QUESTION PAPER CODE 65/1/P

EXPECTED ANSWERS/VALUE POINTS

SECTION-A

Marks

1.
$$|A| = -19$$
 \(\frac{1}{2}\) m

$$A^{-1} = -\frac{1}{19} \begin{pmatrix} -2 & -5 \\ -3 & 2 \end{pmatrix}$$
 ½ m

$$2. \qquad \frac{\mathrm{dy}}{\mathrm{dx}} = c$$

$$y = x \left(\frac{dy}{dx}\right) + \left(\frac{dy}{dx}\right)^2$$

3.
$$\frac{dx}{dy} + \frac{x}{1+y^2} = \frac{\tan^{-1}y}{1+y^2}$$
 1/2 m

I.F.
$$= e^{\tan^{-1}y}$$

4.
$$\vec{a} \cdot (\vec{b} \times \vec{a}) = [\vec{a} \ \vec{b} \ \vec{a}] = 0$$

5.
$$\vec{a} + \vec{b} = 3\hat{i} + 3\hat{j}$$

$$(\vec{a} + \vec{b}) \cdot \vec{c} = 3$$

6.
$$\frac{x+3}{0} = \frac{y-4}{3} = \frac{z-2}{-1}$$

D.Rs are
$$0, 3, -1$$

SECTION - B

7.
$$\begin{array}{c|cccc}
A & 25 & 12 & 34 \\
B & 22 & 15 & 28 \\
C & 26 & 18 & 36
\end{array}
\begin{pmatrix}
20 \\
15 \\
5
\end{pmatrix}$$
1½ m



$$= \begin{pmatrix} 850 \\ 805 \\ 970 \end{pmatrix}$$
1½ m

Any relevant value

1 m

8.
$$\tan^{-1}\left(\sqrt{\frac{a-b}{a+b}}\tan\frac{x}{2}\right) = \cos^{-1}\left\{\frac{1-\frac{a-b}{a+b}\tan^2\frac{x}{2}}{1+\frac{a-b}{a+b}\tan^2\frac{x}{2}}\right\}$$

$$1\frac{1}{2}m$$

$$= \cos^{-1} \left\{ \frac{a + b - a \tan^{2} \frac{x}{2} + b \tan^{2} \frac{x}{2}}{a + b + a \tan^{2} \frac{x}{2} - b \tan^{2} \frac{x}{2}} \right\}$$

$$= \cos^{-1} \left\{ \frac{a \left(1 - \tan^{2} \frac{x}{2}\right) + b \left(1 + \tan^{2} \frac{x}{2}\right)}{\left(1 + \frac{x}{2} + \frac{x}{2}\right)} \right\}$$
1/2 m

$$= \cos^{-1} \left\{ \frac{a \left(1 - \tan^2 \frac{x}{2} \right) + b \left(1 + \tan^2 \frac{x}{2} \right)}{a \left(1 + \tan^2 \frac{x}{2} \right) + b \left(1 - \tan^2 \frac{x}{2} \right)} \right\}$$
¹/₂ m

$$= \cos^{-1} \left\{ \frac{a \frac{1 - \tan^2 \frac{x}{2}}{1 + \tan^2 \frac{x}{2}}}{1 + \tan^2 \frac{x}{2}} \right\}$$

$$\frac{1 - \tan^2 \frac{x}{2}}{1 + \tan^2 \frac{x}{2}}$$

$$\frac{1 - \tan^2 \frac{x}{2}}{1 + \tan^2 \frac{x}{2}}$$

$$= \cos^{-1} \left\{ \frac{a \cos x + b}{a + b \cos x} \right\}$$
¹/₂ m

OR

$$\tan^{-1}\left(\frac{x-2}{x-3}\right) + \tan^{-1}\left(\frac{x+2}{x+3}\right) = \frac{\pi}{4}$$



$$\Rightarrow \tan^{-1}\left(\frac{\frac{x-2}{x-3} + \frac{x+2}{x+3}}{1 - \frac{x-2}{x-3} \cdot \frac{x+2}{x+3}}\right) = \frac{\pi}{4}$$
1½ m

$$\Rightarrow \tan^{-1}\left(\frac{2x^2 - 12}{-5}\right) = \frac{\pi}{4}$$

$$\Rightarrow \frac{2x^2 - 12}{-5} = 1 \Rightarrow x^2 = \frac{7}{2}$$

$$\Rightarrow x = \sqrt{\frac{7}{2}}$$

For writing no solution as |x| < 1

9.
$$A^{2} = \begin{pmatrix} 2 & 0 & 1 \\ 2 & 1 & 3 \\ 1 & -1 & 0 \end{pmatrix} \begin{pmatrix} 2 & 0 & 1 \\ 2 & 1 & 3 \\ 1 & -1 & 0 \end{pmatrix} = \begin{pmatrix} 5 & -1 & 2 \\ 9 & -2 & 5 \\ 0 & -1 & -2 \end{pmatrix}$$
 2 m

$$A^{2} - 5A + 16I = \begin{pmatrix} 5 & -1 & 2 \\ 9 & -2 & 5 \\ 0 & -1 & -2 \end{pmatrix} - \begin{pmatrix} 10 & 0 & 5 \\ 10 & 5 & 15 \\ 5 & -5 & 0 \end{pmatrix} + \begin{pmatrix} 16 & 0 & 0 \\ 0 & 16 & 0 \\ 0 & 0 & 16 \end{pmatrix}$$

$$1 \text{ m}$$

$$= \begin{pmatrix} 11 & -1 & -3 \\ -1 & 9 & -10 \\ -5 & 4 & 14 \end{pmatrix}$$
1 m

10. Taking x from R_2 , x (x – 1) from R_3 and (x + 1) from C_3

$$\Delta = x^{2} (x-1) (x+1) \begin{vmatrix} 1 & x & 1 \\ 2 & x-1 & 1 \\ -3 & x-2 & 1 \end{vmatrix}$$
2 m

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$$C_2 \rightarrow C_2 - x C_1$$
; $C_3 \rightarrow C_3 - C$,

$$= x^{2} (x^{2} - 1) \begin{vmatrix} 1 & 0 & 0 \\ 2 & -1 - x & -1 \\ -3 & 4x - 2 & 4 \end{vmatrix}$$
 1 m

$$= x^{2} (x^{2} - 1) \begin{vmatrix} -1(1+x) & -1 \\ 4x - 2 & 4 \end{vmatrix}$$
¹/₂ m

$$= 6x^2 (1-x^2)$$

11.
$$\frac{dx}{dt} = \alpha \left[-2\sin 2t \sin 2t + 2\cos 2t (1 + \cos 2t) \right]$$

$$\frac{dy}{dt} = \beta \left[2 \sin 2 t \cos 2 t - (1 - \cos 2 t) \cdot 2 \sin 2 t \right]$$

$$\frac{dy}{dx} = \left(\frac{dy}{dt}\right) / \left(\frac{dx}{dt}\right) = \frac{\beta \left(2\sin 4t - 2\sin 2t\right)}{\alpha \left(2\cos 4t + 2\cos 2t\right)}$$
¹/₂+1 m

11.
$$\frac{dx}{dt} = \alpha \left[-2\sin 2t \sin 2t + 2\cos 2t (1 + \cos 2t) \right]$$

$$\frac{dy}{dt} = \beta \left[2\sin 2t \cos 2t - (1 - \cos 2t) \cdot 2\sin 2t \right]$$

$$\frac{dy}{dx} = \left(\frac{dy}{dt} \right) / \left(\frac{dx}{dt} \right) = \frac{\beta \left(2\sin 4t - 2\sin 2t \right)}{\alpha \left(2\cos 4t + 2\cos 2t \right)}$$

$$\frac{\beta}{\alpha} \cdot \frac{2\cos 3t \sin t}{2\cos 3t \cos t} = \frac{\beta}{\alpha} \tan t$$

$$\frac{1}{2} \sin 2t \cos 2t + 2\cos 2t$$

12. Let
$$y = \cos^{-1}\left(\frac{x - x^{-1}}{x - x^{-1}}\right) = \cos^{-1}\left(\frac{x^2 - 1}{x^2 + 1}\right)$$

$$=\pi-\cos^{-1}\left(\frac{1-x^2}{1+x^2}\right)$$

$$=\pi-2\,tan^{-1}x$$

$$\therefore \frac{dy}{dx} = -\frac{2}{1+x^2}$$

13. Let
$$y = \cos^{-1} \left\{ \sin \sqrt{\frac{1+x}{2}} \right\} + x^{x}$$

Let
$$u = \cos^{-1} \left\{ \sin \sqrt{\frac{1+x}{2}} \right\}; \quad v = x^x$$

$$\therefore y = u + v$$

$$\frac{dy}{dx} = \frac{du}{dx} + \frac{dv}{dx}$$

$$u = \cos^{-1} \left\{ \sin \sqrt{\frac{1+x}{2}} \right\} = \cos^{-1} \left[\cos \cdot \left(\frac{\pi}{2} - \sqrt{\frac{1+x}{2}} \right) \right]$$

$$= \frac{\pi}{2} - \sqrt{\frac{1+x}{2}}$$

$$u = \cos^{-1}\left\{\sin\sqrt{\frac{1+x}{2}}\right\} = \cos^{-1}\left[\cos\cdot\left(\frac{\pi}{2} - \sqrt{\frac{1+x}{2}}\right)\right]$$

$$= \frac{\pi}{2} - \sqrt{\frac{1+x}{2}}$$

$$\therefore \frac{du}{dx} = -\frac{1}{2\sqrt{2}\sqrt{1+x}}$$
.....(i)

1/2 m

$$\therefore \log v = x \log x$$

$$\frac{1}{v} \frac{dv}{dx} = x \cdot \frac{1}{x} + 1 \log x = 1 + \log x$$

$$\frac{\mathrm{dv}}{\mathrm{dx}} = \mathbf{x}^{x} \left(1 + \log \mathbf{x} \right) \dots (ii)$$

$$\therefore \frac{dy}{dx} = -\frac{1}{2\sqrt{2}\sqrt{1+x}} + x^{x}\left(1 + \log x\right)$$
¹/₂ m

$$\left(\frac{dy}{dx}\right)_{at \ x=1} = -\frac{1}{4} + 1 = \frac{3}{4}$$
 1/2 m



14.
$$I = \int_{0}^{\frac{\pi}{2}} \frac{2^{\sin x}}{2^{\sin x} + 2^{\cos x}} dx$$
(i)

$$= \int_{0}^{\frac{\pi}{2}} \frac{2^{\sin(\frac{\pi}{2} - x)}}{2^{\sin(\frac{\pi}{2} - x)} + 2^{\cos(\frac{\pi}{2} - x)}} dx \left[\text{using } \int_{0}^{a} (x) dx = \int_{0}^{a} f(a - x) dx \right]$$
1½ m

$$= \int_{0}^{\frac{\pi}{2}} \frac{2^{\cos x}}{2^{\sin x} + 2^{\cos x}} dx \qquad (ii)$$

Adding (i) and (ii),

$$2I = \int_{0}^{\pi/2} 1 \, dx = \left[x\right]_{0}^{\pi/2} = \frac{\pi}{2}$$

$$\Rightarrow I = \frac{\pi}{4}$$

$$I = \int_{0}^{\pi/2} |x \cos(\pi x)| \, dx$$

$$y_{2} = \frac{\pi}{2}$$

$$y_{3} = \frac{\pi}{2}$$

$$y_{4} = \frac{\pi}{2}$$

$$y_{5} = \frac{\pi}{2}$$

$$y_{6} = \frac{\pi}{2}$$

$$y_{7} = \frac{\pi}{2}$$

$$y_{8} = \frac{\pi}{2}$$

$$\Rightarrow I = \frac{\pi}{4}$$

$$I = \int_{0}^{3/2} |x \cos(\pi x)| dx$$

$$= \int_{0}^{\frac{1}{2}} x \cos \pi x \, dx - \int_{\frac{1}{2}}^{\frac{3}{2}} x \cos \pi x \, dx$$
1 m

$$= \left[\frac{x \sin \pi x}{\pi}\right]_{0}^{\frac{1}{2}} - \int_{0}^{\frac{1}{2}} \frac{\sin \pi x}{\pi} dx - \left[\frac{x \sin \pi x}{\pi}\right]_{\frac{1}{2}}^{\frac{3}{2}} + \int_{\frac{1}{2}}^{\frac{3}{2}} \frac{-\sin \pi x}{\pi} dx$$

$$1\frac{1}{2}m$$

$$= \frac{1}{2\pi} + \frac{1}{\pi^2} \left[\cos \pi \, x\right]_0^{\frac{1}{2}} + \frac{3}{2\pi} + \frac{1}{2\pi} + \frac{1}{\pi^2} \left[\cos \pi \, x\right]_{\frac{1}{2}}^{\frac{3}{2}}$$

$$= \frac{1}{2\pi} - \frac{1}{\pi^2} + \frac{3}{2\pi} + \frac{1}{2\pi} + 0$$

$$=\frac{5}{2}-\frac{1}{-2}$$

15.
$$I = \int \left(\sqrt{\cot x} + \sqrt{\tan x} \right) dx$$

$$= \int \frac{\cos x + \sin x}{\sqrt{\sin x \cos x}} dx$$

$$= \sqrt{2} \int \frac{\left(\cos x + \sin x\right)}{\sqrt{1 - \left(1 - 2\sin x \cot x\right)}} dx$$

$$= \sqrt{2} \int \frac{\cos x + \sin x}{\sqrt{1 - (\sin x - \cos x)^2}} dx$$

Put
$$\sin x - \cos x = t \implies (\cos x + \sin x) dx = dt$$

$$\therefore I = \sqrt{2} \int \frac{dt}{\sqrt{1-t^2}} = \sqrt{2} \sin^{-1}t + c$$

$$= \sqrt{2} \sin^{-1} (\sin x - \cos x) + c$$
 \(\frac{1}{2} \sin^{-1} (\sin x - \cos x) + c

$$= \sqrt{2} \int \frac{1}{\sqrt{1 - (\sin x - \cos x)^2}} dx$$

$$Put \sin x - \cos x = t \Rightarrow (\cos x + \sin x) dx = dt$$

$$\therefore I = \sqrt{2} \int \frac{dt}{\sqrt{1 - t^2}} = \sqrt{2} \sin^{-1} t + c$$

$$= \sqrt{2} \sin^{-1} (\sin x - \cos x) + c$$

$$1/2 m$$

$$= \sqrt{2} \sin^{-1} (\sin x - \cos x) + c$$

$$1/2 m$$

$$= x - \int \frac{x^3 - 1}{x(x^2 + 1)} dx$$

$$= x - \int \frac{x + 1}{x(x^2 + 1)} dx$$

$$1/2 m$$

$$= x - \int \frac{x+1}{x(x^2+1)} dx$$

$$= x - I_1$$

Let
$$\frac{x+1}{x(x^2+1)} = \frac{A}{x} + \frac{Bx+C}{x^2+1} = \frac{1}{x} + \frac{1-x}{x^2+1}$$

$$I_1 = \int \frac{1}{x} + \frac{(1-x)}{x^2 + 1} dx = \log x - \frac{1}{2} \log |x^2 + 1| + \tan^{-1} x$$

:.
$$I = x - \log |x| + \frac{1}{2} \log |x^2 + 1| - \tan^{-1}x + c$$

17. Here
$$\overrightarrow{AB} = -4\hat{i} - 6\hat{j} - 2\hat{k}$$

$$\overrightarrow{AC} = -\hat{i} + 4\hat{j} + 3\hat{k}$$

$$\overrightarrow{AD} = -8\hat{i} - \hat{j} + 3\hat{k}$$
1½ m

For them to be coplanar,
$$\begin{bmatrix} \vec{AB} & \vec{AC} & \vec{AD} \end{bmatrix} = 0$$
 1½ m

i.e.
$$\begin{vmatrix} -4 & -6 & -2 \\ -1 & 4 & 3 \\ -8 & -1 & 3 \end{vmatrix} = -60 + 126 - 66 = 0$$
^{1/2} m

∴ Points A, B, C and D are coplanar

18. Here
$$\begin{vmatrix} b-c-(a-d) & b-a & b+c-(a+d) \\ \alpha-\delta & \alpha & \alpha+\delta \\ \beta-\gamma & \beta & \beta+\gamma \end{vmatrix}$$

21/2 m

18. Here $\begin{vmatrix} b-c-(a-d) & b-a & b+c-(a+d) \\ \alpha-\delta & \alpha & \alpha+\delta \\ \beta-\gamma & \beta & \beta+\gamma \end{vmatrix}$

21/2 m

19. The second representation of the seco

$$= 2 \begin{vmatrix} b-a & b-a & b+c-a-d \\ \alpha & \alpha & \alpha+\delta \\ \beta & \beta & \beta+\gamma \end{vmatrix} C_1 \rightarrow C_1 + C_3$$

$$\beta + \gamma = 2 \begin{vmatrix} b-a & b-a & b+c-a-d \\ \alpha & \alpha+\delta & C_1 + C_3 \end{vmatrix}$$

$$\beta + \gamma = 2 \begin{vmatrix} b-a & b-a & b+c-a-d \\ \alpha & \alpha+\delta & C_1 + C_3 \end{vmatrix}$$

= 0 (:
$$C_1$$
 and C_2 are identical)

Hence given lines are coplanar
$$\frac{1}{2}$$
 m

OR

D.R's of normal to the plane are
$$5, -4, 7$$

D.R's of y - axis :
$$0, 1, 0$$

If θ is the angle between the plane and y-axis, then

$$\sin \theta = \frac{a_1 a_2 + b_1 b_2 + c_1 c_2}{\sqrt{a_1^2 + b_1^2 + c_1^2} \sqrt{a_2^2 + b_2^2 + c_2^2}}$$

$$=\frac{-4}{3\sqrt{10}}$$



$$\therefore \quad \theta = \sin^{-1} \left(\frac{-4}{3\sqrt{10}} \right)$$

$$\therefore \text{ Acute angle is } \sin^{-1} \left(\frac{4}{3\sqrt{10}} \right)$$

Let E be the event of getting number greater than 4 19.

∴
$$P(E) = \frac{1}{3}$$
 and $P(\overline{E}) = \frac{2}{3}$

1 m

$$= \frac{2}{3} \cdot \frac{1}{3} + \left(\frac{2}{3}\right)^3 \cdot \frac{1}{3} + \left(\frac{2}{3}\right)^5 \cdot \frac{1}{3} + \dots \infty$$

$$= \frac{2}{9} \left[1 + \left(\frac{2}{3} \right)^2 + \left(\frac{2}{3} \right)^4 + \dots \infty \right]$$
¹/₂ m

$$= \frac{2}{3} \cdot \frac{1}{3} + \left(\frac{2}{3}\right)^{3} \cdot \frac{1}{3} + \left(\frac{2}{3}\right)^{5} \cdot \frac{1}{3} + \dots \infty$$

$$= \frac{2}{9} \left[1 + \left(\frac{2}{3}\right)^{2} + \left(\frac{2}{3}\right)^{4} + \dots \infty \right]$$

$$= \frac{2}{9} \times \frac{9}{5} = \frac{2}{5}$$
OR
OR

$$A = \{(5, 6, 1), (5, 6, 2), (5, 6, 3), (5, 6, 4), (5, 6, 5), (5, 6, 6), \}$$

$$P(A) = \frac{6}{6 \times 6 \times 6} = \frac{1}{36}, P(B) = P(\text{getting 3 or 4 on the third throw})$$
 1½ m

$$A \cap B = \{(5, 6, 3), (5, 6, 4)\} \Rightarrow P(A \cap B) = \frac{2}{6 \times 6 \times 6} = \frac{1}{108}$$

$$P(B/A) = \frac{P(A \cap B)}{P(A)} = \frac{1}{3}$$

SECTION - C

20. Let
$$y = (fog)(x)$$
 [say $y = h(x)$]
= $f[g(x)] = f(x^3 + 5)$ 2½ m



$$= 2(x^3+5)-3$$

$$= 2 x^3 + 7$$

$$2\frac{1}{2}$$
 m

$$\therefore x = \sqrt[3]{\frac{y-7}{2}} = h^{-1}(y)$$

$$\frac{1}{2}$$
 m

$$\therefore \quad (\text{fog})^{-1} = \sqrt[3]{\frac{x-7}{2}}$$

$$\frac{1}{2}$$
 m

OR

Let (x, y) be the identity element in $Q \times Q$, then

$$(a,b) * (x,y) = (a,b) = (x,y)*(a,b) \forall (a,b) \in Q \times Q$$

$$1\frac{1}{2}$$
 n

$$\Rightarrow$$
 $(ax, b + ay) = (a, b)$

$$\Rightarrow$$
 a = ax and b = b + ay

$$\Rightarrow$$
 x = 1 and y =

$$\therefore$$
 (1,0) is the identity element in Q × Q

I m Let (a,b) be the invertible element in $Q\times Q$. Let (a,b) be the invertible element in $Q\times Q$, then $-\infty$ is the identity element in $Q\times Q$, then

there exists
$$(\alpha, \beta) \in Q \times Q$$
 such that $(a, b) * (\alpha, \beta) = (\alpha, \beta) * (a, b) = (1, 0)$

 $1\frac{1}{2}$ m

$$\Rightarrow$$
 $(a\alpha, b + a\beta) = (1, 0)$

1 m

$$\Rightarrow \alpha = \frac{1}{a}, \beta = -\frac{b}{a}$$

$$\therefore \text{ the invertible element in A is } \left(\frac{1}{a}, - \frac{b}{a}\right)$$

 $\frac{1}{2}$ m

21.
$$f(x) = 2x^3 - 9 m x^2 + 12 m^2 x + 1, m > 0$$

$$f'(x) = 6x^2 - 18 \text{ m x} + 12 \text{ m}^2$$

1 m

$$f''(x) = 12x - 18 \text{ m}$$

1 m

For Max. or minimum, $f'(x) = 0 \Rightarrow 6x^2 - 18 \text{ m x} + 12 \text{ m}^2 = 0$

$$\Rightarrow$$
 $(x-2m)(x-m)=0$

$$\Rightarrow$$
 x = m or 2 m

At
$$x = m$$
, $f'(x) = 12m - 18m = -ve \implies x = m$ is a maxima

At
$$x = 2$$
 m, $f''(x) = 24m - 18m = + ve \implies x = 2m$ is manimum

$$p = m \text{ and } q = 2 m$$

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Given
$$p^2 = q \implies m^2 = 2 m \implies m^2 - 2 m = 0$$

$$\Rightarrow$$
 m = 0, 2

$$\Rightarrow m=2 \text{ as } m>0$$

22. y = 2 + x (i)

$$y = 2 - x \quad (ii)$$

$$x = 2$$
 (iii),

y₁ is the value of y from (i)

and y₂ is the value of y from (ii)

Required Area =
$$\int_{0}^{2} (y_1 - y_2) dx$$



1 m

$$= \int_{0}^{2} \{(2+x)-(2-x)\} dx$$
 correct shading 1 m

$$= 2 \int_{0}^{2} x \, dx = 2 \left[\frac{x^{2}}{2} \right]_{0}^{2}$$
¹/₂ m

$$= 4 \text{ sq. units}$$

23. Let the equation of line be y = mx + c

 $1\frac{1}{2}$ m

the line is at unit distance from the origin

i.e.
$$\left| \frac{0+c}{\sqrt{1+m^2}} \right| = 1 \implies c = \sqrt{1+m^2}$$

$$y = m x + \sqrt{1 + m^2}$$
(i)

$$\frac{\mathrm{dy}}{\mathrm{dx}} = \mathrm{m}$$

$$\therefore y = x \frac{dy}{dx} + \sqrt{1 + \left(\frac{dy}{dx}\right)^2}$$

OR

$$\frac{dy}{dx} = \frac{x^2 + 3y^2}{2 xy} = \frac{1 + 3\left(\frac{y}{x}\right)^2}{2\left(\frac{y}{x}\right)} \dots (i)$$
1 m

Differential equation is homogeneous

Put y = v x

$$\Rightarrow \frac{dy}{dx} = v + x \frac{dv}{dx}$$

$$\therefore v + x \frac{dv}{dx} = \frac{1 + 3v^2}{2v}$$

$$\Rightarrow x \frac{dv}{dx} = \frac{1+v^2}{2v}$$

$$\Rightarrow \int \left(\frac{2v}{1+v^2}\right) dv = \int \frac{dx}{x}$$

$$\Rightarrow \log \left| 1 + v^2 \right| = \log \left| x \right| + \log c$$

$$\Rightarrow 1 + v^2 = c x$$

$$\Rightarrow 1 + \left(\frac{y}{x}\right)^2 = c x \text{ or } x^2 + y^2 = c x^3$$



Equation of plane passing through (1, 0, 0) 24.

$$a(x-1)+b(y-0)+c(z-0)=0$$

or
$$a x + b y + c z - a = 0$$
(i)

Plane (i) passes through (0, 1, 0)

$$b-a = 0 \dots (ii)$$

Angle between plane (i) and plane x + y = 3 is $\frac{\pi}{4}$ $\frac{1}{2}$ m

$$\therefore \quad \cos\frac{\pi}{4} = \frac{a+b}{\sqrt{a^2+b^2+c^2}} \frac{1}{\sqrt{2}}$$

$$\Rightarrow \frac{1}{\sqrt{2}} = \frac{a+b}{\sqrt{a^2+b^2+c^2}} = \frac{a+b}{\sqrt{a^2+b^2+c^2}}$$

$$\Rightarrow \overline{\sqrt{2}} = \overline{\sqrt{a^2 + b^2 + c^2}} \sqrt{2}$$
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$$\Rightarrow a + b = \sqrt{a^2 + b^2 + c^2}$$

$$\Rightarrow$$
 2a = $\sqrt{2a^2 + c^2}$ (using ii)

Equation (i) becomes

$$a(x-1) + a(y-0) \pm \sqrt{2} a(z-0) = 0$$

$$\Rightarrow x + y \pm \sqrt{2} z - 1 = 0$$

D.R's of the normal is
$$1, 1, \pm \sqrt{2}$$

Let E_1 , E_2 and E be the events such that 25.

E₁: students residing in hostel

 $1\frac{1}{2}$ m E₂: students residing outside hostel

E₃: students getting 'A' grade

$$P(E_1) = \frac{40}{100}, \quad P(E/E_1) = \frac{50}{100}$$

$$P(E_2) = \frac{60}{100}, P(E/E_2) = \frac{30}{100}$$

$$P(E_{1}/E) = \frac{P(E_{1}) \cdot P(E/E_{1})}{P(E_{1}) \cdot P(E/E_{1}) + P(E_{2}) P(E/E_{2})}$$
1 m

$$= \frac{\frac{40}{100} \times \frac{50}{100}}{\frac{40}{100} \times \frac{50}{100} + \frac{30}{100} \times \frac{60}{100}}$$
1 m

$$=\frac{10}{19}$$

Let x be the man helpers and y be the woman helpers 26.

Pay roll:
$$Z = 225 x + 200 y$$

Subject to constraints:

$$x + y \le 10$$

$$3x + 4y \ge 34$$

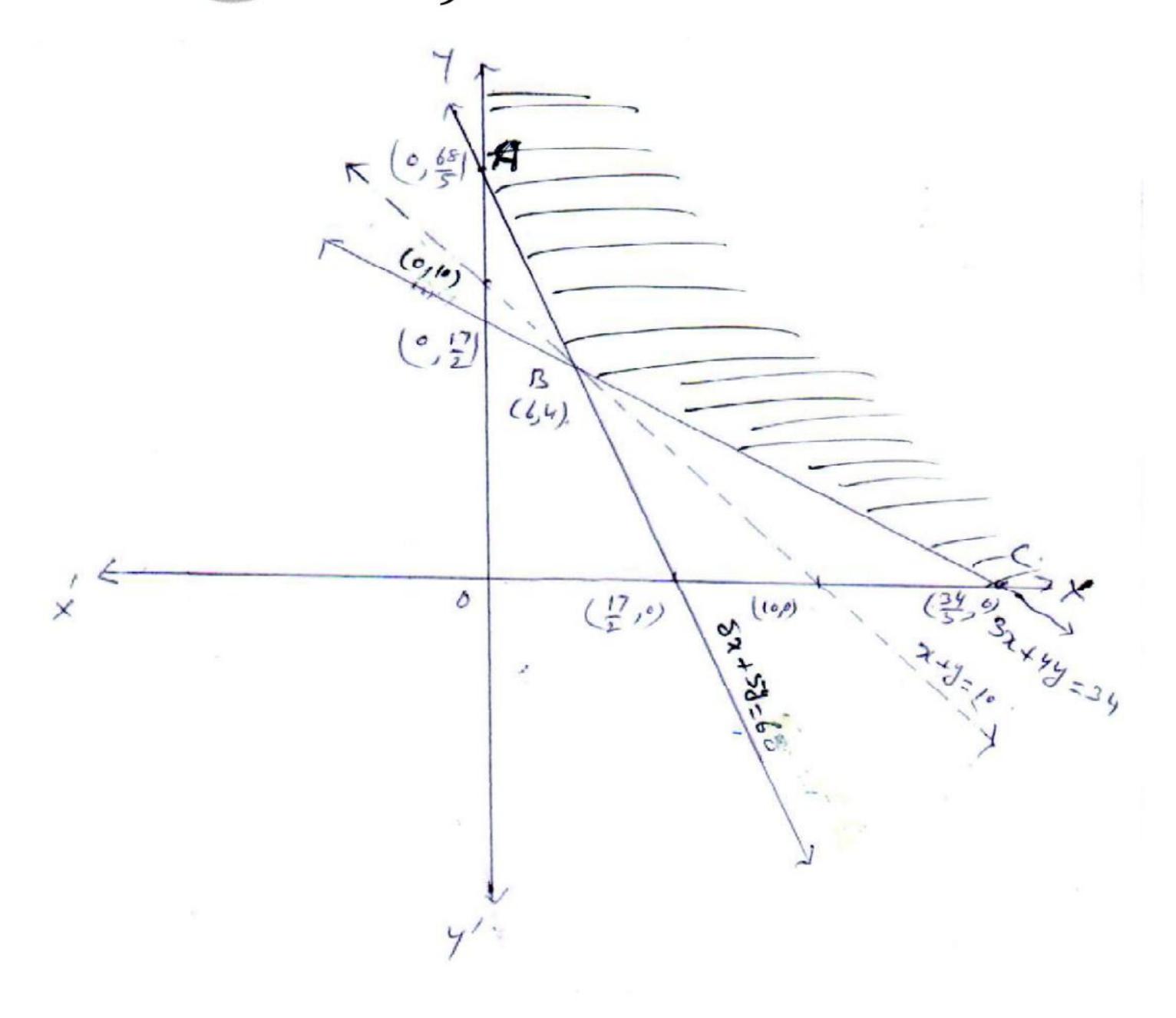
$$8x + 5y \ge 68$$

$$x \ge 0, y \ge 0$$

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 $2 \, \mathrm{m}$

 $2 \, \mathrm{m}$ correct graph:





At A
$$\left(0, \frac{68}{5}\right)$$
, Z (A) = Rs. 2720

At B (6, 4), Z(B) = Rs. 2150 Minimum

 $\frac{1}{2}$ m

At
$$C\left(\frac{34}{5}, 0\right)$$
, $Z(C) = Rs. 2550$

Minimum Z = Rs. 2150 at (6, 4)

 $\frac{1}{2}$ m

[Feasible region is unbounded and to check minimum

of Z, 225x + 200y < 2150

corresponding line is outside of the shaded region]

