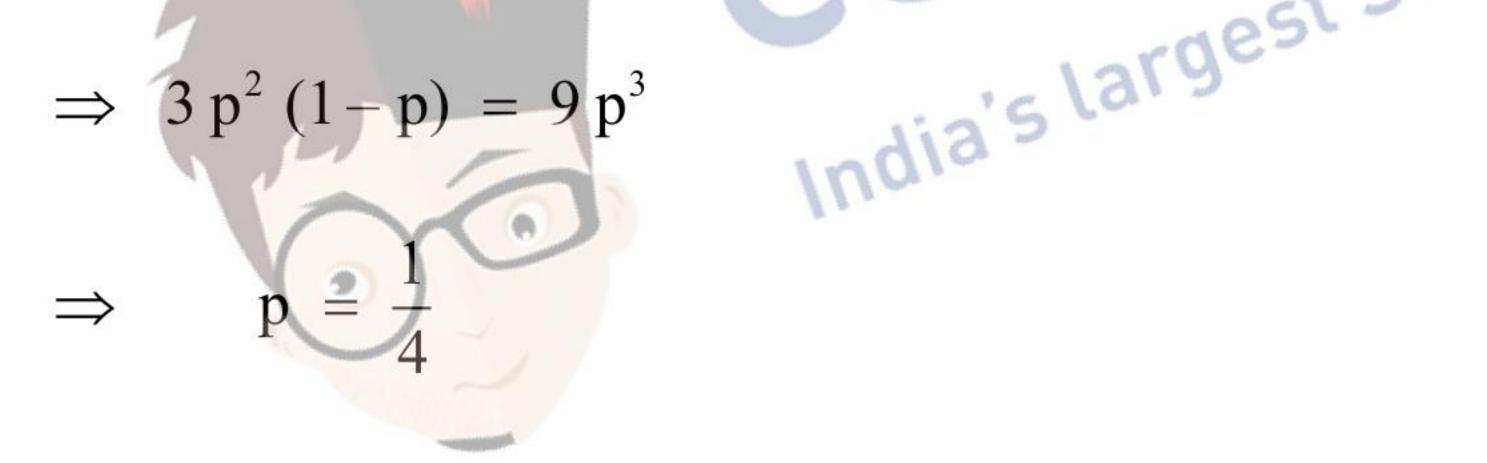
$$\begin{vmatrix} \vec{b}_1 \times \vec{b}_2 \end{vmatrix} = \frac{7}{12}$$
  
S.D. = 
$$\begin{vmatrix} \frac{(\vec{a}_2 - \vec{a}_1) \cdot (\vec{b}_1 \times \vec{b}_2)}{|\vec{b}_1 \times \vec{b}_2|} \end{vmatrix} = 2$$

1 m

1 m

# Foot of perpendicular are (0, b, c) & (a, 0, c)Equ. of required plane

 $\begin{vmatrix} x & y & z \\ 0 & b & c \\ a & 0 & c \end{vmatrix} = 0$ 1 m Student Review Platform bcx + acy - abz = 0 $\Rightarrow$  $p(x=2) = 9 \cdot P(x=3)$ 16.  $\Rightarrow {}^{3}C_{2} p^{2} q = 9 \cdot {}^{3}C_{3} p^{3} \cdot q^{0}$ 



1 m

OR

Let  $H_1$  be the event that red ball is drawn H, be the event that black ball is drawn E be the event that both balls are red

$$P(H_1) = \frac{3}{8}, P(H_2) = \frac{5}{8}$$

1 m

$$P(E/H_1) = \frac{5_{C_2}}{10_{C_2}} = \frac{2}{9}, P(E/H_2) = \frac{3_{C_2}}{10_{C_2}} = \frac{1}{15}$$

 $P(E) = P(H_1) P(E/H_1) + P(H_2) \cdot P(E/H_2)$ 

1 m

1 m

19



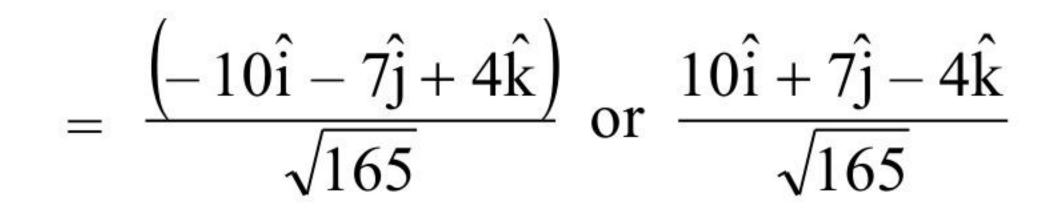
$$= \frac{3}{8} \cdot \frac{2}{9} + \frac{5}{8} \cdot \frac{1}{15} = \frac{1}{8}$$
  
17. I =  $\int \frac{x \cos x}{\cos x + x \sin x} dx$   
put  $\cos x + x \sin x = t$ 

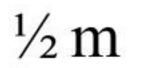
1 m

put cos x + x sin x = t  $\Rightarrow x \cos x \, dx = dt$   $= \int \frac{dt}{t}$   $= \log |\cos x + x \sin x| + c$  1 m  $= \log |\cos x + x \sin x| + c$  1 m  $18. \int \frac{x^4 \, dx}{(x-1)(x^2+1)} = \int \left[ (x+1) + \frac{1}{(x-1)(x^2+1)} \right] dx$  (using partial fractions)  $= \int (x+1) \, dx + \frac{1}{2} \int \frac{dx}{(x-1)} - \frac{1}{2} \int \frac{x+1}{x^2+1} \, dx$   $1\frac{1}{2} m$ 

19. 
$$\overrightarrow{AB} = -2\hat{i} - 5\hat{k}$$
$$\overrightarrow{AC} = \hat{i} - 2\hat{j} - \hat{k}$$
$$1m$$
$$\overrightarrow{AB} \times \overrightarrow{AC} = -10\hat{i} - 7\hat{j} + 4\hat{k}$$
$$1m$$
$$\hat{n} = \frac{\overrightarrow{AB} \times \overrightarrow{AC}}{|\overrightarrow{AB} \times \overrightarrow{AC}|}$$
$$1m$$

20







#### **SECTION - C**

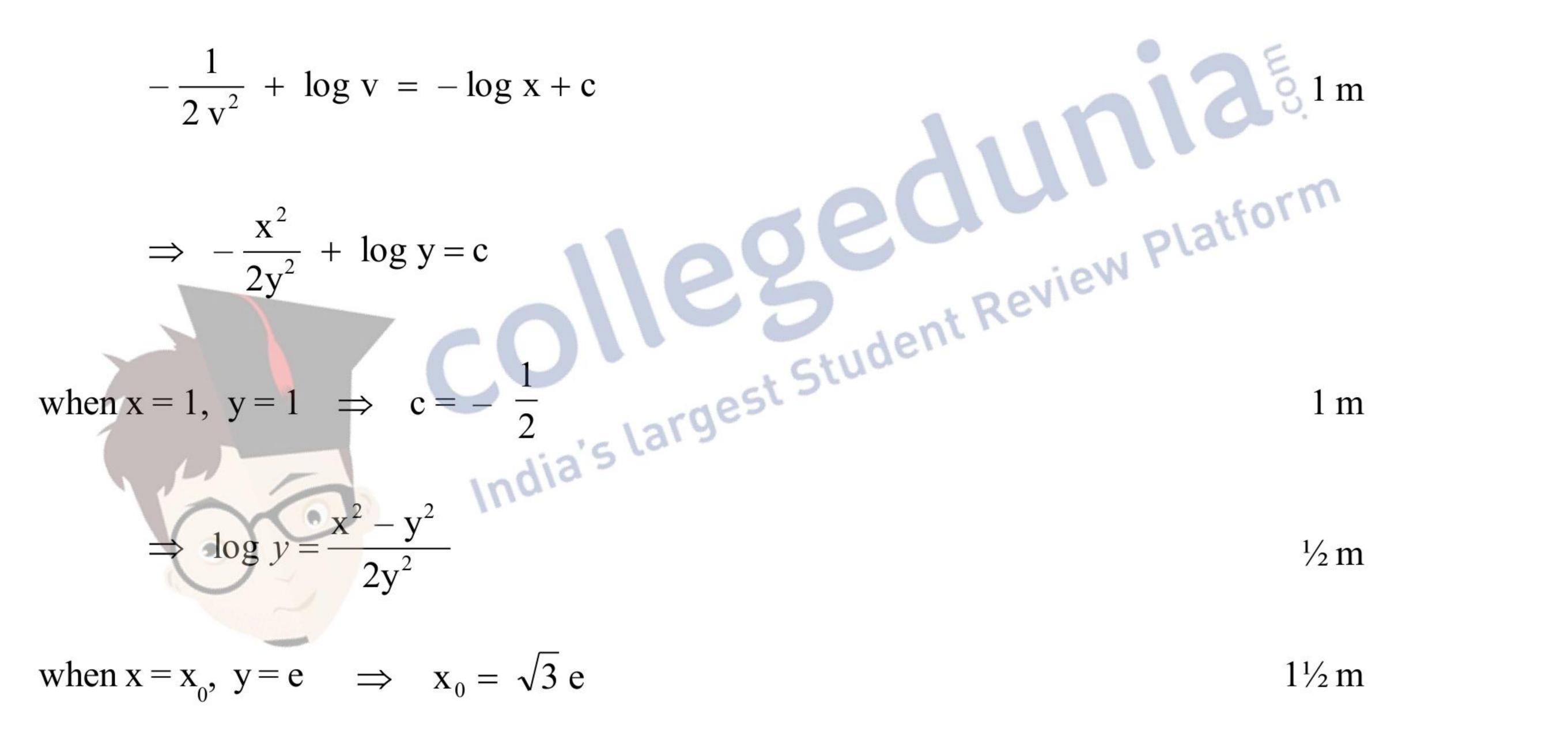
20. 
$$\frac{dy}{dx} = \frac{xy}{x^2 + y^2}$$

dv

put 
$$y = v x \implies \frac{dy}{dx} = v + x \frac{dv}{dx}$$

$$\Rightarrow \frac{1+v^2}{v^3} = -\frac{dx}{x}$$

Integrating both sides



#### OR

I F = 
$$e^{\int \tan x \, dx}$$
 =  $e^{\log \sec x}$  = sec x  
 $\therefore \quad \frac{d}{dx} (y \cdot \sec x) = 3x^2 \sec x + x^3 \sec x \tan x$  1 m

$$\Rightarrow y \sec x = \int 3x^2 \sec x \cdot dx + x^3 \sec x - \int 3x^2 \cdot \sec x \, dx + c \qquad 2m$$
$$\Rightarrow y = x^3 + c \cos x$$

21

when 
$$x = \frac{\pi}{3}$$
,  $y = 0$ ; we get  $c = \frac{-2\pi^3}{27}$ 

\*These answers are meant to be used by evaluators



1 m

1 m

1 m

$$\therefore \quad y = x^3 - \frac{2\pi^3}{27} \cos x$$

21. Equation of line is 
$$\frac{x-3}{2} = \frac{y-4}{-3} = \frac{z-1}{5}$$

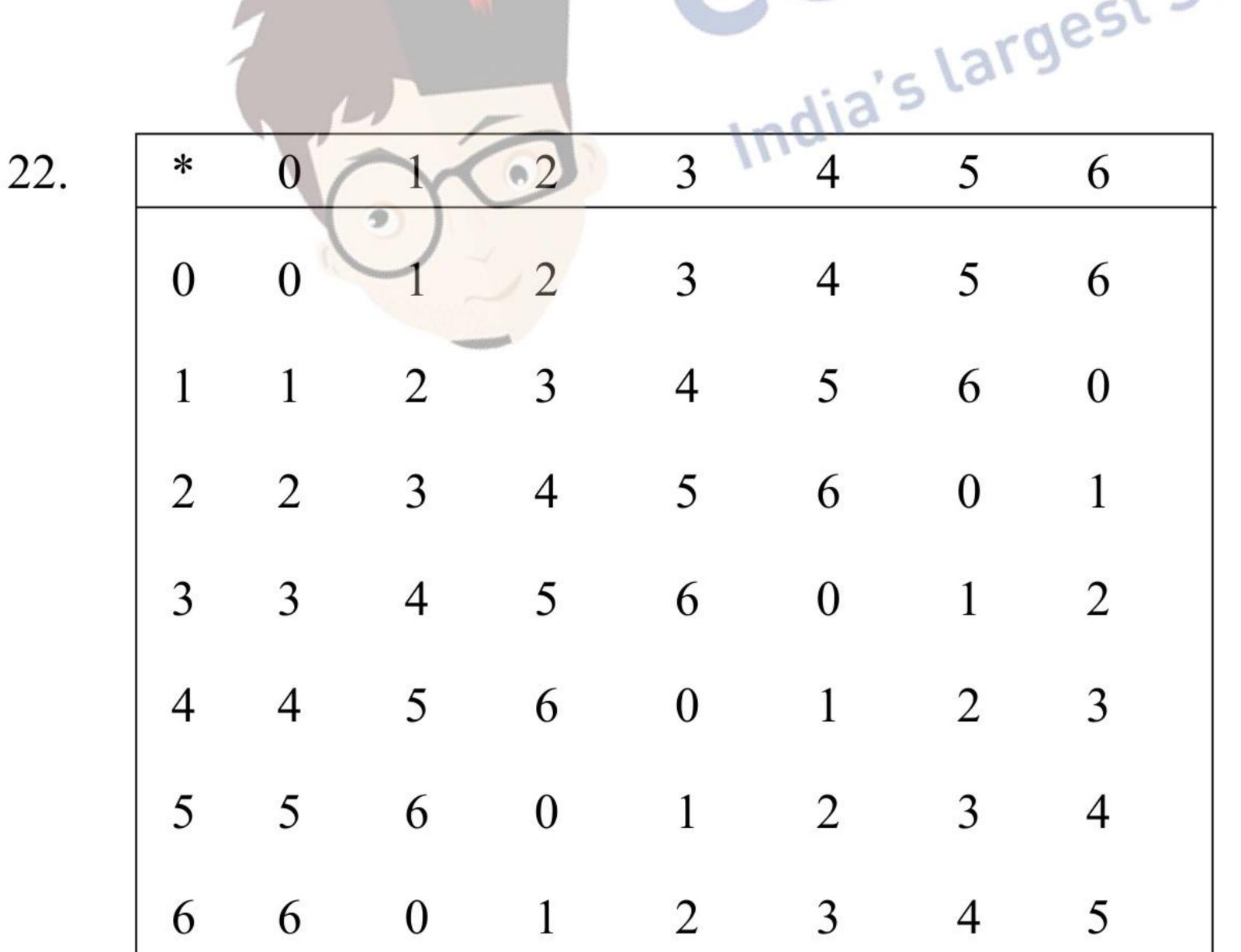
1 m

# Equation of plane is

$$\begin{vmatrix} x - 2 & y - 1 & z - 2 \\ 1 & 0 & -2 \\ 2 & -3 & -1 \end{vmatrix} = 0$$

$$2x + y + z - 7 = 0$$
implies the second second

$$\Rightarrow 2x + y + z - 7 = 0 \dots (1) \qquad 1 \text{ m}$$
  
general point on given line  $(2\lambda + 3, -3\lambda + 4, 5\lambda + 1)$  lies on (i)  
$$\therefore 2(2\lambda + 3) + (-3\lambda + 4) + (5\lambda + 1) - 7 = 0 \Rightarrow \lambda = -\frac{2}{3}$$
  
$$\therefore \text{ Point of intersection } \left(\frac{5}{3}, 6, -\frac{7}{3}\right) \qquad 1 \text{ m}$$



4 m

1 m

# $\forall a \in \{0, 1, 2, 3, 4, 5, 6\}$

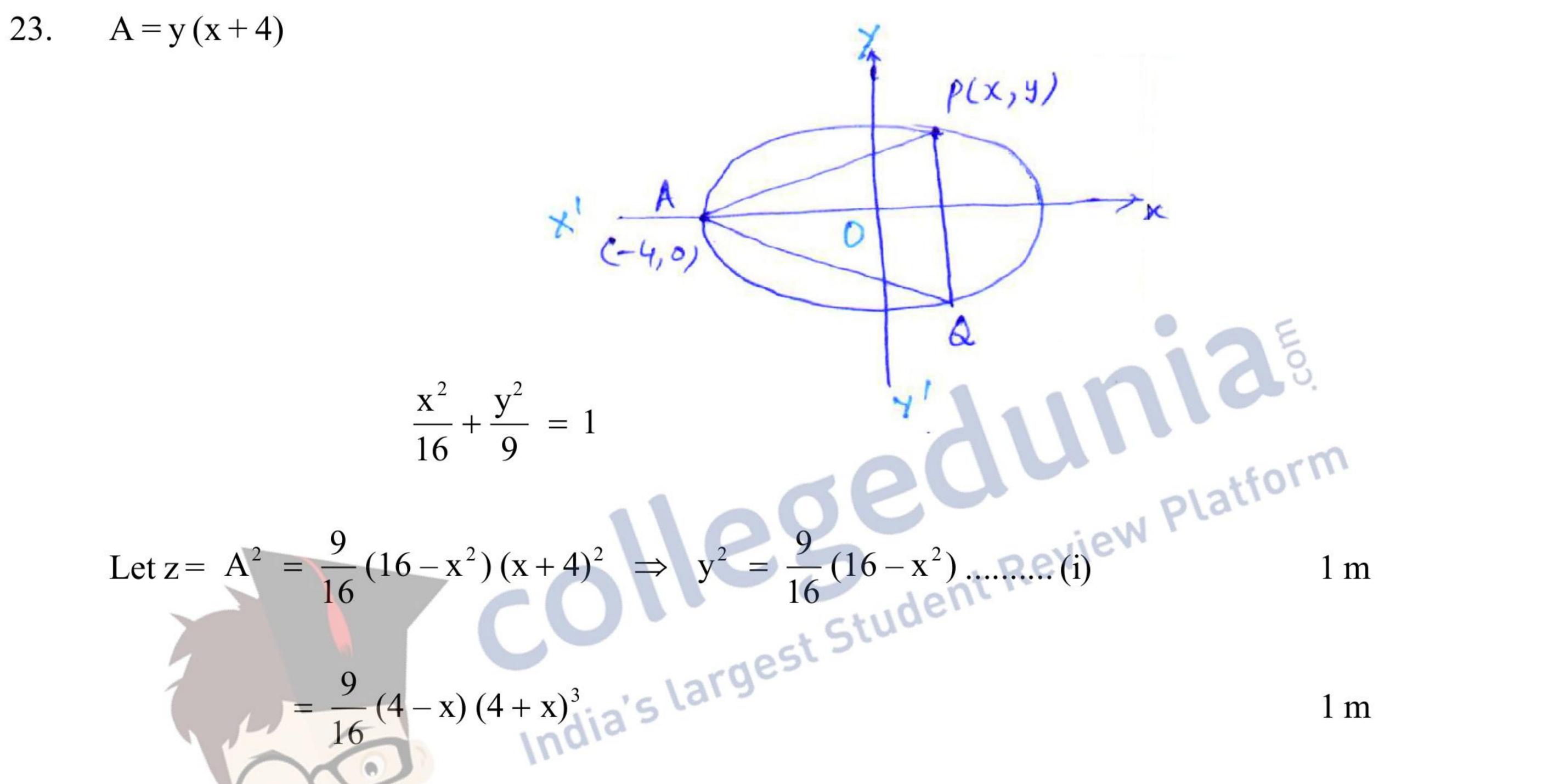
 $a * 0 = a = 0 * a \implies 0$  is identity

\*These answers are meant to be used by evaluators



22

$$\forall a \in \{1, 2, 3, 4, 5, 6\}$$
  
 $a * b = 0 = b * a$   
 $\Rightarrow a * (7-a) = 0 = (7-a) * a$   
 $\Rightarrow (7-a)$  is inverse of a



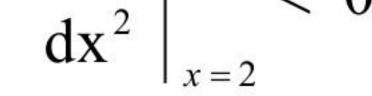
$$\frac{dz}{dx} = \frac{9}{16} (4 - x) (4 + x)^{3}$$
 is largest  
$$\frac{dz}{dx} = \frac{9}{16} (4 + x)^{2} (8 - 4x)$$

$$\frac{dz}{dx} = 0 \implies x = 2$$

1 m

$$\frac{d^2 z}{dx^2} = -\frac{9}{4} (4+x)^2 + \frac{9}{8} (4+x) (8-4x)$$

$$\frac{\mathrm{d}^2 z}{<0}$$



#### Maximum value of $A = 9\sqrt{3}$ sq. units · .

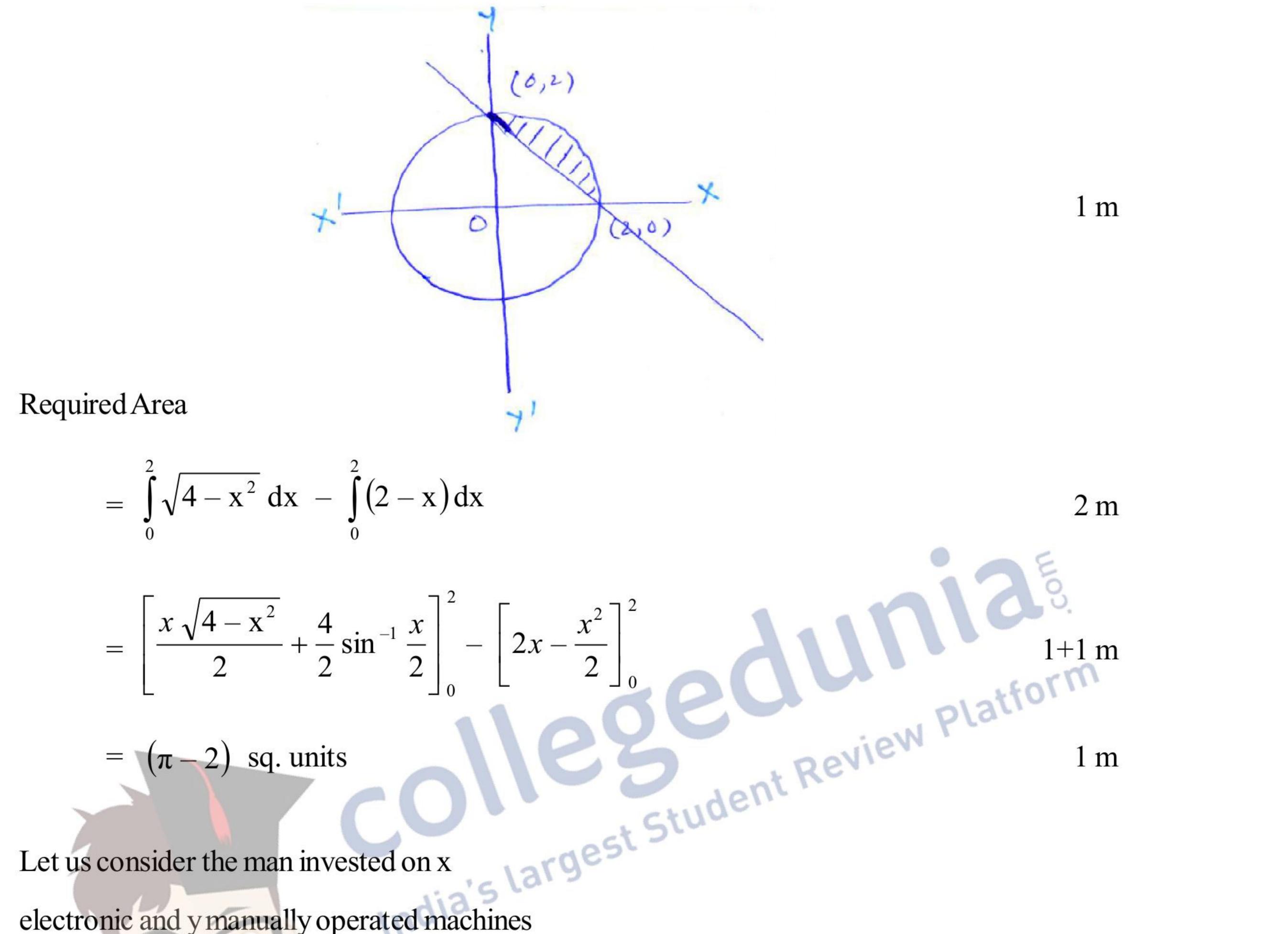
23

\*These answers are meant to be used by evaluators



1 m



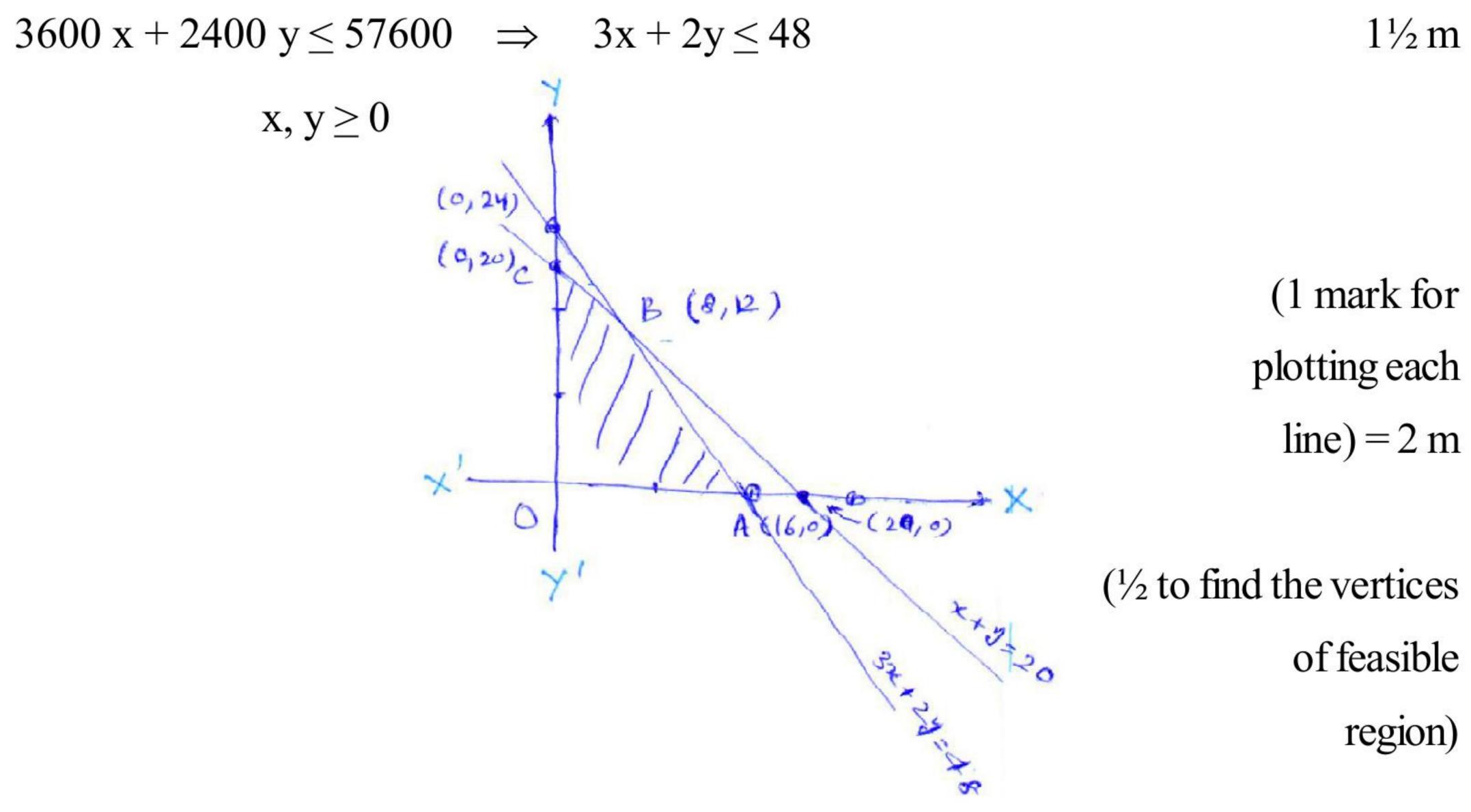


Let us consider the man invested on x 25.

electronic and y manually operated machines

subject to

 $x + y \leq 20$ 



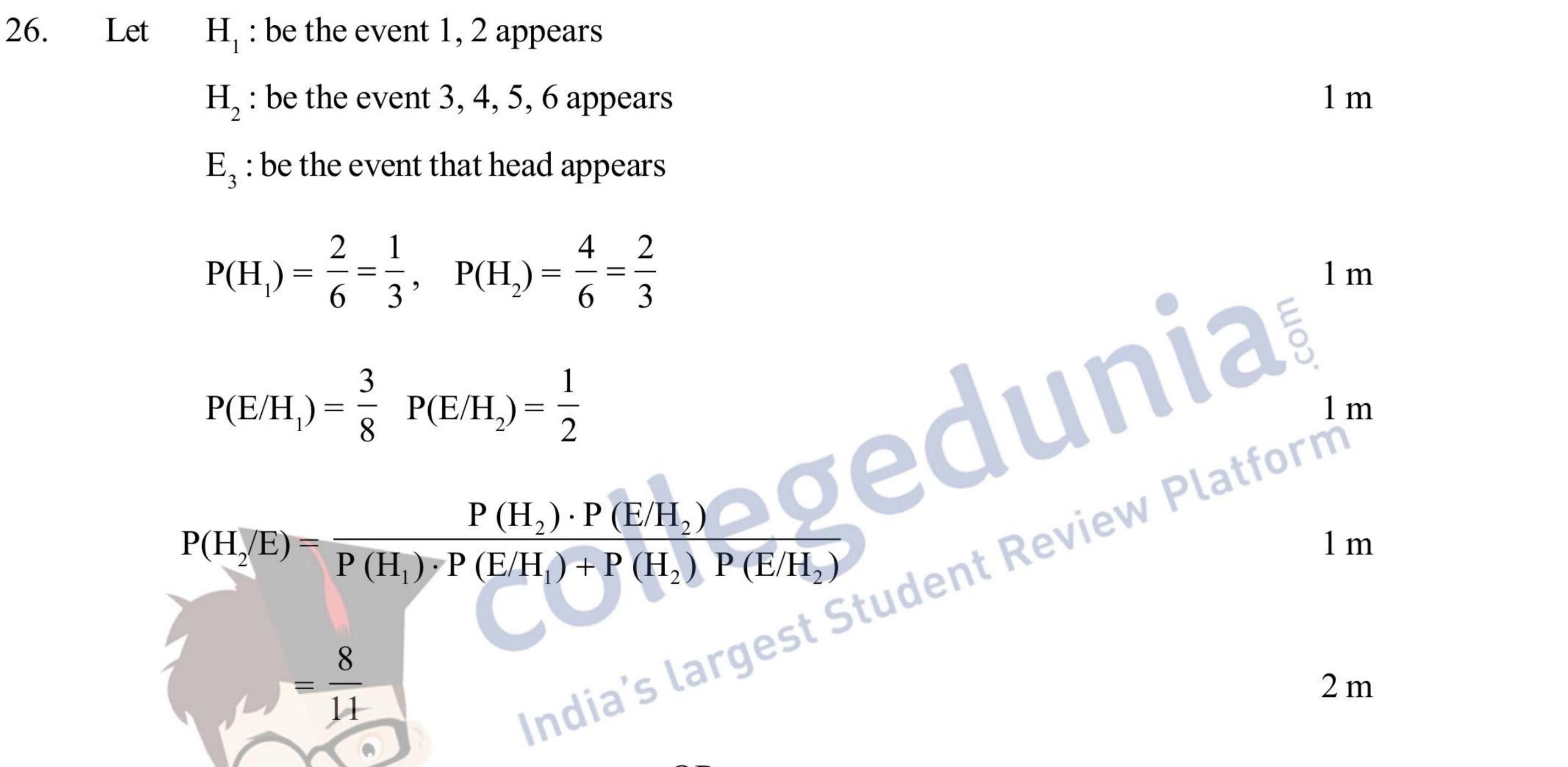
24

1 m

region)



P 
$$\Big|_{A(16,0)} = 3520 \text{ Rs.}$$
  
P  $\Big|_{B(8,12)} = 3920 \text{ Rs.}$   
P  $\Big|_{C(0,20)} = 3600 \text{ Rs.}$   
Maximum profit is Rs. 3920 at x = 8, y = 12





1 m

 $H_1$ : be the event that 4 occurs Let

H<sub>2</sub>: be the event that 4 does not occurs

E : be the event that man reports 4 occurs

on a throw of dice

$$P(H_1) = \frac{1}{6}, \quad P(H_2) = \frac{5}{6}$$
$$P(E/H_1) = \frac{3}{5} \quad P(E/H_2) = 1 - \frac{3}{5} = \frac{2}{5}$$

1 m

1 m

 $(2^{-11})^{-11} 5^{-1} (2^{-11})^{-1} 5 5$  $P(H_{1}/E) = \frac{P(H_{1}) \cdot P(E/H_{1})}{P(H_{1}) \cdot P(E/H_{1}) + P(H_{2}) \cdot P(E/H_{2})}$ 1 m  $=\frac{3}{13}$ 2 m

25



