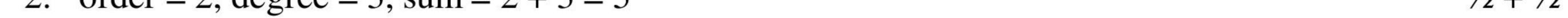
CBSE Class 12 Mathematics Compartment Answer Key 2015 (July 16, Set 2 - 65/1/2)

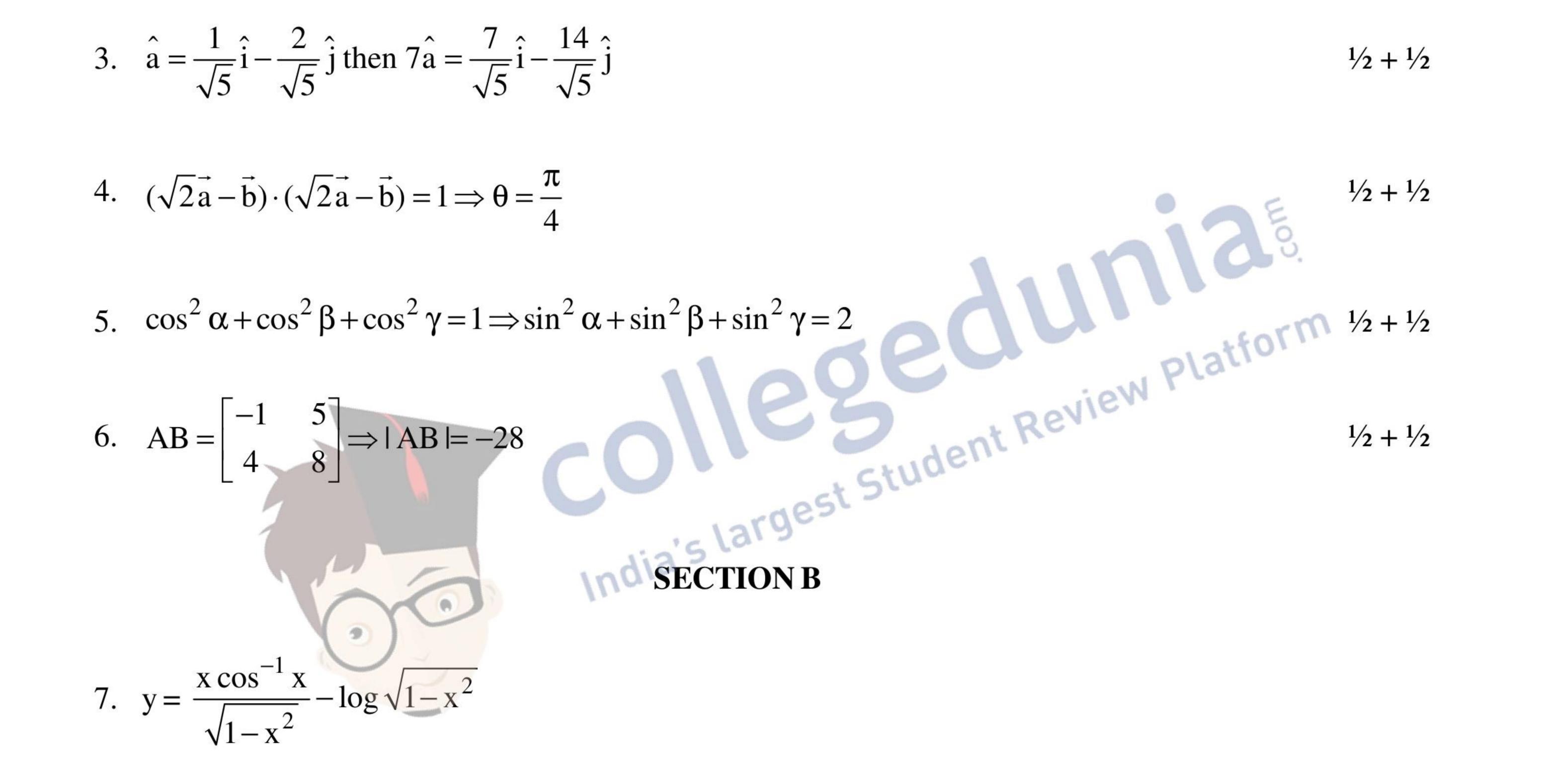
QUESTION PAPER CODE 65/1/2 EXPECTED ANSWER/VALUE POINTS SECTION A

Marks

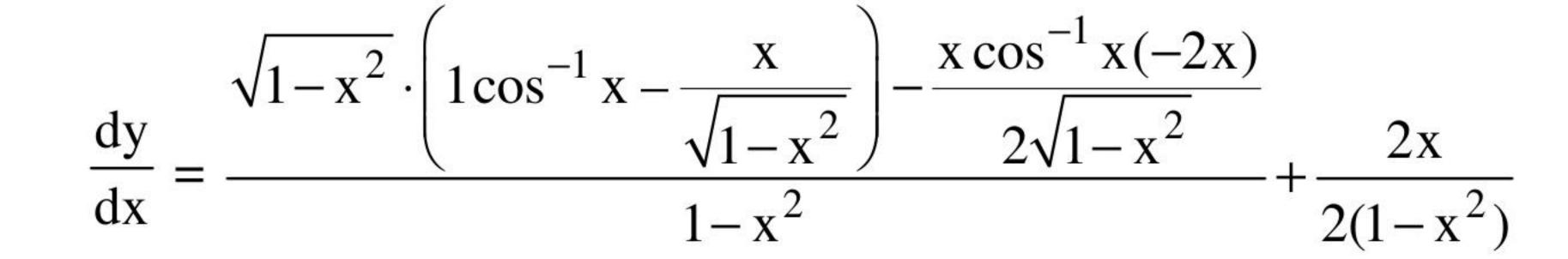
1.
$$1 \cdot y + x \frac{dy}{dx} = -c \sin x \Rightarrow x \frac{dy}{dx} + y + xy \tan x = 0$$

2. order = 2. degree = 3. sum = 2 + 3 = 5. $\frac{1/2 + 1/2}{1/2}$

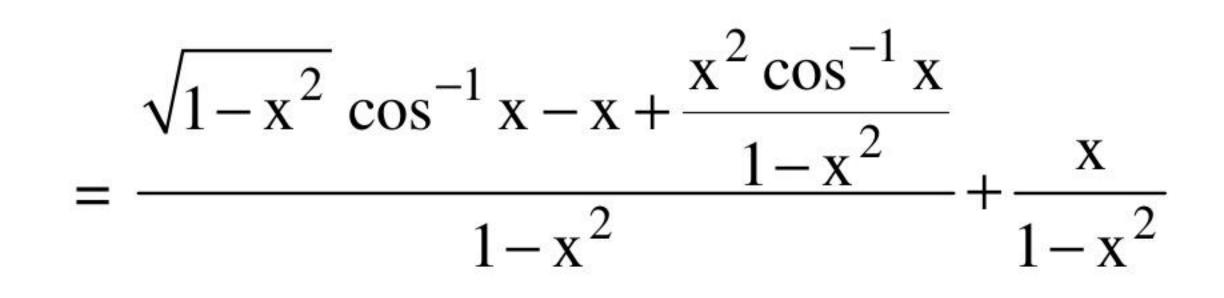




12



1 + 1



$$=\frac{(1-x^2)\cos^{-1}x + x^2\cos^{-1}x}{(1-x^2)^{3/2}} = \frac{\cos^{-1}x}{(1-x^2)^{3/2}}$$



8.
$$y = (\sin x)^x + \sin^{-1} \sqrt{x}$$

$$\Rightarrow$$
 y = e^{x log sin x} + sin⁻¹ \sqrt{x}

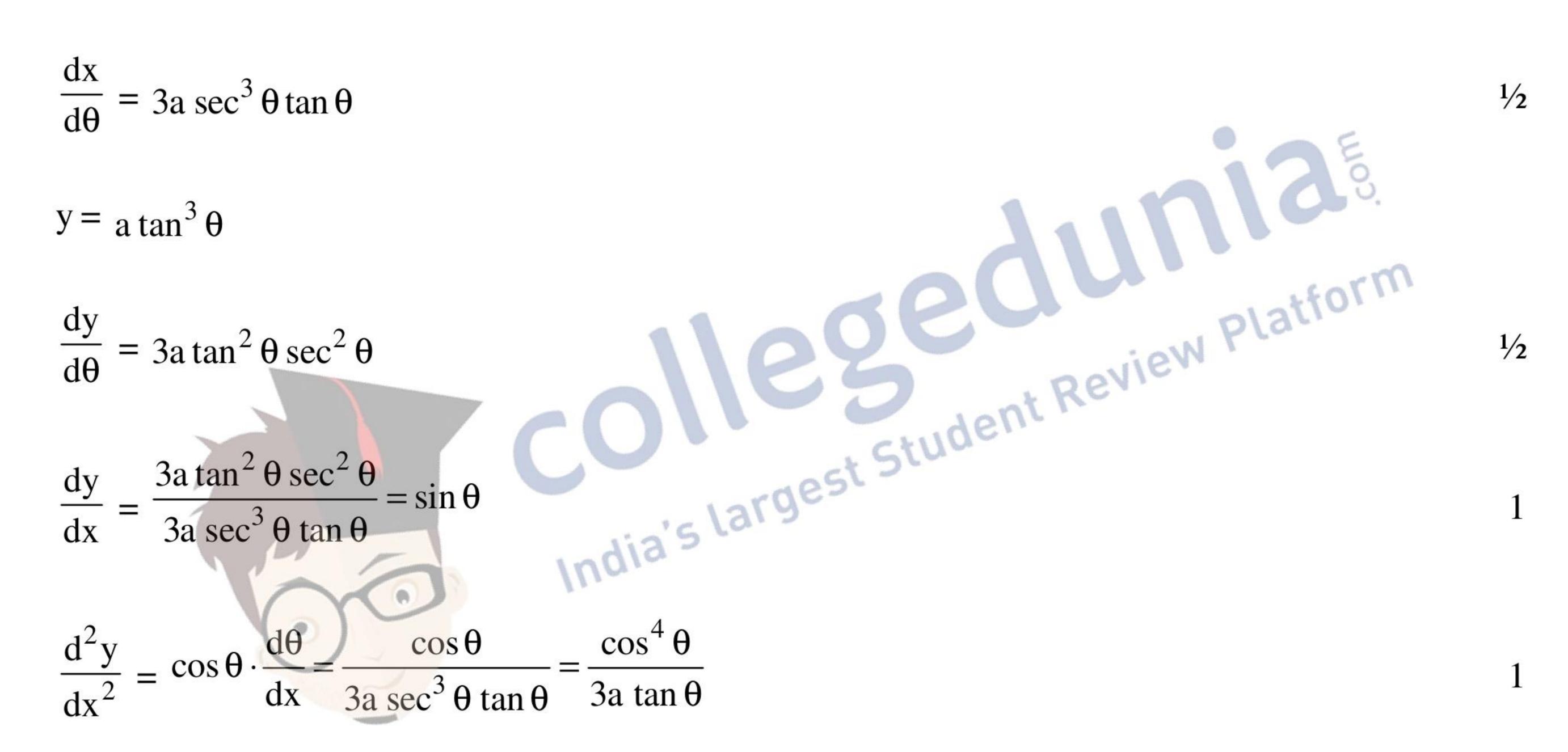
$$\Rightarrow \frac{dy}{dx} = e^{x \log \sin x} [\log \sin x + x \cot x] + \frac{1}{2\sqrt{x} \sqrt{1-x}}$$

11/2

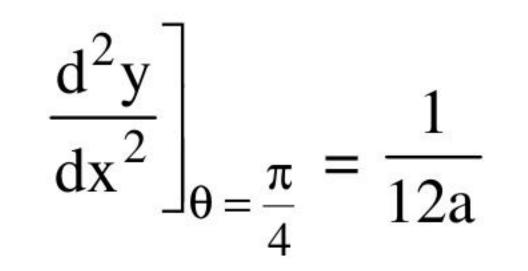
$$\Rightarrow \frac{dy}{dx} = (\sin x)^{x} (\log \sin x + x \cot x) + \frac{1}{2\sqrt{x} \sqrt{1-x}}$$

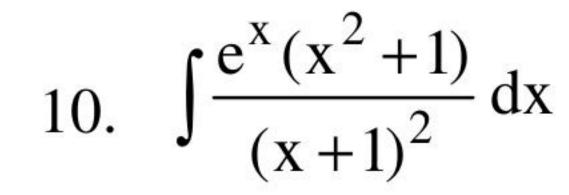
11⁄2

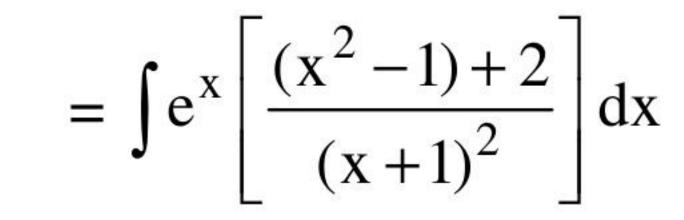
9. $x = a \sec^3 \theta$

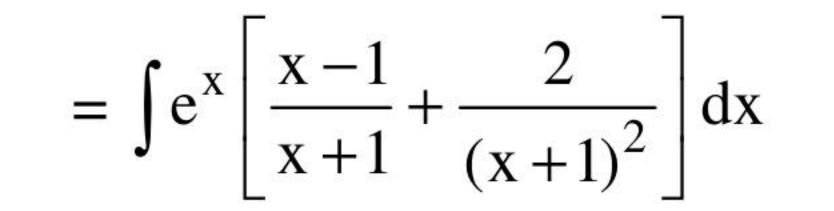


13

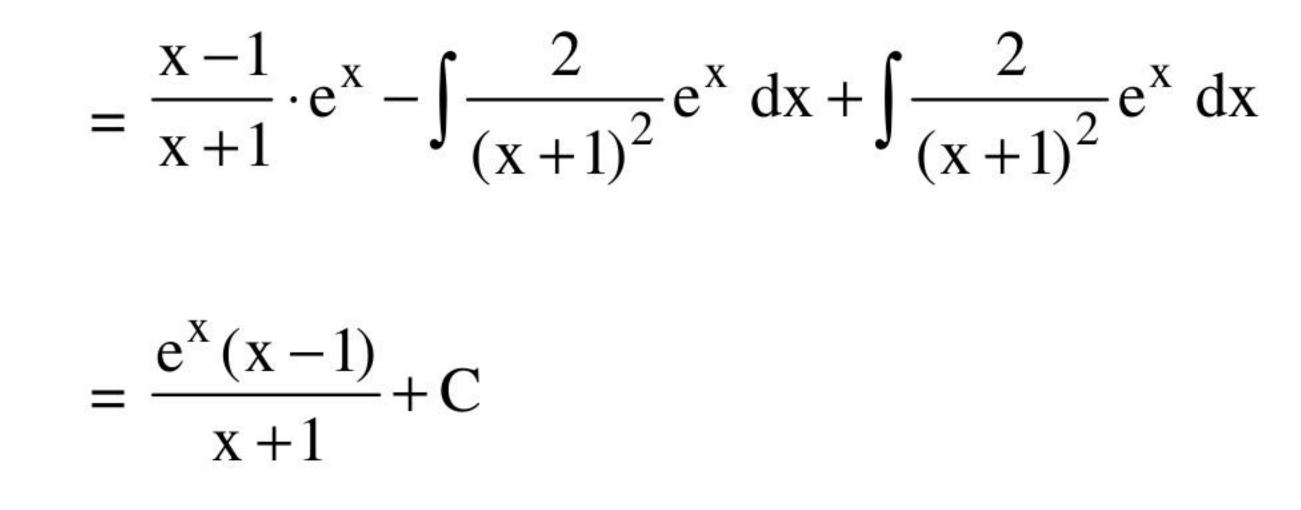








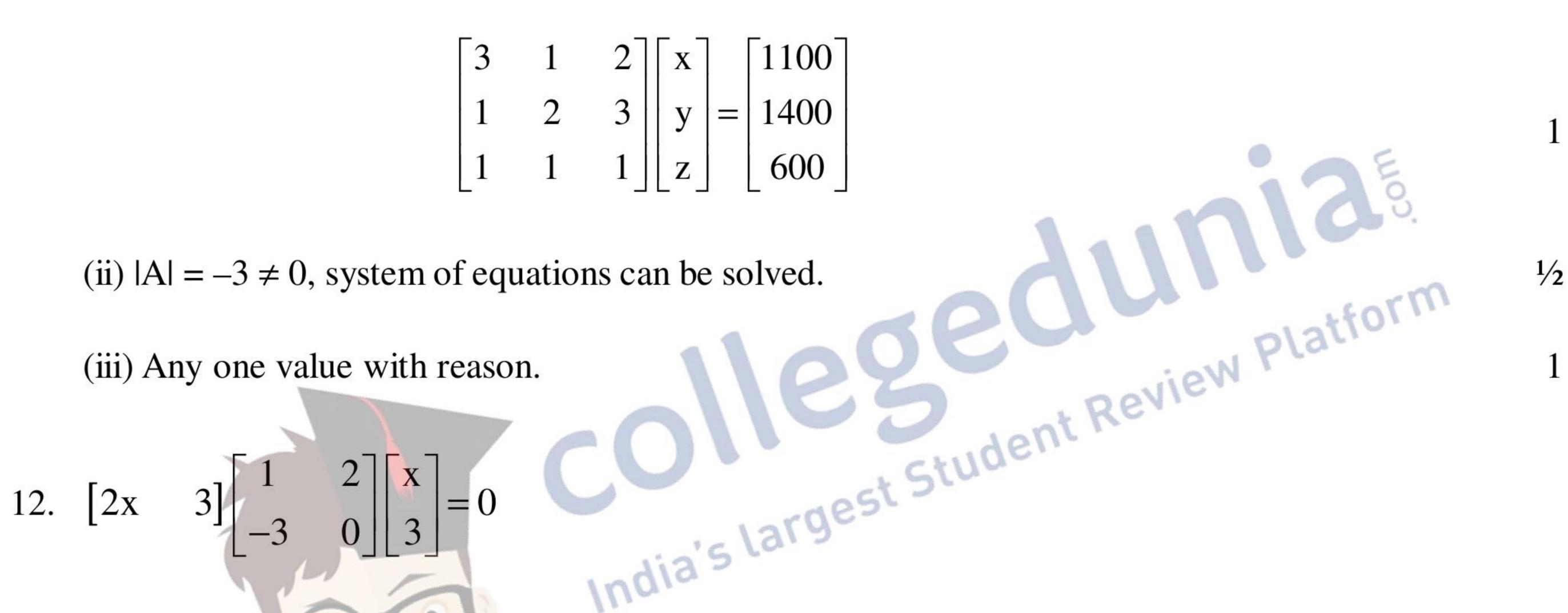




11. System of equation is

$$3x + y + 2z = 1100, x + 2y + 3z = 1400, x + y + z = 600$$
 1¹/₂

(i) Matrix equation is



14

$$\begin{bmatrix} 2x - 9 & 4x \end{bmatrix} \begin{bmatrix} x \\ 3 \end{bmatrix} = 0$$

$$[2x^2 - 9x + 12x] = [0] \Rightarrow 2x^2 + 3x = 0, x = 0 \text{ or } \frac{-3}{2}$$

1 + 1 + 1

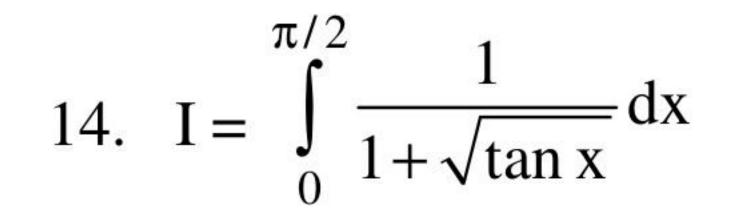
13.
$$\begin{vmatrix} (a+1) (a+2) & a+2 & 1 \\ (a+2) (a+3) & a+3 & 1 \\ (a+3) (a+4) & a+4 & 1 \end{vmatrix}$$

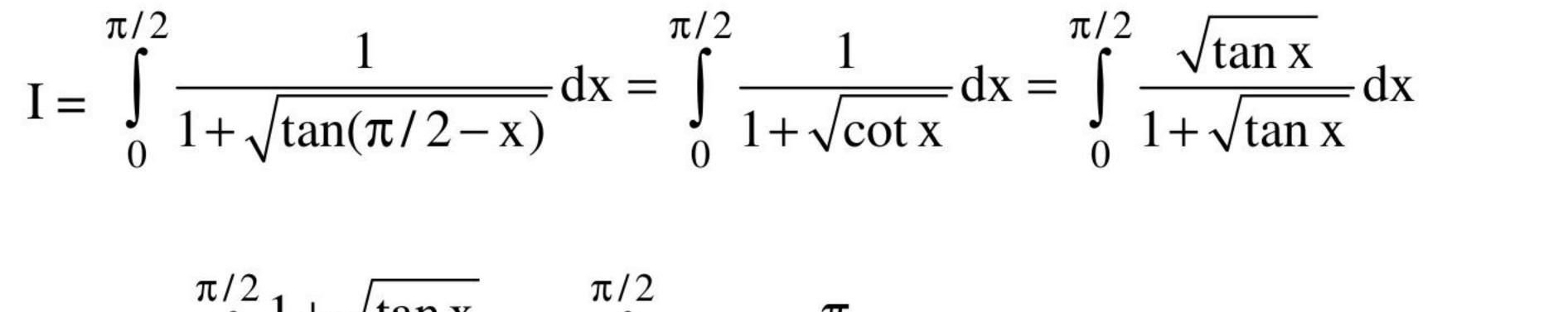
$$= \begin{vmatrix} (a+1) (a+2) & a+2 & 1 \\ 2(a+2) & 1 & 0 \\ 4a+10 & 2 & 0 \end{vmatrix} \begin{array}{c} R_2 \to R_2 - R_1 \\ R_3 \to R_3 - R_1 \end{array}$$

1 + 1

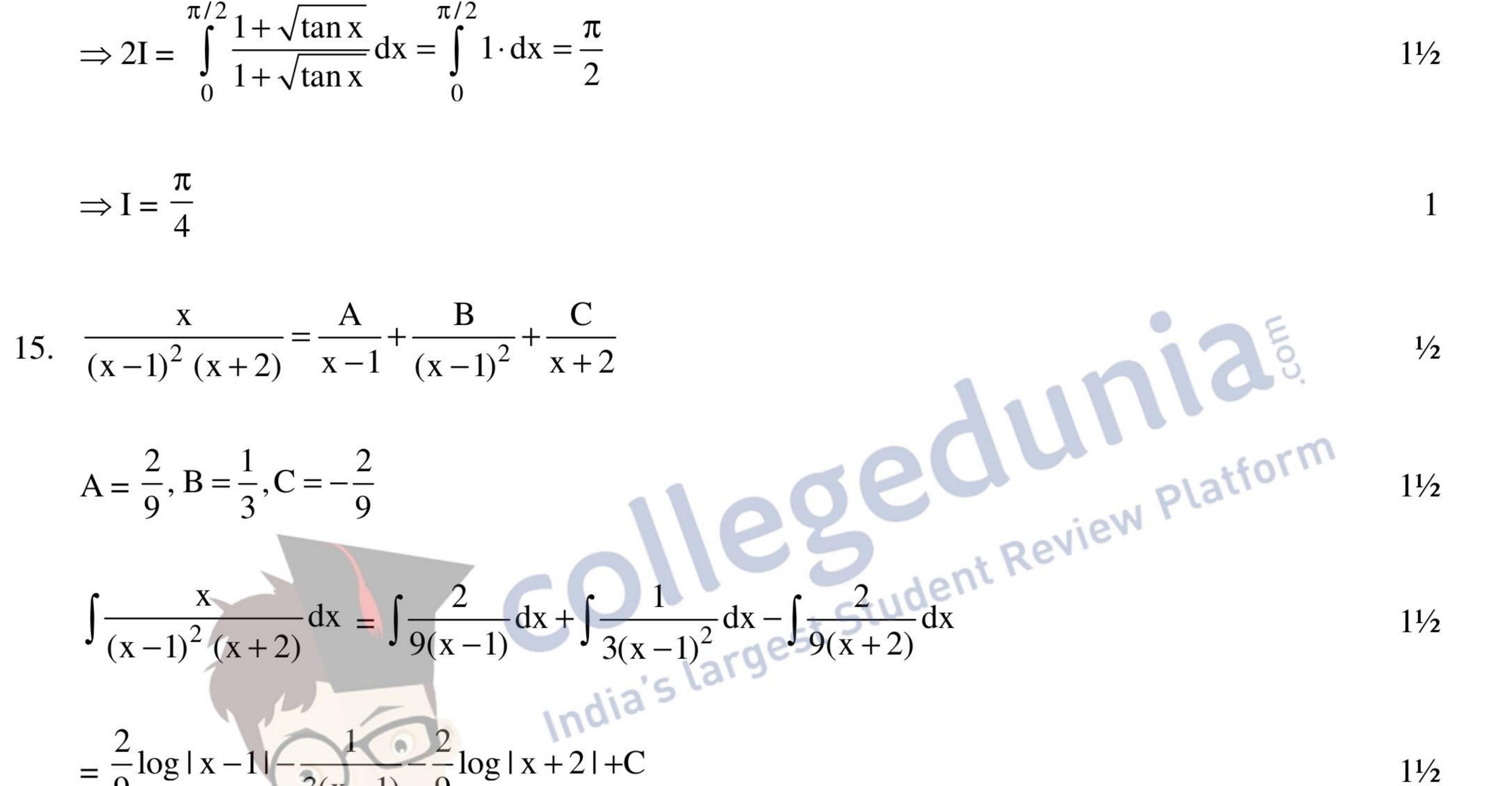
$$= 4a + 8 - 4a - 10 = -2.$$

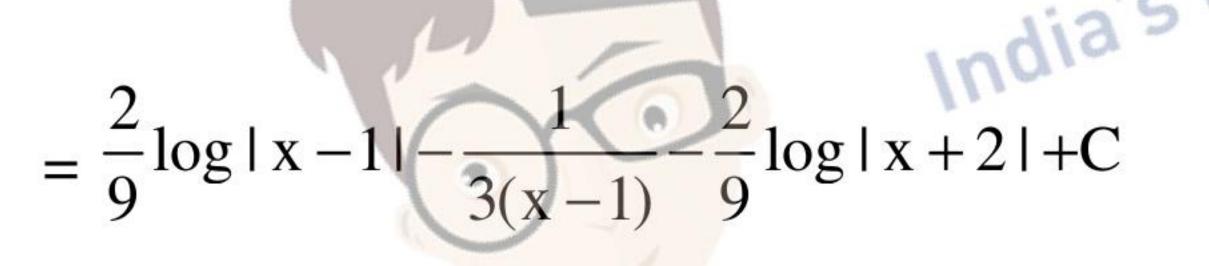






11/2





16. Let X be the number of defective bulbs. Then

X = 0, 1, 2

$$P(X = 0) = \frac{10_{C_2}}{15_{C_2}} = \frac{3}{7}, \ P(X = 1) = \frac{10_{C_1} \cdot 5_{C_1}}{15_{C_2}} = \frac{10}{21}$$

$$P(X = 2) = \frac{5_{C_2}}{15_{C_2}} = \frac{2}{21}$$

1 + 1

X	0	1	2
P(X)	$\frac{3}{7}$	10 21	$\frac{2}{21}$

15



OR

E_1 : Problem is solved by A.

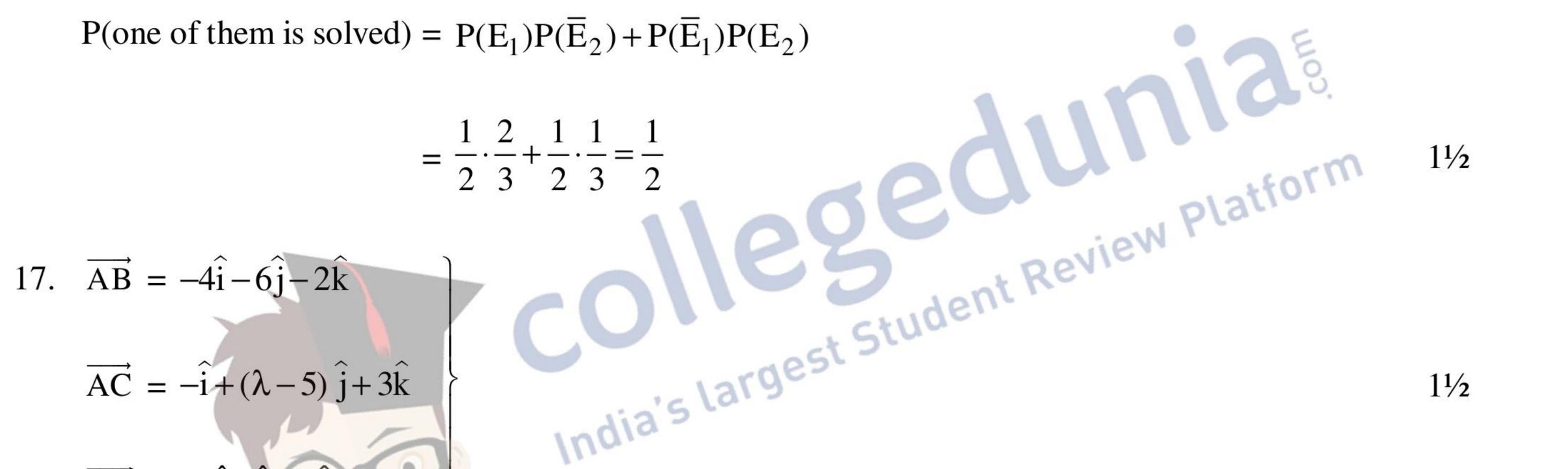
E_2 : Problem is solved by B.

$$P(E_1) = \frac{1}{2}, P(E_2) = \frac{1}{3}, P(\overline{E}_1) = \frac{1}{2}, P(\overline{E}_2) = \frac{2}{3}$$

$$P(E_1 \cap E_2) = P(E_1) \cdot P(E_2) = \frac{1}{6}$$

11/2

P(problem is solved) =
$$1 - P(\overline{E}_1) \cdot P(\overline{E}_2) = 1 - \frac{1}{2} \cdot \frac{2}{3} = \frac{2}{3}$$



$$\overrightarrow{AD} = -8\hat{i} - \hat{j} + 3\hat{k}$$

$$\overrightarrow{AD} = -8\hat{i} - \hat{j} + 3\hat{k}$$

$$\overrightarrow{AD} = \begin{vmatrix} -4 & -6 & -2 \\ -1 & \lambda - 5 & 3 \\ -8 & -1 & 3 \end{vmatrix} = 0$$

$$-4(3\lambda - 12) + 6(21) - 2(8\lambda - 39) = 0 \Longrightarrow \lambda = 9$$

18.
$$\vec{a}_1 = \hat{i} + 2\hat{j} + \hat{k}, \vec{b}_1 = \hat{i} - \hat{j} + \hat{k}$$

 $\vec{a}_2 = 2\hat{i} - \hat{i} - \hat{k}, \vec{b}_2 = 2\hat{i} + \hat{i} + 2\hat{k}$

11/2

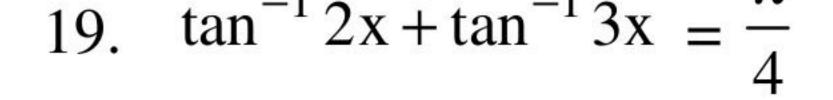
$$\vec{a}_2 - \vec{a}_1 = \hat{i} - 3\hat{j} - 2\hat{k}, \vec{b}_1 \times \vec{b}_2 = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & -1 & 1 \\ 2 & 1 & 1 \end{vmatrix} = -3\hat{i} + 3\hat{k}$$
16

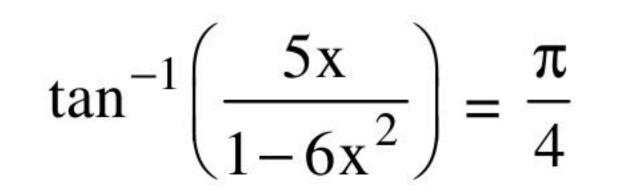
 $\frac{1}{2} + 1$

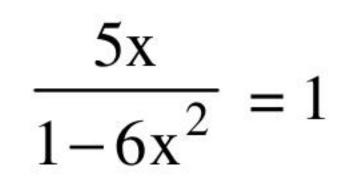


$$|\vec{b}_{1} \times \vec{b}_{2}| = 3\sqrt{2}$$

$$(\vec{a}_{2} - \vec{a}_{1}) \cdot (\vec{b}_{1} - \vec{b}_{2}) = -3 - 6 = -9$$
Shortest distance $= \left|\frac{-9}{3\sqrt{2}}\right| = \frac{3\sqrt{2}}{2}$







$$\Rightarrow 6x^2 + 5x - 1 = 0$$

$$\frac{5x}{1-6x^2} = 1$$

$$\Rightarrow 6x^2 + 5x - 1 = 0$$

$$\Rightarrow x = \frac{1}{6}, x = -1 \text{ (rejected)}$$

$$1$$

$$1$$

$$1$$

$$1$$

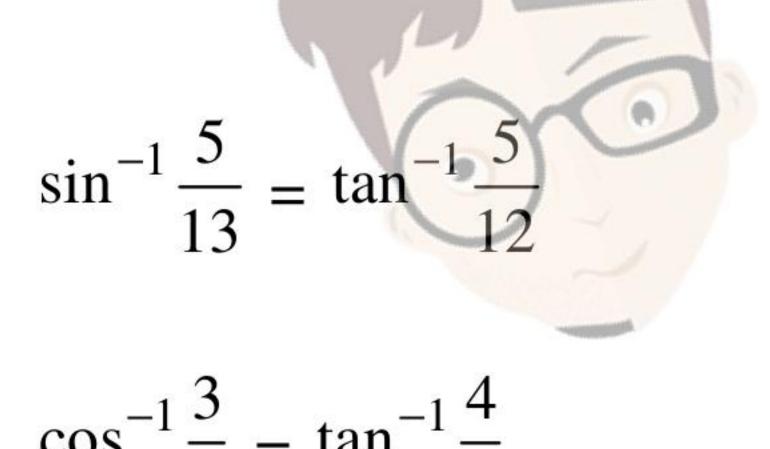
$$1$$

$$1$$

$$1$$

$$1$$

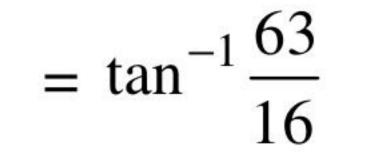
17



 $\cos^{-1}\frac{3}{5} = \tan^{-1}\frac{4}{3}$

R.H.S. =
$$\sin^{-1}\frac{5}{13} + \cos^{-1}\frac{3}{5} = \tan^{-1}\frac{5}{12} + \tan^{-1}\frac{4}{3}$$

$$= \tan \left(\frac{\frac{5}{12} + \frac{4}{3}}{\frac{1}{12} + \frac{5}{3}} \right)$$



*These answers are meant to be used by evaluators



 $1/_{2}$

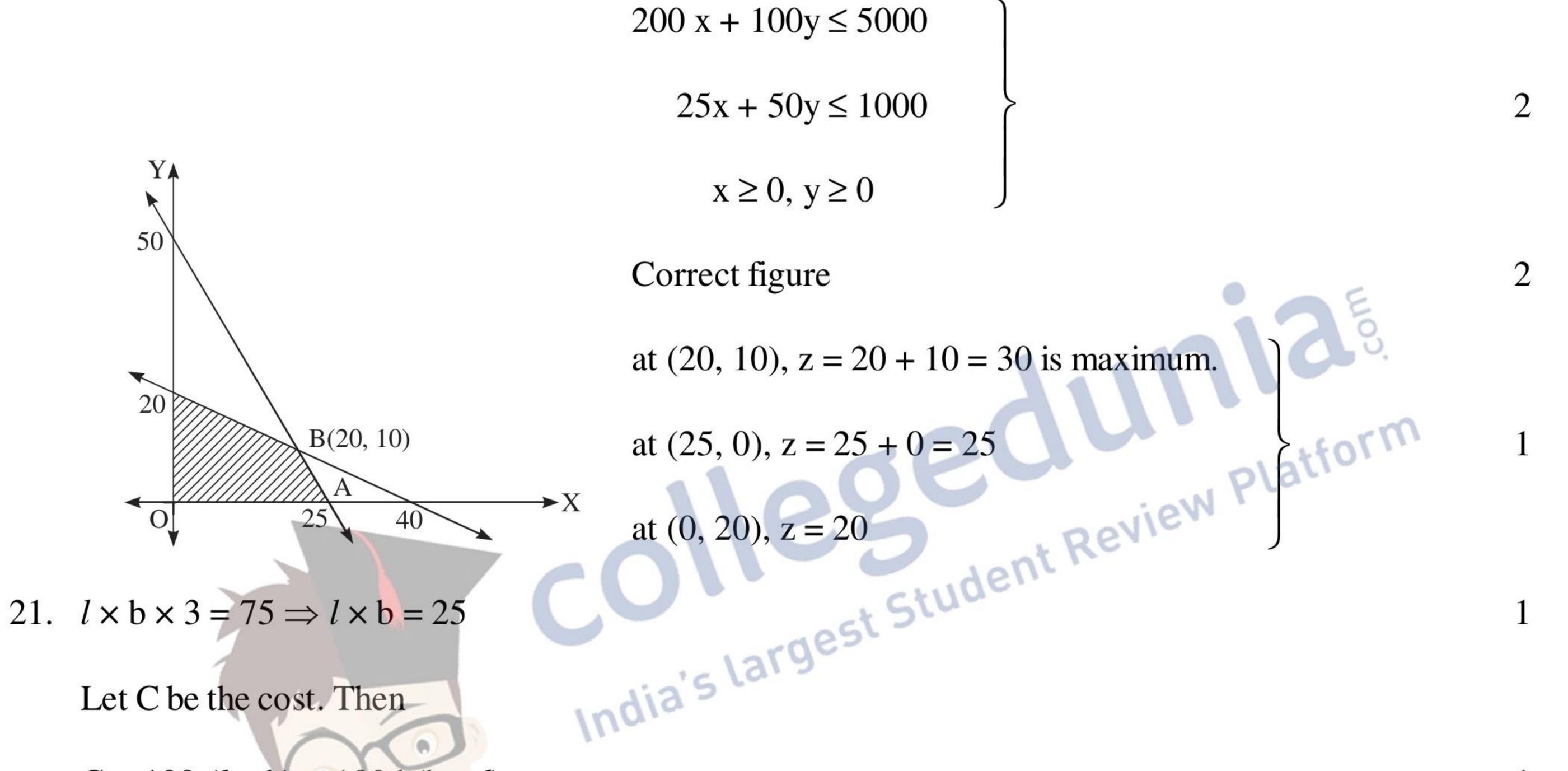
SECTION C

Let x and y be the number of takes. Then

Maximise:

z = x + y

Subject to:



18

Let C be the cost. Then

 $C = 100 \ (l \times b) + 100 \ h(b + l)$

$$C = 100 \left(l \times \frac{25}{l} \right) + 300 \left(\frac{25}{l} + l \right)$$

$$\frac{dC}{dl} = 0 + 300 \left(\frac{-25}{1^2} + 1 \right)$$

$$\frac{\mathrm{dC}}{\mathrm{d}l} = 0 \Longrightarrow l = 5$$

$$d^2C$$

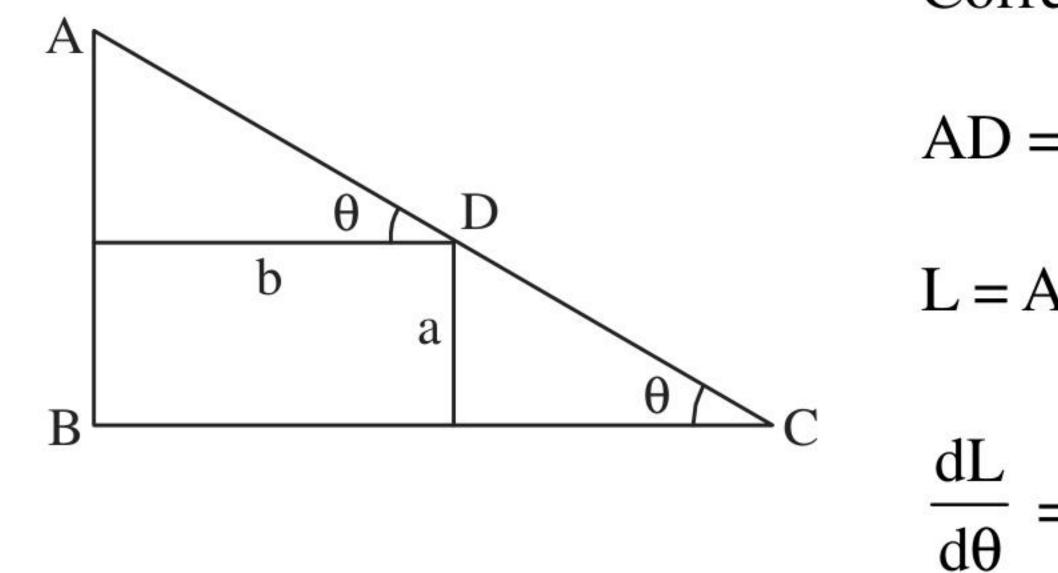
$\frac{1}{dl^2} > 0 \Rightarrow C$ is maximum when $l = 5 \Rightarrow b = 5$

C = 100 (25) + 300(10)) = Rs. 5500



OR

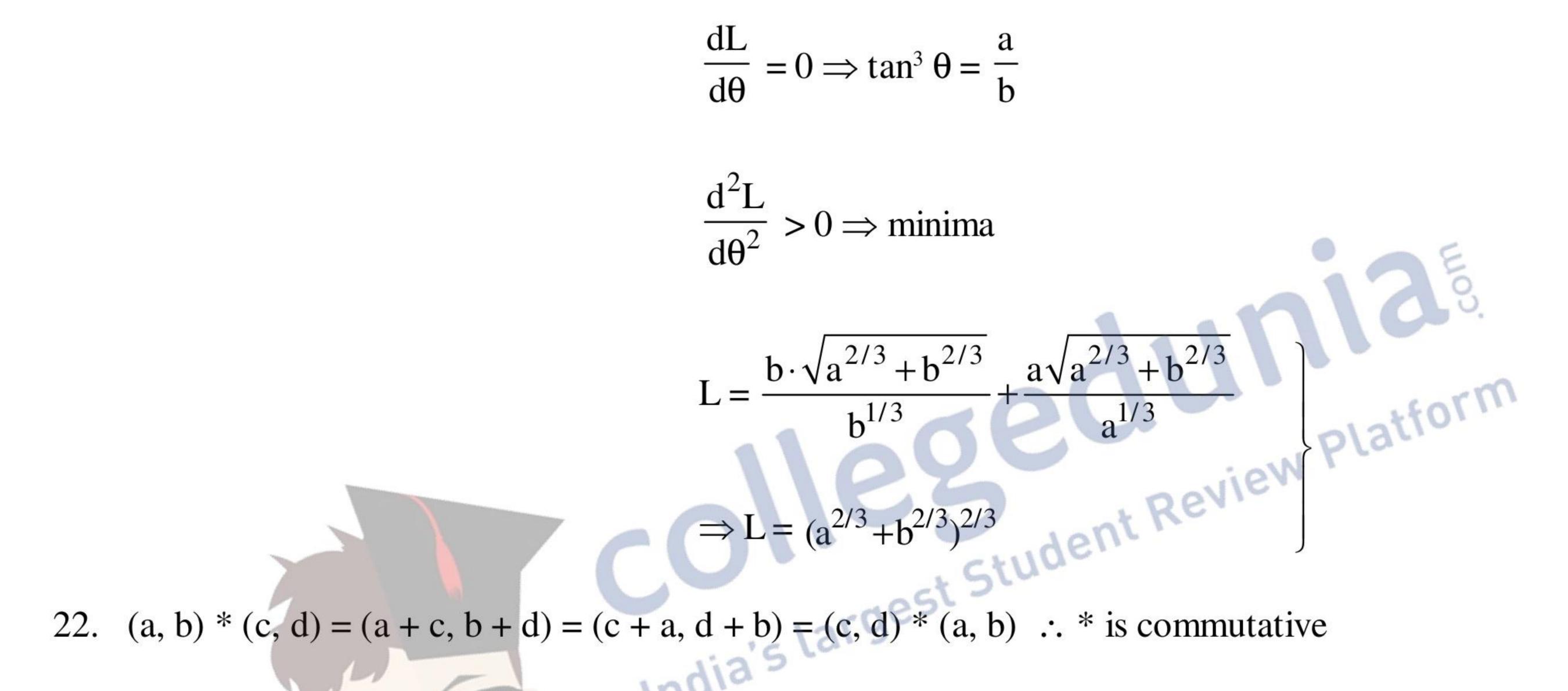
Correct figure



 $AD = b \sec \theta$, $DC = a \csc \theta$

$$L = AC = b \sec \theta + a \csc \theta$$

= b sec θ tan θ – acosec θ cot θ



11/2

2

 $1/_{2}$

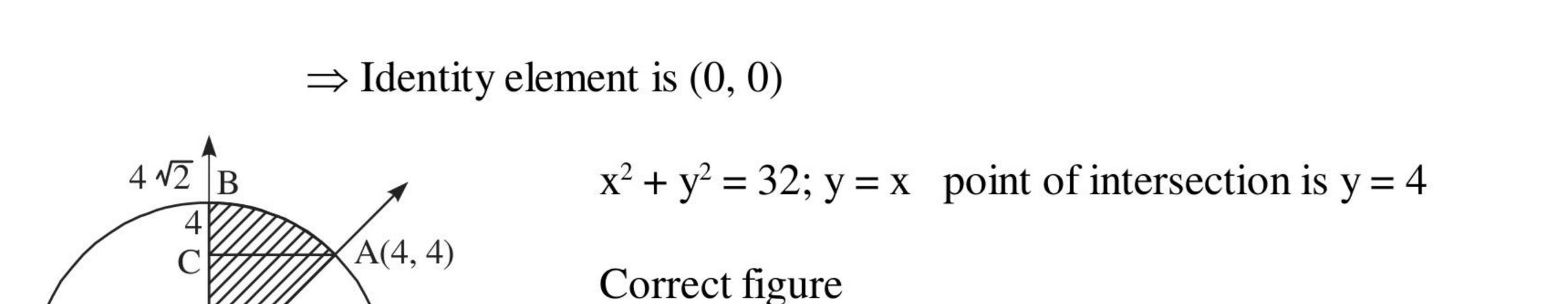
 $1\frac{1}{2}$

- [(a, b) * (c, d)] * (e, f) = (a + c, b + d) * (e, f)
 - = (a + c + e, b + d + f) = (a, b) * (c + e, d + f)
 - = (a, b) * [(c, d) * (e, f) :: * is associate

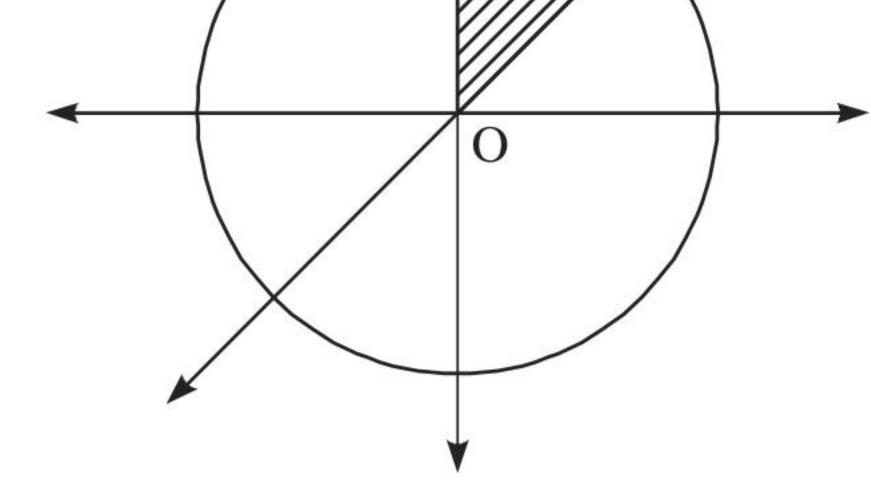
Let (e, e') be the identity

23.

 $(a, b) * (e, e') = (a, b) \Rightarrow (a + e, b + e') = (a, b) \Rightarrow e = 0, e' = 0$



19



Required Area =
$$\int_{0}^{4} y \, dy + \int_{4}^{4\sqrt{2}} \sqrt{32 - y^2} dy$$



$$= \left[\frac{y^2}{2}\right]_0^4 + \left[\frac{y}{2}\sqrt{32 - y^2} + 16\sin^{-1}\frac{y}{4\sqrt{2}}\right]_4^{4\sqrt{2}}$$

$$= 8 + \left(0 + 16 \cdot \frac{\pi}{2}\right) - \left(8 + 16 \cdot \frac{\pi}{2}\right) = 4\pi \qquad 1\frac{1}{2}$$

 $dy = \frac{dy}{dy + v - v + vv \cot v} = 0 \rightarrow \frac{dy}{dy + (1 + \cot v)} v = 1$ $1/_{2}$

OR

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24.
$$x - x + y - x + xy \cot x = 0 \Rightarrow \frac{1}{dx} + \left(\frac{1}{x} + \cot x\right)y = 1$$

I.F. =
$$e^{\int \left(\frac{1}{x} + \cot x\right) dx} = x \sin x$$

Solution: $y \cdot x \sin x = \int 1 \cdot x \sin x \, dx$

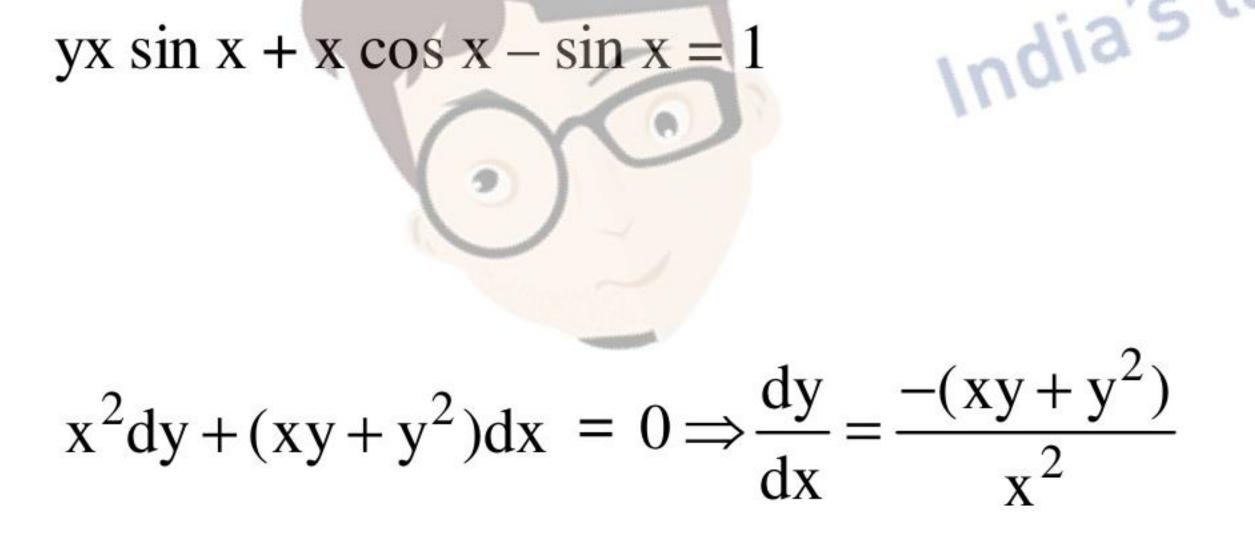
$$\Rightarrow$$
 yx sin x = -x cos x + sin x + C

when

x =

ution:
$$y \cdot x \sin x = \int 1 \cdot x \sin x \, dx$$

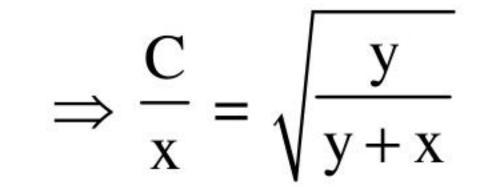
 $yx \sin x = -x \cos x + \sin x + C$
 $\frac{\pi}{2}, y = 0$, we have $C = -1$
 $\sin x + x \cos x - \sin x = 1$
OP



Put
$$y = vx \Rightarrow \frac{dy}{dx} = v + x \frac{dv}{dx}$$

$$\Rightarrow v + x \frac{dv}{dx} = -(v + v^2) \Rightarrow \frac{dv}{v^2 + 2v} = -\frac{dx}{dx}$$

$$\Rightarrow \int \frac{dv}{(v+1)^2 - (1)^2} - \int \frac{dx}{x} \Rightarrow \frac{1}{2} \log \frac{v}{v+2} = -\log x + \log C$$





If x = 1, y = 1, then C =
$$\frac{1}{\sqrt{3}}$$

 $\Rightarrow \frac{1}{\sqrt{3} x} = \sqrt{\frac{y}{y+x}}$

25. Plane passing through the intersection of given planes:

 $(x + y + z - 1) + \lambda(2x + 3y + 4z - 5) = 0$

$$(1 + 2\lambda)x + (1 + 3\lambda)y + (1 + 4\lambda)z + (-1 - 5\lambda) = 0$$

$$1\frac{1}{2}$$
Now $(1 + 2\lambda) 1 + (1 + 3\lambda) (-1) + (1 + 4\lambda)1 = 0$

$$1\frac{1}{2}$$
Equation of required plane is
$$\Rightarrow x - z + 2 = 0$$
26. • _1: First bag is selected.
E_2: Second bag is selected.
A: both balls are red.
$$1$$

21

A: both balls are red.

9

$$P(E_1) = \frac{1}{2}, P(E_2) = \frac{1}{2}, P\left(\frac{A}{E_1}\right) = \frac{12}{56}, P\left(\frac{A}{E_2}\right) = \frac{2}{56}$$

