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	elements in the set A (1) 21	A ∪ B is: (2) 10	(3) 7	(4) Can not say
2.	If A and B are two to:	sets, then $A \cap (A \cup$) B) ^C (where 'C' den	notes complement) is equal
	(1) φ	(2) A	(3) B	(4) A - B
3.	Let $A = \{0, 1, 2, 3, R^{-1} \text{ is } :$	4, 5} and a relation	R is defined by xRy s	such that $2x + y = 10$. Then
	(1) {(4, 3), (2, 4), ((3) {(3, 4), (4, 2), ((2) {(4, 3), (2, 4), (4), (4) {(3, 4), (4, 2), (4)}	
4.	If $A + C = B$, then t	an A tan B tan C =		
	(1) $\tan A + \tan B +$		(2) $\tan A + \tan B$	- tan C
	(3) tan B – tan C –	tan A	$(4) \tan B + \tan C -$	- tan A
5.	If $\sin x + \sin^2 x = 1$,	then $\cos^8 x + 2\cos^6$	$x + \cos^4 x =$	
	(1) 0	(2) 1	(3) -1	(4) 2
6.	If $4 \sin^2 x = 1$, then	the values of x are:		#3
	$(1) n\pi \pm \frac{\pi}{3}$		$(2) n\pi \pm \frac{\pi}{4}$	
	$(3) 2n\pi \pm \frac{\pi}{6}$		$(4) n\pi \pm \frac{\pi}{6}$	
7.	If $n \in \mathbb{N}$, then 3^{3n}	-26n - 1 is divisible	by:	
	(1) 4	(2) 3	(3) 9	(4) 15
8.	$If z = (K+3) + i \sqrt{2}$	$\sqrt{5-k^2}$, then the locu	is of z is:	©.
	(1) a straight line		(2) a parabola	34
	(3) an ellipse		(4) a circle	
9.	If 1, w and w^2 at $(x-1)^3 - 8 = 0$ are		roots of unity, then	the roots of the equation
	(1) $2, 2w, 2w^2$		(2) $3, 2w, 2w^2$ (4) $2, 1 - 2w, 1 -$	
	(3) 3, 1 + 2w, 1 +	$2w^2$	(4) 2, 1-2w, 1-	$2w^2$
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1. The set A has 3 elements and the Set B has 7 elements. The minimum number of

	37	(\n	
10.	The smallest positive integer n for which	$\left(\frac{1+i}{1-i}\right)$	=1, is:

- (1) 4
- (2) 3
- (3) 2
- (4) 1

11. The value of K for which one of the roots of $x^2 - 3x + 2K = 0$ is double of one of the roots of $x^2 - x + K = 0$, is:

- (1) 2
- (3) -1
- (4) 1

12. The interior angles of a regular polygon measure 160° each. The number of diagonals of the polygon are:

- (1) 105
- (2) 135
- (3) 145
- (4) 147

13. The number of ways in which 9 identical balls can be placed in three identical boxes, · is :

- (1) 9
- (2) 12
- (3) 55
- (4) 27

14. In the expansion of $\left(x^2 - \frac{1}{3x}\right)^9$, the term independent of x is :

- (1) 5th
- (2) 6th
- (3) 7th
- (4) 4th

15. If the coefficients of rth and (r + 1)th terms in the expansion of $(3 + 7x)^{29}$ are equal, then r =

- (1) 14
- (2) 15
- (3) 18
- (4) 21

16. Three numbers forms an increasing G.P. If the middle number is doubled, then the new numbers are in A. P. The common ratio of the G. P. is:

(1) $2 + \sqrt{3}$

(2) $3 + \sqrt{2}$

(3) $\sqrt{3} + 1$

(4) $3-\sqrt{2}$

17. If $\frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} + \frac{1}{4^2} + \dots$ to $\infty = \frac{\pi^2}{6}$, then $\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots = \frac{\pi^2}{6}$

- (1) $\frac{\pi^2}{3}$ (2) $\frac{\pi^2}{4}$ (3) $\frac{\pi^2}{8}$ (4) $\frac{\pi^2}{12}$

18. If a, b, c are in A.P. as well as G.P., then which of the following is *true*?

(1) a = b = c

(2) $a = b \neq c$

(3) $a \neq b = c$

(4) $a \neq b \neq c$

19.	quadratic equation is: (1) $x^2 - Ax + G^2 = 0$ (3) $x^2 - 2Ax + G = 0$		(2) $x^2 - Ax + G = 0$ (4) $x^2 - 2Ax + G^2 = 0$	
20.	A line passes throu y-intercept is:	igh the point (2, 2) an	d is perpendicular to	the line $3x + y = 3$, then its
	(1) 2/3	(2) 4/3	(3) 4/5	(4) 3/4
21.	The line $x + y = 4$ value of K is:	divides the line joini	ng (-1, 1) and (5, 7)	in the ratio $K: 1$, then the
	(1) 1/4	(2) 4/3	(3) 1/2	(4) 2
22.	If the foot of the perpendicular from the origin to a straight line is at the point $(3, -4)$. Then the equation of the line is:			line is at the point $(3, -4)$.
	$(1) \ 3x - 4y = 25$	WI No.	$(2) \ 4x - 3y = 25$	
	$(3) \ 4x + 3y = 25$		$(4) \ 3x + 4y = 25$	
23.	The distance between the parallel lines $6x - 3y - 5 = 0$ and $2x - y + 4 = 0$ is:			x - y + 4 = 0 is:
	(1) $3/\sqrt{5}$		(2) $\sqrt{5}/3$	
	(3) $17/3\sqrt{5}$		(4) $17/\sqrt{3}$	
24.	The points $(K+1,$	1), $(2K+1, 3)$ and $(2K+1, 3)$	2K + 2, $2K$) are colling	near, then $K=$
	(1) -1	(2) $\frac{1}{3}$	(3) $\frac{1}{2}$	$(4) -\frac{1}{2}$
25.	The equation of the circle of radius 5 whose centre lies on x-axis and passing through $(2,3)$ is:			x-axis and passing through
	(1) $x^2 + y^2 - 4x - $	21 = 0	(2) $x^2 + y^2 + 4x - 1$	21 = 0
	(3) $x^2 + y^2 + 4x -$	17 = 0	$(4) x^2 + y^2 - 4x + 1$	21 = 0
26.	If the parabola y^2 :	= 4 ax passes through	(3, 2), then the leng	th of its latus-rectum is:
	(1) 2/3	(2) 3/4	(3) 4	(4) 4/3

27. The eccentricity of the hyperbola $16x^2 - 3y^2 - 32x + 12y - 44 = 0$ is:

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(1) $\sqrt{13}$ (2) $\sqrt{7}$ (3) $\sqrt{\frac{17}{3}}$ (4) $\sqrt{\frac{19}{3}}$

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28. The eccentricity of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ whose latus-rectum is half of its major axis,

is:

- (1) $\frac{\sqrt{3}}{2}$ (2) $\frac{\sqrt{3}}{4}$ (3) $\frac{1}{\sqrt{2}}$ (4) $\frac{1}{2}$
- The ratio in which the yz-plane divides the segment joining the points (-2, 4, 7) and (3, -5, 8) is:
 - (1) 7:8
- (2) -7:8 (3) 2:3
- (4) -3:2
- 30. If α , β , γ are the angles which a directed line makes with the positive directions of the co-ordinate axes, then $\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma =$
 - (1) 0
- (2) 1
- (4) 3

- 31. $\lim_{x \to 1} (1-x) \tan \left(\frac{\pi x}{2} \right) =$
 - (1) $\frac{\pi}{2}$ (2) $\frac{2}{\pi}$ (3) $\frac{\pi}{4}$

- (4) 1

- $\lim_{n\to\infty} \frac{(1-2+3-4+5-6....-2n)}{\sqrt{n^2+1}+\sqrt{4n^2-1}} =$
- (1) -2 (2) $\frac{1}{2}$ (3) $\frac{1}{3}$
- $(4) -\frac{1}{3}$

- 33. $\lim_{x\to 0} \frac{\sin(\pi\cos^2 x)}{x^2} =$
 - (1) π
- (2) $\pi/2$
- $(3) -\pi$
- (4) 1

34. If $f(x) = \begin{cases} \frac{x-1}{2x^2 - 7x + 5}, & x \neq 1 \end{cases}$

then the derivative of f(x) at x = 1, is:

- (1) $\frac{9}{2}$
- (2) $\frac{-9}{2}$ (3) $\frac{-2}{9}$ (4) $\frac{2}{9}$
- 35. The mean of n terms is \bar{x} . If the first term is increased by 1, second by 2 and so on, then the new mean is:

- (1) $\overline{x} + \frac{n+1}{2}$ (2) $\overline{x} + \frac{n}{2}$ (3) $\overline{x} + n$ (4) $\overline{x} + \frac{n-1}{2}$

(4) 40.75

(1) 45

	(1) 3/5	(2) 4/5	(3) 3/10	(4) 2/5
38.	There are <i>n</i> person probability that two	ns sitting in a row selected persons are	Two of them are not sitting together,	selected at random. The is:
	$(1) \ \frac{2}{n-2}$	$(2) \frac{n}{n+2}$	$(3) \ \frac{2}{n}$	$(4) 1 - \frac{2}{n}$
39.	Seven digits from the digits 1, 2, 3, 4, 5, 6, 7, 8, 9 are written in a random order. The probability that this seven digit number is divisible by 9, is:			ten in a random order. The
	$(1) \frac{1}{3}$	(2) $\frac{2}{7}$	(3) $\frac{1}{9}$	$(4) \frac{2}{9}$
40.	The coefficients of first three prime nu (1) 2/3	mbers, the probabili	on $ax^2 + bx + c = 0$ (ty that roots of the ed) $(3) 1/4$	$a \neq b \neq c$) are chosen from quation are real, is: (4) 3/4
41.	The graph of the function $y = f(x)$ is symmetrical about the line $x = a$, then which of the following is true ? (1) $f(x+a) = f(x-a)$ (2) $f(x) = f(-x)$			
	(1) $f(x+a) = f(x-a)$ (3) $f(a+x) = f(a)$		(4) $f(x) = -f(-x)$	
42.	Let $f: R \to R$ be a	function defined by	$f(x) = \frac{x^2 + 2x + 5}{x^2 + x + 1},$	then f is:
	(1) one-one and or	nto	(2) one-one and is	nto
	(3) many one and		(4) many one and	l into
43.	$\sin \lambda x + \cos \lambda x$ and	$d \sin x + \cos x $ are	periodic of same fun	damental period, if $\lambda =$
	(1) 4	(2) 0	(3) 2	(4) 1
44.	Let R be a relation (i.e. n/m). Then R		iral numbers defined	by $nRm \Leftrightarrow n$ is a factor of m
	(1) equivalence		(2) transitive and	
	(3) reflexive and	symmetric	(4) reflexive, tran	nsitive but not symmetric
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36. The standard deviation of 25 numbers is 40. If each of the numbers which is greater

37. The sum of 10 items is 12 and the sum of their squares is 18, then the standard

(2) 40

than the standard deviation, is increased by 5, then the new standard deviation will be:

(3) 65



45. If
$$\sin^{-1}\left(\frac{x}{5}\right) + \csc^{-1}\left(\frac{5}{4}\right) = \frac{\pi}{2}$$
, then $x = \frac{\pi}{2}$

- (1) 4
- (3) 5
- (4) 2

$$\tan^{-1}(1+x) + \tan^{-1}(1-x) = \frac{\pi}{2}$$
, is:

- (1) x = 0 (2) x = 1
- (3) x = -1
- (4) $x = \pi$

47. The value of
$$\tan\left(\frac{1}{2}\cos^{-1}\left(\frac{\sqrt{5}}{3}\right)\right)$$
 is:

- (1) $3+\sqrt{5}$ (2) $3-\sqrt{5}$ (3) $\frac{1}{2}(3-\sqrt{5})$ (4) $\frac{1}{2}(\sqrt{5}+3)$

48. Solution of
$$\sin^{-1} x - \cos^{-1} x = \cos^{-1} \frac{\sqrt{3}}{2}$$
 is :

- (1) $x = \frac{1}{2}$ (2) $x = \frac{1}{\sqrt{3}}$ (3) $x = \frac{\sqrt{3}}{2}$ (4) x = 1

49. If
$$A = \begin{bmatrix} 1 & 0 \\ -1 & 7 \end{bmatrix}$$
 and $A^2 = 8A + KI_2$, then the value of K is:

- (1) -1
- (2) 1
- (3) 7
- (4) -7

50. If 1,
$$w$$
, w^2 are cube roots of unity, inverse of which of the following matrices exists?

- (1) $\begin{vmatrix} w & w^2 \\ w^2 & 1 \end{vmatrix}$ (2) $\begin{vmatrix} 1 & w \\ w & w^2 \end{vmatrix}$ (3) $\begin{vmatrix} w^2 & 1 \\ 1 & w \end{vmatrix}$ (4) None of these

51. If A an orthogonal matrix, then which of the following is true?

- (1) |A| = 0

- (2) $|A| = \pm 1$ (3) $|A| = \pm 2$ (4) $|A| = \pi/2$

52. If
$$\Lambda(\alpha) = \begin{bmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{bmatrix}$$
, then $A(\alpha) A(\beta) = \begin{bmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{bmatrix}$

(1) $A(\alpha) + A(\beta)$

(2) $A(\alpha) - A(\beta)$

(3) $\Lambda(\alpha + \beta)$

(4) $A(\alpha - \beta)$

- **53.** If A and B are two matrices such that AB = B and BA = A, then $A^2 + B^2 = A$
 - (1) A + B
- (2) AB
- (3) 2AB
- 54. If K is a real cube root of -2, then the value of $\begin{vmatrix} 1 & 2K & 1 \\ K^2 & 1 & 3K^2 \end{vmatrix}$ is equal to : $\begin{vmatrix} 2 & 2K & 1 \end{vmatrix}$
 - (1) -10
- (2) -12 (3) -13 (4) -15
- 55. The equations Kx y = 2, 2x 3y = -K, 3x 2y = -1 are consistent if K = -K
 - (1) 2, -3
- (2) -2, 3 (3) 1, -4

- **56.** If $f(x) = \begin{vmatrix} a & -1 & 0 \\ ax & a & -1 \\ ax^2 & ax & a \end{vmatrix}$, then $f(2x) f(x) = \begin{bmatrix} a & -1 & 0 \\ ax^2 & ax & a \end{bmatrix}$
 - (1) ax(3a + 2x) (2) ax(2a + 3x) (3) a(2a + 3x) (4) x(3a + 2x)

- 57. Let $f(x) = \frac{1 \tan x}{4x \pi}$, $x \neq \pi/4$ and $x \in [0, \pi/2] = a$, $x = \pi/4$
 - If f(x) is continuous in $[0, \pi/2]$, then a =
 - (1) 1/2
- (2) -1/2
- (3) 1
- (4) 0
- **58.** Let $f(x) = 1 + x (\sin x) [\cos x]$, $0 < x \le \pi/2$, where [.] denotes the greatest integer function. Then which of the following is true?
 - (1) f(x) is continuous in $(0, \pi/2)$
- (2) f(x) is strictly increasing in $(0, \pi/2)$
- (3) f(x) is strictly decreasing in $(0, \pi/2)$ (4) f(x) has global maximum value 2
- **59.** If $y = \tan^{-1} \sqrt{\frac{1 + \sin x}{1 \sin x}}$, $\pi/2 < x < \pi$, then $\frac{dy}{dx} = \frac{1}{2}$
 - (1) -1
- (2) 1
- (3) 1/2
- (4) -1/2

- **60.** If $x = e^{y + e^{y} + e^{y} + \dots + \infty}$, then $\frac{dy}{dx} = \frac{dy}{dx} = \frac{dy}{dx}$
 - (1) $\frac{1-x}{x}$ (2) $\frac{x}{1-x}$ (3) $\frac{1+x}{x}$
- (4) $\frac{x}{1+x}$

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61. If
$$x = a \cos^3 \theta$$
, $y = a \sin^3 \theta$, then $\sqrt{1 + \left(\frac{dy}{dx}\right)^2} =$

- (1) $\sec^2\theta$
- (2) $tan^2\theta$
- (3) $|\sec \theta|$

62. If
$$e^y + xy = e$$
, then the value of $\frac{d^2y}{dx^2}$ for $x = 0$, is:

- (2) $\frac{1}{a^2}$ (3) $\frac{1}{a}$

63. If
$$x^y$$
. $y^x = 16$, then $\frac{dy}{dx}$ at (2, 2) is:

- (1) 0
- (2) 1
- (3) -1
- (4) -4

The approximate value of square root of 25.2 is:

- (1) 5.01
- (2) 5.02
- (3) 5.03
- (4) 5.04

65. The tangent at (1, 1) on the curve $y^2 = x(2-x)^2$ meets it again at the point :

- (1) (-3,7)
- (2) (4, 4)
- $(3) \left(\frac{3}{8}, \frac{9}{4}\right)$

The distance between the origin and the normal to the curve $y = e^{2x} + x^2$ at x = 0 is:

- (1) $4/\sqrt{5}$
- (2) $3/\sqrt{5}$
- (3) $2/\sqrt{5}$
- (4) $2/\sqrt{7}$

67. The length of longest interval in which Rolle's theorem can be applied for the function $f(x) = |x^2 - a^2|, (a > 0), \text{ is }:$

- (1) 2a
- (2) 3a
- (3) 4a
- (4) $a\sqrt{2}$

68. If the function $f(x) = \sqrt{3} \sin x - \cos x - 2ax + b$ decreases for all real values of x, then the value of a is given by:

- (1) a < 1
- $(2) \ a < \sqrt{2} \qquad (3) \ a \ge \sqrt{2}$
- (4) $a \ge 1$

69. The condition that $x^3 + ax^2 + bx + c$ may have no extremum, is :

- (1) $a^2 > 3b$ (2) $a^2 < 3b$ (3) $a^2 > 2b$ (4) $a^2 < 2b$

70. $\int \frac{3 + 2\cos x}{(2 + 3\cos x)^2} dx =$

(1)
$$\frac{\sin x}{2+3\cos x} + c$$
 (2) $\frac{\cos x}{2+3\cos x} + c$ (3) $\frac{2\sin x}{2+3\cos x} + c$ (4) $\frac{2\cos x}{2+3\cos x} + c$

$$(2) \frac{\cos x}{2+3\cos x} + c$$

(3)
$$\frac{2\sin x}{2 + 3\cos x} + c$$

$$(4) \frac{2\cos x}{2+3\cos x} +$$

71. $\int x^x (1 + \log x) dx =$

(1)
$$x^{x} + c$$

(2)
$$x^x \log x + c$$

(3)
$$x \log x + c$$

(1) $x^x + c$ (2) $x^x \log x + c$ (3) $x \log x + c$ (4) none of these

72. $\int \sin \sqrt{x} dx =$

(1)
$$(\cos\sqrt{x} - \sin\sqrt{x}) + c$$

$$(2) \left(\sqrt{x}\cos\sqrt{x} - \sin\sqrt{x}\right) + c$$

$$(3) -2(\sqrt{x}\cos\sqrt{x} - \sin\sqrt{x}) + c \qquad (4) 2(\sqrt{x}\cos\sqrt{x} - \sin\sqrt{x}) + c$$

(4)
$$2(\sqrt{x}\cos\sqrt{x}-\sin\sqrt{x})+c$$

73. $\int \frac{1}{\sqrt{\sin^3 x \cos x}} dx =$

(1)
$$2(\tan x)^{-\frac{1}{2}} + c$$
 (2) $(\tan x)^{\frac{1}{2}} + c$ (3) $(\tan x)^{-\frac{1}{2}} + c$ (4) $2(\tan x)^{\frac{1}{2}} + c$

(2)
$$(\tan x)^{\frac{1}{2}} + c$$

(3)
$$(\tan x)^{-\frac{1}{2}} + c$$

(4)
$$2(\tan x)^{1/2} + c$$

74. If $I_n = \int_0^1 x^n e^{-x} dx$ for $n \in \mathbb{N}$, then $I_n - n I_{n-1} =$

$$(2) -1/e$$

$$(4) -2/e$$

75. If $\int_{\pi/2}^{\theta} \sin x \, dx = \sin 2\theta$, then the value of θ satisfying $0 < \theta < \pi$, is:

- (1) $\pi/6$
- (2) $\pi/4$
- (3) $\pi/2$
- (4) $5\pi/6$

76. $\int_0^{[x]} (x - [x]) dx =$

(1)
$$\frac{1}{2}[x]$$
 (2) $[x]$

- $(3) \ 2[x]$
- (4) -2[x]

77. $\int_0^{\pi/4} \log(1 + \tan x) dx =$

- (1) $\frac{\pi}{4} \log 2$ (2) $\frac{\pi}{8} \log 2$ (3) $\frac{\pi}{2} \log 2$

78. The area bounded by the curve $y = x \sin x$ and x-axis between x = 0 and $x = 2\pi$, is :

(1) π sq. units

(2) $\frac{\pi}{2}$ sq. units

(3) 2π sq. units

(4) 4π sq. units

79. If the area bounded by the curves $y^2 = 4ax$ and y = mx is $a^2/3$ sq. units, then the value of m is:

- (1) 2
- (2) -2
- (3) 1/2
- (4) 3/2

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- **80.** Solution of $\frac{dy}{dx} = \cos(x+y)$ is:
 - (1) $\sin(x+y) = x + c$

(2) $\tan\left(\frac{x+y}{2}\right) + x = c$

- (3) $\cot\left(\frac{x+y}{2}\right) = x+c$
- $(4) \tan\left(\frac{x+y}{2}\right) = x+c$
- **81.** Solution of $ydx + (x y^3) dy = 0$ is :
 - (1) $xy + \frac{y^2}{2} = c$

(2) $xy = \frac{y^2}{2} + c$

(3) $xy = \frac{y^2}{4} + c$

- (4) $xy = \frac{x^2}{4} + c$
- The differential equation $y \frac{dy}{dx} = x + a$ (a being constant) represents a set of:
 - (1) circles having centre on the x-axis
- (2) circles having centre on the y-axis

(3) ellipses

- (4) hyperbolas
- From a bag containing 2 white, 3 red and 4 black balls, two balls are drawn one by one without replacement. The probability that at least ones ball is red, is:
 - $(1) \frac{5}{12}$
- (2) $\frac{7}{12}$ (3) $\frac{5}{8}$
- $(4) \frac{3}{7}$
- 84. A box contains 15 items in which 4 items are defective. The items are selected at random, one by one, and examined. The ones examined are not put back. The probability that 9th one examined is the last defective, is:

- (1) $\frac{7}{195}$ (2) $\frac{8}{195}$ (3) $\frac{16}{255}$ (4) $\frac{14}{255}$
- 85. A person is known to speak truth 3 out of 4 times. He throws a die and reports that it is a six. The probability that it is actually a six, is:
 - $(1) \ \frac{7}{36} \qquad \qquad (2) \ \frac{11}{36} \qquad \qquad (3) \ \frac{3}{8}$

- (4) $\frac{5}{8}$

86.	Four numbers are multiplied together. The probability that the product will be divisible
	by 5 or 10, is:

- (2) $\frac{133}{625}$
- $(4) \frac{369}{625}$

The least number of times a fair coin must be tossed so that the probability of getting at least one head is at lest 0.8, is:

- (1) 3
- (2) 5
- (3) 6
- (4) 8

88. If $P(A \cup B) = \frac{3}{4}$ and $P(\overline{A}) = 2/3$, then $P(\overline{A} \cap B) =$

- (1) $\frac{7}{12}$ (2) $\frac{5}{12}$ (3) $\frac{1}{12}$

89. If $\vec{a} + \vec{b} + \vec{c} = \vec{0}$, $|\vec{a}| = 3$, $|\vec{b}| = 5$, $|\vec{c}| = 7$, then the angle between \vec{a} and \vec{b} is:

- (1) $\pi/3$
- (2) $2\pi/3$
- (3) $\pi/6$
- (4) $5\pi/3$

90. Let \vec{a} and \vec{b} be two unit vectors and α be the angle between them, then $\vec{a} + \vec{b}$ is a unit vector if $\alpha =$

- (1) $\pi/2$
- (2) $\pi/3$
- (3) $2\pi/3$
- (4) $\pi/4$

The unit vector perpendicular to the vectors $\hat{i} + \hat{j}$ and $\hat{j} + \hat{k}$ is/are:

(1) $\pm \frac{1}{\sqrt{3}}(\hat{i} - \hat{j} - \hat{k})$

(2) $\frac{1}{\sqrt{3}}(\hat{i}+\hat{j}-\hat{k})$

(3) $\pm \frac{1}{\sqrt{3}}(\hat{i} - \hat{j} + \hat{k})$

(4) $\frac{1}{\sqrt{2}}(\hat{i} + \hat{k})$

92. The vector $\hat{i} + x\hat{j} + 3\hat{k}$ is rotated through an angle θ and doubled in magnitude, then it becomes $4\hat{i} + (4x-2)\hat{j} + 2\hat{k}$. The value of x is:

- $(1) \frac{1}{3}$

- (2) -3 (3) $\frac{2}{3}$ (4) $-\frac{2}{3}$

93. The vectors $\overrightarrow{AB} = 3\hat{i} + 2\hat{j} + 2\hat{k}$ and $\overrightarrow{BC} = -\hat{i} - 2\hat{k}$ are the adjacent sides of a parallelogram. The angle between its diagonals is:

- (1) $\pi/6$
- (2) $\pi/3$
- (3) $\pi/2$
- (4) $\pi/4$

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- 94. Consider a LPP: min Z = 6x + 10ysubjected to $x \ge 6$, $y \ge 2$, $2x + y \ge 10$; $x, y \ge 0$. Redundand constraints in this LPP are:
 - (1) $x \ge 0, y \ge 0$

(2) $2x + y \ge 10$

(3) $x \ge 6$, $2x + y \ge 10$

- (4) None of these
- The angle between the lines having direction ratios 4, -3, 5 and 3, 4, 5 is:
 - (1) $\pi/3$
- (2) $\pi/4$
- (3) $\pi/6$
- (4) $2\pi/3$
- 96. If a plane meets the coordinate axes at A, B and C in such a way that the centroid of triangle ABC it at the point (1, 2, 3), then the equation of the plane is:
 - (1) $\frac{x}{1} + \frac{y}{2} + \frac{z}{3} = 1$

(2) $\frac{x}{3} + \frac{y}{6} + \frac{z}{9} = 1$

(3) $\frac{x}{1} + \frac{y}{2} + \frac{z}{3} = \frac{1}{3}$

- (4) $\frac{x}{3} + \frac{y}{6} + \frac{z}{9} = 3$
- 97. The image of the point (1, 3, 4) in the plane 2x y + z + 3 = 0 is:
 - (1) (3, 5, 2)

(2) (3, 5, -2)

(3) (-3, 5, 2)

- (4) (3, -5, 2)
- **98.** The lines $\frac{x}{1} = \frac{y}{2} = \frac{z}{3}$ and $\frac{x-1}{-2} = \frac{y-2}{-4} = \frac{z-3}{-6}$ are :
 - (1) intersecting

(2) parallel

(3) coincidental

- (4) skew
- 99. The distance between the line $\vec{r} = 2\hat{i} 2\hat{j} + 3\hat{k} + \lambda(\hat{i} \hat{j} + 4\hat{k})$ and the plane $\vec{r} \cdot (\hat{i} + 5\hat{j} + \hat{k}) = 5$ is:

- (1) $\frac{10}{3\sqrt{3}}$ (2) $\frac{10}{\sqrt{3}}$ (3) $\frac{10}{3}$ (4) $\frac{5}{3\sqrt{3}}$
- 100. The lines $\frac{x-2}{1} = \frac{y-3}{1} = \frac{z-4}{-k}$ and $\frac{x-1}{k} = \frac{y-4}{2} = \frac{z-5}{1}$ are coplanar if $k = \frac{y-4}{1} = \frac{y-4}{1} = \frac{z-5}{1}$
 - (1) 4
- $(2) \ 3$
- (3) -1
- (4) -3