

GGSIPO mathematics 2012

- If the lines $x-y-1=0$, $4x+3y=k$ and $2x-3y+1=0$ are concurrent, then k is
 - 1
 - 1
 - 25
 - 5
- the number of common tangents to the circles $x^2+y^2=4$ and $x^2+y^2-8x+12=0$ is
 - 1
 - 2
 - 3
 - 4
- The centroid of a triangle formed by the points $0,0$, $(\cos \theta, \sin \theta)$ and $(\sin \theta, -\cos \theta)$ lie on the line $y=2x$; then θ is
 - $\tan^{-1} 2$
 - $\tan^{-1} \frac{1}{3}$
 - $\tan^{-1} \frac{1}{2}$
 - $\tan^{-1} -3$
- The orthocentre of the triangle formed by $8,0$ and $4,6$ with the origin, is
 - $(4, \frac{8}{3})$
 - $(3, -4)$
 - $(4,3)$
 - $(3,4)$
- If the angle between two lines represented by $2x^2+5xy+3y^2+7y+4=0$ is $\tan^{-1} m$, then m is equal to
 - $\frac{1}{5}$
 - 1
 - $\frac{7}{5}$
 - 7
- If $xy-4x+3y-\lambda=0$ represents the asymptotes of $xy-4x+3y=0$, then λ is
 - 3
 - 6
 - 8
 - 12
- The equation of the chord of the parabola $y^2=8x$ which is bisected at the point $(2, -3)$, is
 - $4x+3y+1=0$
 - $3x+4y-1=0$
 - $4x-3y-1=0$
 - $3x-4y+1=0$
- If $x+y+1=0$ touches the parabola $y^2=\lambda x$, then λ is equal to

a) 2 b 4 (c 6 d 8

9. The equations $x = \frac{e^t + e^{-t}}{2}$, $y = \frac{e^t - e^{-t}}{2}$ where t is real number, represents

a an ellipse b a parabola

c a hyperbola d a circle

10. if e_1 and e_2 are the eccentricities of two conics with $e_1^2 + e_2^2 = 3$, then the conics are

a ellipses b parabolas

c circles d hyperbolas

11. The sum of the distances of any point on the ellipse $3x^2 + 4y^2 = 24$ from its foci, is

a $8\sqrt{2}$ b 8

c $16\sqrt{2}$ d $4\sqrt{2}$

12. In $\triangle ABC$, if a tends to 2c and b tends to 3c, then $\cos B$ tends to

a -1 b $\frac{1}{2}$ c $\frac{1}{3}$ d $\frac{2}{3}$

13. if $\sin \pi \cos \theta = \cos \pi \sin \theta$, then which of the following is correct

a $\cos \theta = \frac{3}{2\sqrt{2}}$

b $\cos \left(\theta - \frac{\pi}{2} \right) = \frac{1}{2\sqrt{2}}$

c $\cos \left(\theta - \frac{\pi}{4} \right) = \frac{1}{2\sqrt{2}}$

d $\cos \left(\theta + \frac{\pi}{4} \right) = -\frac{1}{2\sqrt{2}}$

14. The value of $\sin 12^\circ \sin 48^\circ \sin 54^\circ$ is equal to

a $\frac{2}{3}$ b $\frac{1}{2}$

(c) $\frac{1}{8}$ (d) $\frac{1}{3}$

15. If $3\sin^{-1} \left(\frac{2x}{1+x^2} \right) - 4\cos^{-1} \left(\frac{1-x^2}{1+x^2} \right) + 2\tan^{-1} \left(\frac{2x}{1-x^2} \right) = \frac{\pi}{3}$, then x is equal to

a $\frac{1}{\sqrt{3}}$ b $-\frac{1}{\sqrt{3}}$

$$c \quad \sqrt{3} \quad (c) \quad -\frac{\sqrt{3}}{2}$$

16. The shadow of a pole is $\sqrt{3}$ times longer. The angle of elevation is equal to

- a 40° b $\frac{45^\circ}{2}$
 c 60° d 30°

17. The point of contact of the line $x-y+2=0$ with the parabola $y^2-8x=0$ is

- a 2,4 b -2,4
 c 2, -4 d 2,2

18. If the sides of a triangle are x^2+x+1 , x^2-1 and $2x+1$, then the greatest angle is

- a 90° b 135° c 115° d 120°

19. The value of $\cos 1^\circ \cdot \cos 2^\circ \cdot \cos 3^\circ \dots \cos 179^\circ$ is equal to

- a $\frac{1}{\sqrt{2}}$ b 0
 c 1 d -1

20. If $\cot \alpha + \beta = 0$, then $\sin \alpha + 2\beta$ is equal to

- a $\sin \alpha$ b $\cos \alpha$
 c $\sin \beta$ d $\cos 2\beta$

21. The value of $4 \sin A \cos^3 A - 4 \cos A \sin^3 A$ is equal to

- a $\cos 2A$ b $\sin 3A$
 c $\sin 2A$ d $\sin 4A$

22. If the solutions for θ of $\cos p\theta + \cos q\theta = 0$, $0 < q < p$ are in AP, then the numerically smallest common difference of AP is

- a $\frac{\pi}{p+q}$ b $\frac{2\pi}{p+q}$
 c $\frac{\pi}{2(p+q)}$ d $\frac{1}{p+q}$

23. The value of k for which $\cos x + \sin x^2 + k \sin x \cos x - 1 = 0$ is that identity, is

- a -1 b -2 c 0 d 1

24. If $4 \cos^{-1} x + \sin^{-1} x = \pi$, then the value of x is

- a $\frac{1}{2}$ b $\frac{1}{\sqrt{2}}$
c $\frac{\sqrt{3}}{2}$ d $\frac{2}{\sqrt{3}}$

25. a problem in mathematics is given to 3 students whose chances of solving individually are $\frac{1}{2}$, $\frac{1}{3}$ and $\frac{1}{4}$. The probability that the problem will be solved at least by one, is

- a $\frac{1}{4}$ b $\frac{1}{24}$
c $\frac{23}{24}$ d $\frac{3}{4}$

26. In a non-leap year the probability of getting 53 Sundays or 53 Tuesdays or 53 Thursdays is

- a $\frac{1}{7}$ b $\frac{2}{7}$
c $\frac{3}{7}$ d $\frac{4}{7}$

27. The probability for a randomly chosen month to have its 10th day as Sunday, is

- a $\frac{1}{84}$ b $\frac{10}{12}$
c $\frac{10}{84}$ d $\frac{1}{7}$

28. If the mean of numbers $27+x, 31+x, 89+x, 107+x, 156+x$ is 82, then the mean of $130+x, 126+x, 68+x, 50+x, 1+x$ is

- a 79 b 157
c 82 d 75

29. if μ is the mean distribution of $\{Y_i, f_i\}$, then $\sum f_i(Y_i - \mu)$ is equal to

- a MD b SD
c 0 d relative frequency

30. Two cards are drawn successively with replacement from a well-shuffled pack of 52 cards. The probability of drawing two aces is

- a $\frac{1}{13}$ b $\frac{1}{13} \times \frac{1}{17}$
c $\frac{1}{52} \times \frac{1}{51}$ d $\frac{1}{13} \times \frac{1}{13}$

31. If $\sec\left(\frac{x+y}{x-y}\right) = a$, then $\frac{dy}{dx}$ is

a $\frac{x}{y}$ b $\frac{y}{x}$

(c) y d x

32. If $x^y = e^{x-y}$, then $\frac{dy}{dx}$ is equal to

a $\frac{\log x}{1+\log x}$ (b) $\frac{\log x}{1-\log x}$

c $\frac{\log x}{1+\log x)^2}$ (d) $\frac{y \log x}{x(1+\log x)}$

33. For $y = \cos m \sin^{-1} x$ which of the following is true?

a $1 - x^2 y_2 + xy_1 - m^2 y = 0$

b $1 - x^2 y_2 - xy_1 + m^2 y = 0$

c $1+x^2 y_2 + xy_1 - m^2 y = 0$

(d) $(1-x^2) y_2 + xy_1 + m^2 y = 0$

34. If $f(x) = \begin{cases} x+1 & x \leq 1 \\ 3-ax^2 & x > 1 \end{cases}$ is continuous at $x=1$, then the value of a is

a -1 b 2

(c) -3 (d) 1

35. $\lim_{x \rightarrow \frac{\pi}{2}} \frac{a^{\cot x} - a^{\cos x}}{\cot x - \cos x}$ is equal to

a $\log a$ b $\log 2$

c a^a (d) $\log a$

36. If $f'(0) = k$, then $\lim_{x \rightarrow 0} \frac{2f(x) - 3f(2x) + f(4x)}{x^2}$ is equal to

a k b $2k$ c $3k$ d $4k$

37. If g is the inverse function of f and $f'(x) = \frac{1}{1+x^n}$, then $g'(x)$ is equal to

a $1+gx^n$ b $1-gx^n$

c $1+gx^n$ d $1-gx^n$

38. The curves $4x^2+9y^2 = 72$ and $x^2-y^2 = 5$ at $(3,2)$

a touch each other b cut orthogonally

c interest at 45° d interest at 60°

39. The velocity v m/s of a particle is proportional to the cube of the time. If the velocity after 2 s is 4m/s, then v is equal to

a t^3 b $\frac{t^3}{8}$

c $\frac{t^3}{3}$ d $\frac{t^3}{4}$

40. The minimum value of $x \log x$ is equal to

a e b $\frac{1}{e}$

c $-\frac{1}{e}$ d $\frac{2}{e}$

41. A particle moves along the x-axis so that its position is given $x = 2t^3 - 3t^2$ at a time t second. What is the time interval during which particle will be on the negative half of the axis?

a $0 < t < \frac{2}{3}$ b $0 < t < 1$

c $0 < t < \frac{3}{2}$ d $\frac{1}{2} < t < 1$

42. A stone thrown vertically upwards satisfies the equations $s = 80t - 16t^2$. The time required to reach the maximum height is

a 2 s b 4 s

c 3 s d 2.5 s

43. If $f(x+y) = f(x) \cdot f(y)$, $f(3) = 3$, $f'(0) = 11$. Then $f'(3)$ is equal to

a $11 \cdot e^{33}$ b 33

c 11 d $\log 33$

44. If $y = x \tan y$, then $\frac{dy}{dx}$ is equal to

a $\frac{\tan y}{x-x^2-y^2}$ b $\frac{y}{x-x^2-y^2}$

c $\frac{\tan y}{y-x}$ d $\frac{\tan x}{x-y^2}$

45. The product of the lengths of subtangent and subnormal at any point x, y of a curve is

a x^2 b y^2

c a constant d x

46. The equation of tangent to the curve

$$\left(\frac{x}{a}\right)^n + \left(\frac{y}{b}\right)^n = 2 \text{ at } (a, b) \text{ is}$$

a $\frac{x}{a} + \frac{y}{b} = 2$ b $\frac{x}{a} + \frac{y}{b} = \frac{1}{2}$

c $\frac{x}{b} - \frac{y}{a} = 2$ d $ax + by = 2$

47. If $\int_0^{\infty} \frac{x^2 dx}{x^2+a^2)(x^2+b^2)(x^2+c^2)} = \frac{\pi}{2(a+b)(b+c)(c+a)}$, then the value of $\int_0^{\infty} \frac{1}{x^2+4)(x^2+9)} dx$ is

(a) $\frac{\pi}{60}$ (b) $\frac{\pi}{20}$ c $\frac{\pi}{40}$ d $\frac{\pi}{80}$

48. $\int e^{a \log x} + e^{x \log a} dx$ is equal to

a $\frac{x^{a+1}}{a+1} + c$ b $\frac{x^{a+1}}{a+1} + \frac{a^x}{\log a} + c$

c $x^{a+1} + a^x + c$ d $\frac{x^{a+1}}{a-1} + \frac{\log a}{a^x} + c$

49. $\int_0^a \frac{dx}{x + \sqrt{a^2 - x^2}}$ is

(a) $\frac{a^2}{4}$ (b) $\frac{\pi}{2}$ (c) $\frac{\pi}{4}$ (d) π

50. If $\int_{-1}^4 f(x) dx = 4$ and $\int_2^4 [3 - f(x)] dx = 7$, then the value of $\int_{-1}^2 f(x) dx$ is

a -2 b 3 c 5 d 8