# AIEEE-2011 (Set - Q)

### IMPORTANT INSTRUCTIONS

- 1. Immediately fill in the particulars on this page of the Test Booklet with Blue/Black Ball Point Pen. Use of Pencil is strictly prohibited.
- 2. The Answer Sheet is kept inside the Test Booklet. When you are directed to open the Test Booklet, take out the Answer Sheet and fill in the particulars carefully.
- 3. The test is of 3 hours duration.
- 4. The Test Booklet consists of 90 questions. The maximum marks are 360.
- 5. There are three parts in the question paper A, B, C consisting of Physics, Mathematics, Chemistry having 30 questions in each part of equal weight age. Each question is allotted 4(four) marks for each correct response.
- 6. Candidates will be awarded marks as stated above in instruction No. 5 for correct response of each question <sup>1</sup>/<sub>4</sub> (one fourth) marks will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer sheet.
- 7. There is only one correct response for each question. Filling up more than one response in each question will be treated as wrong response and marks for wrong response will be deducted accordingly as per instruction 6 above.
- 8. Use Blue/Black Ball Point Pen only for writing particulars/marking responses on Side-1 and Side-2 of the Answer Sheet. Use of pencil is strictly prohibited.
- 9. No candidate is allowed to carry any textual material, printed or written, bits of papers, pager, mobile phone, any electronic device, etc., except the Admit Card inside the examination hall/room.
- 10. Rough work is to be done on the space provided for this purpose in the Test Booklet only. This space is given at the bottom of each page and in 3 pages (Pages 21 23) at the end of the booklet.
- 11. On completion of the test, the candidate must hand over the Answer Sheet to the Invigilator on duty in the Room/Hall. However, the candidates are allowed to take away this Test Booklet with them.
- 12. The CODE for this Booklet is Q. Make sure that the CODE printed on Side-2 of the Answer Sheet is the same as that on this booklet. In case of discrepancy, the candidate should immediately report the matter to the Invigilator for replacement of both the Test Booklet and the Answer Sheet.
- 13. Do not fold or make any stray marks on the Answer Sheet.



# PART A: PHYSICS

1.	This represents a	ement y(x,t) of a wave		
	(1) wave moving in – x	direction with speed $\sqrt{\frac{b}{a}}$	(2) standing wave of fr	equency √b
	(3) standing wave of fre	equency $\frac{1}{\sqrt{b}}$	(4) wave moving in + x	direction with $\sqrt{\frac{a}{b}}$
2.	Main scale reading: 0 Circular scale reading Given that 1 mm on ma The diameter of wire fr	: 52 divisions ain scale corresponds to om the above date is :	100 divisions of the circu	ular scale.
	(1) 0.052 cm	(2) 0.026 cm	(3) 0.005 cm	(4) 0.52 cm
3.	has mass m and radiu		be a perfect uniform ci	a frictionless bearing. The pulley rcular disc, the acceleration of the
	(1) g	(2) $\frac{2}{3}$ g	(3) $\frac{9}{3}$	(4) $\frac{3}{2}$ g
4.	Work done in increasing the size of a soap bubble from a radius of 3 cm to 5 cm is nearly (Surface tension of soap solution = $0.03 \text{ Nm}^{-1}$ ):			
	(1) 0.2π mJ	(2) $2\pi$ mJ	(3) $0.4 \text{ mJ}$	(4) $4\pi$ mJ
5.	A thin horizontal circular disc is rotating about a vertical axis passing through its centre. An insect is at rest at a point near the rim of the disc. The insect now moves along a diameter of the disc to reach its other end. During the journey of the insect, the angular speed of the disc:  (1) continuously decreases  (2) continuously increases  (3) first increases and then decreases  (4) remains unchanged			
6.	x-axis. Their mean po		stance $X_0(X_0 > A)$ . If	tude A and frequency ⊚ along the the maximum separation between
		15. <del></del> 10	TT.	π
	(1) $\frac{\pi}{3}$	(2) $\frac{\pi}{4}$	(3) $\frac{\pi}{6}$	$(4) \frac{\pi}{2}$
7.	Two bodies of masses m and 4 m are placed at a distance r. The gravitational potential at a point on the line joining them where the gravitational field is zero is:			
	(1) $-\frac{4Gm}{r}$	$(2) - \frac{6Gm}{r}$	(3) $-\frac{9Gm}{r}$	(4) zero
8.	initially a distance d(co	d << 1) apart because of constant rate. As a resul	their mutual repulsion.	o massless strings of length I are The charge begins to leak from each other with a velocity v. Then
	as a function of distant (1) $v \propto x^{-1}$	ce x between them, (2) $V \propto X^{1/2}$	(3) v ∝ x	(4) $V \propto X^{-1/2}$



- 9. A boat is moving due east in a region where the earth's magnetic field is 5.0 × 10<sup>-5</sup> NA<sup>-1</sup>m<sup>-1</sup> due north and horizontal. The boat carries a vertical aerial 2m long. If the speed of the boat is 1.50 ms<sup>-1</sup>, the magnitude of the induced emf in the wire of aerial is:

  (1) 0.75 mV
  (2) 0.50 mV
  (3) 0.15 mV
  (4) 1 mV

  10. An object, moving with a speed of 6.25 m/s, is decelerated at a rate given by:

  dv/dt = -2.5√v
  where v is the instantaneous speed. The time taken by the object, to come to rest, would be:
  (1) 2 s
  (2) 4 s
  (3) 8 s
  (4) 1 s
- 11. A fully charged capacitor C with initial charge  $q_0$  is connected to a coil of self inductance L at t=0. The time at which the energy is stored equally between the electric and the magnetic field is :

(2)  $2\pi\sqrt{LC}$  (3)  $\sqrt{LC}$  (4)  $\pi\sqrt{LC}$ 

- 12. Let the x z plane be the boundary between two transparent media. Medium 1 in  $z \ge 0$  has a refractive index of  $\sqrt{2}$  and medium 2 with z < 0 has a refractive index of  $\sqrt{3}$ . A ray of light in medium 1 given by the vector  $\vec{A} = 6\sqrt{3}\,\hat{i} + 8\sqrt{3}\,\hat{j} 10\hat{k}$  is incident on the plane of separation. The angle of refraction in
  - medium 2 is (1)  $45^{\circ}$  (2)  $60^{\circ}$  (3)  $75^{\circ}$  (4)  $30^{\circ}$

 $(1) \frac{\pi}{4}\sqrt{LC}$ 

- 13. A current I flows in an infinitely long wire with cross section in the form of a semicircular ring of radius R. The magnitude of the magnetic induction along its axis is
  - (1)  $\frac{\mu_0 I}{2\pi^2 R}$  (2)  $\frac{\mu_0 I}{2\pi R}$  (3)  $\frac{\mu_0 I}{4\pi^2 R}$  (4)  $\frac{\mu_0 I}{\pi^2 R}$
- 14. A thermally insulated vessel contains an ideal gas of molecular mass M and ratio of specific heats  $\gamma$ . It is moving with speed  $\upsilon$  and is suddenly brought to rest. Assuming no heat is lost to the surroundings, its temperature increases by :
  - $(1) \ \frac{\left(\gamma 1\right)}{2\gamma R} M \upsilon^2 K \qquad \qquad (2) \ \frac{\gamma M \upsilon^2}{2R} K \qquad \qquad (3) \ \frac{\left(\gamma 1\right)}{2R} M \upsilon^2 K \qquad \qquad (4) \ \frac{\left(\gamma 1\right)}{2\left(\gamma + 1\right)R} M \upsilon^2 K$
- 15. A mass M, attached to a horizontal spring, executes S.H.M. with amplitude  $A_1$ . When the mass M passes through its mean position then a smaller mass m is placed over it and both of them move together with amplitude  $A_2$ . The ratio of  $\left(\frac{A_1}{A_2}\right)$  is :
  - (1)  $\frac{M+m}{M}$  (2)  $\left(\frac{M}{M+m}\right)^{1/2}$  (3)  $\left(\frac{M+m}{M}\right)^{1/2}$  (4)  $\frac{M}{M+m}$
- 16. Water is flowing continuously from a tap having an internal diameter  $8 \times 10^{-3}$  m. The water velocity as it leaves the tap is  $0.4 \text{ ms}^{-1}$ . The diameter of the water stream at a distance  $2 \times 10^{-1}$  m below the lap is close to:
  - $(1) \quad 7.5 \times 10^{-3} \, \text{m} \qquad \qquad (2) \quad 9.6 \times 10^{-3} \, \text{m} \qquad \qquad (3) \quad 3.6 \times 10^{-3} \, \text{m} \qquad \qquad (4) \quad 5.0 \times 10^{-3} \, \text{m}$



17. This question has Statement – 1 and Statement – 2. Of the four choices given after the statements, choose the one that best describes the two statements.

**Statement-1**: Sky wave signals are used for long distance radio communication. These signals are in general, less stable than ground wave signals.

**Statement-2**: The state of ionosphere varies from hour to hour, day to day and season to season.

- (1) Statement-1 is true, Statement-2 is true; Statement-2 is the correct explanation of Statement-1.
- (2) Statement-1 is true, Statement-2 is true; Statement-2 is not the correct explanation of Statement-1.
- (3) Statement-1 is false, Statement-2 is true.
- (4) Statement-1 is true, Statement-2 is false.
- Three perfect gases at absolute temperatures  $T_1$ ,  $T_2$  and  $T_3$  are mixed. The masses of molecules are  $m_1$ , 18. m<sub>2</sub> and m<sub>3</sub> and the number of molecules are n<sub>1</sub>, n<sub>2</sub> and n<sub>3</sub> respectively. Assuming no loss of energy, the final temperature of the mixture is:

$$(1) \ \frac{n_1T_1+n_2T_2+n_3T_3}{n_1+n_2+n_3} \quad (2) \ \frac{n_1T_1+n_2T_2^2+n_3T_3^2}{n_1T_1+n_2T_2+n_3T_3} \quad (3) \ \frac{n_1^2T_1^2+n_2^2T_2^2+n_3^2T_3^2}{n_1T_1+n_2T_2+n_3T_3} \quad (4) \ \frac{\left(T_1+T_2+T_3\right)}{3}$$

$$(3) \ \frac{n_1^2T_1^2+n_2^2T_2^2+n_3^2T_3^2}{n_1T_1+n_2T_2+n_3T_3} \ (4) \ \frac{\left(T_1+T_2+T_3\right)}{3}$$

- A pulley of radius 2 m is rotated about its axis by a force  $F = (20t 5t^2)$  Newton (where t is measured in 19. seconds) applied tangentially. If the moment of inertia of the pulley about its axis of rotation made by the pulley before its direction of motion if reversed, is:
  - (1) more than 3 but less than 6
- (2) more than 6 but less than 9

(3) more than 9

- (4) less than 3
- 20. A resistor 'R' and 2μF capacitor in series is connected through a switch to 200 V direct supply. Across the capacitor is a neon bulb that lights up at 120 V. Calculate the value of R to make the bulb light up 5 s after the switch has been closed. ( $log_{10} 2.5 = 0.4$ )
  - (1)  $1.7 \times 10^5 \Omega$

- (2)  $2.7 \times 10^{8} \Omega$  (3)  $3.3 \times 10^{7} \Omega$  (4)  $1.3 \times 10^{4} \Omega$
- A Carnot engine operating between temperatures  $T_1$  and  $T_2$  has efficiency  $\frac{1}{6}$ . When  $T_2$  is lowered by 62 21.

K, its efficiency increases to  $\frac{1}{3}$ . Then T<sub>1</sub> and T<sub>2</sub> are, respectively:

- (1) 372 K and 330 K (2) 330 K and 268 K (3) 310 K and 248 K (4) 372 K and 310 K
- 22. If a wire is stretched to make it 0.1% longer, its resistance will:
  - (1) increase by 0.2% (2) decrease by 0.2% (3) decrease by 0.05% (4) increases by 0.05%
- 23. Direction:

The question has a paragraph followed by two statements, Statement -1 and statement -2. Of the given four alternatives after the statements, choose the one that describes the statements.

A thin air film is formed by putting the convex surface of a plane – convex lens over a plane glass plate. With monochromatic light, this film gives an interference pattern due to light reflected from the top (convex) surface and the bottom (glass plate) surface of the film.

**Statement-1**: When light reflects from the air-glass plate interface, the reflected wave suffers a phase change of  $\pi$ .

**Statement-2**: The centre of the interference pattern is dark.

- (1) Statement-1 is true, Statement-2 is true; Statement-2 is the correct explanation of Statement-1.
- (2) Statement-1 is true, Statement-2 is true; Statement-2 is not the correct explanation of Statement-1.
- (3) Statement-1 is false, Statement-2 is true.
- (4) Statement-1 is true, Statement-2 is false.



24.	A car is fitted with a convex side-view mirror of focal length 20cm. A second car 2.8 m behind the first car is overtaking the first car at relative speed of 15 m/s. The speed of the image of the second car as seen in the mirror of the first one is:				
	(1) $\frac{1}{15}$ m/s	(2) 10m/s	(3) 15m/s	(4) $\frac{1}{10}$ m/s	
25.	Energy required for (1) 36.3 eV	or the electron excitation i	n Li <sup>++</sup> from the first to the		
26.	• 100 Annual Control of the Control	1000	**************************************	by $\phi = \alpha \rho^2 + b$ where r is the	distance

A water fountain on the ground sprinkles water all around it. If the speed of water coming out of the fountain is v, the total area around the fountain that gets wet is:
v<sup>4</sup>
π v<sup>4</sup>
v<sup>2</sup>
v<sup>4</sup>

(1)  $\pi \frac{v^4}{g^2}$  (2)  $\frac{\pi}{2} \frac{v^4}{g^2}$  (3)  $\pi \frac{v^2}{g^2}$  (4)  $\pi \frac{v^4}{g}$ 

28. 100g of water is heated from 30°C to 50°C. Ignoring the slight expansion of the water, the change in its internal energy is (specific heat of water is 4148 J/kg/K):

(1) 8.4 kJ

(2) 84 kJ

(3) 2.1 kJ

(4) 4.2 kJ

29. The half life of a radioactive substance is 20 minutes. The approximate time interval  $(t_2 - t_1)$  between the time  $t_2$  when  $\frac{2}{3}$  of it has decayed and time  $t_1$  and  $\frac{1}{3}$  of it had decayed is :

(1) 14 min (2) 20 min (3) 28 min (4) 7 min

30. This question has Statement – 1 and Statement – 2. Of the four choices given after the statements, choose the one that best describes the two statements.

**Statement-1**: A metallic surface is irradiated by a monochromatic light of frequency  $v > v_0$  (the threshold frequency). The maximum kinetic energy and the stopping potential are  $K_{max}$  and  $V_0$  respectively. If the frequency incident on the surface doubled, both the  $K_{max}$  and  $V_0$  are also doubled.

**Statement-2**: The maximum kinetic energy and the stopping potential of photoelectrons emitted from a surface are linearly dependent on the frequency of incident light.

(1) Statement-1 is true, Statement-2 is true; Statement-2 is the correct explanation of Statement-1.

(2) Statement-1 is true, Statement-2 is true; Statement-2 is not the correct explanation of Statement-1.

(3) Statement-1 is false, Statement-2 is true.

(4) Statement-1 is true, Statement-2 is false.



### PART B: MATHEMATICS

31. The lines  $L_1: y-x=0$  and  $L_2: 2x+y=0$  intersect the line  $L_3: y+2=0$  at P and Q respectively. The bisector of the acute angle between  $L_1$  and  $L_2$  intersect  $L_3$  at R.

Statement – 1 : The ratio PR:RQ equals  $2\sqrt{2}:\sqrt{5}$ .

Statement -2: In any triangle, bisector of an angle divides the triangle into two similar triangles.

- (1) Statement 1 is true, Statement 2 is true; Statement 2 is not a correct explanation for Statement
- (2) Statement 1 is true, Statement 2 is false.
- (3) Statement 1 is false, Statement 2 is true.
- (4) Statement 1 is true, Statement 2 is true; Statement 2 is a correct explanation for Statement 1
- If  $A = \sin^2 x + \cos^4 x$ , then for all real x 32.
- (1)  $\frac{13}{16} \le A \le 1$  (2)  $1 \le A \le 2$  (3)  $\frac{3}{4} \le A \le \frac{13}{16}$  (4)  $\frac{3}{4} \le A \le 1$
- The coefficient of  $x^7$  in the expansion of  $(1-x-x^2+x^3)^6$  is 33.
  - (1) 132
- (2) -144
- (3)132
- (4) 144

- 34.
- (1) equals  $\sqrt{2}$  (2) equals  $-\sqrt{2}$  (3) equals  $\frac{1}{\sqrt{2}}$  (4) does not exist
- The number of ways of distributing 10 identical balls in 4 distinct boxes such that no 35. Statement – 1 : box is empty is <sup>9</sup>C<sub>3</sub>

Statement -2: The number of ways of choosing any 3 places from 9 different places is  ${}^9C_3$ .

- (1) Statement 1 is true, Statement 2 is true; Statement 2 is not a correct explanation for Statement
- (2) Statement 1 is true, Statement 2 is false.
- (3) Statement 1 is false, Statement 2 is true.
- (4) Statement 1 is true, Statement 2 is true; Statement 2 is a correct explanation for Statement 1
- $\frac{d^2x}{dv^2}$  equals

$$(1) - \left(\frac{d^2y}{dx^2}\right)^{-1} \left(\frac{dy}{dx}\right)^{-3} \qquad (2) \left(\frac{d^2y}{dx^2}\right) \left(\frac{dy}{dx}\right)^{-2} \qquad \qquad (3) - \left(\frac{d^2y}{dx^2}\right) \left(\frac{dy}{dx}\right)^{-3}$$

$$(2) \left(\frac{d^2y}{dx^2}\right) \left(\frac{dy}{dx}\right)^{-2}$$

$$(3) - \left(\frac{d^2y}{dx^2}\right) \left(\frac{dy}{dx}\right)^{-3}$$

$$(4) \left( \frac{d^2y}{dx^2} \right)^{-1}$$



37.	If $\frac{dy}{dx} = y + 3 >$	If $\frac{dy}{dx} = y + 3 > 0$ and $y(0) = 2$ , then $y(\ln 2)$ is equal to				
	(1) 5	(2) 13	(3) -2	(4) 7		

38. Let R be the set of real numbers

Statement -1:  $A = \{(x,y) \in R \times R : y - x \text{ is an integer}\}$  is an equivalence relation on R.

 $Statement-2 \quad : \quad B = \left\{ \left( x,y \right) \in R \times R : x = \alpha y \text{ for some rational number } \alpha \right\} \text{ is an equivalence relation on } a \in \left\{ \left( x,y \right) \in R \times R : x = \alpha y \text{ for some rational number } \alpha \right\}$ 

- (1) Statement 1 is true, Statement 2 is true; Statement 2 is not a correct explanation for Statement -1
- (2) Statement 1 is true, Statement 2 is false.
- (3) Statement 1 is false, Statement– 2 is true.
- (4) Statement 1 is true, Statement 2 is true; Statement 2 is a correct explanation for Statement 1
- The value of  $\int_{0}^{1} \frac{8\log(1+x)}{1+x^2} dx$  is 39.
  - (1)  $\frac{\pi}{8} \log 2$  (2)  $\frac{\pi}{2} \log 2$
- (3)  $\log 2$  (4)  $\pi \log 2$
- Let  $\alpha$ ,  $\beta$  be real and z be a complex number. If  $z^2 + \alpha z + \beta = 0$  has two distinct roots on the line 40. Rez = 1, then it is necessary that
  - (1)  $\beta \in (-1, 0)$  (2)  $|\beta| = 1$
- (3)  $\beta \in (1, \infty)$  (4)  $\beta \in (0, 1)$
- Consider 5 independent Bernoulli's trials each with probability of success p. If the probability of at least 41. one failure is greater than or equal to  $\frac{31}{32}$ , then p lies in the interval
  - (1)  $\left(\frac{3}{4}, \frac{11}{12}\right]$  (2)  $\left[0, \frac{1}{2}\right]$  (3)  $\left(\frac{11}{12}, 1\right]$  (4)  $\left(\frac{1}{2}, \frac{3}{4}\right]$

- 42. A man saves Rs. 200 in each of the first three months of his service. In each of the subsequent months his saving increases by Rs. 40 more than the saving of immediately previous month. His total saving from the start of service will be Rs. 11040 after
  - (1) 19 months
- (2) 20 months
- (3) 21 months
- (4) 18 months

- The domain of the function  $f(x) = \frac{1}{\sqrt{|x|-x}}$  is 43.
  - $(1) (0, \infty)$
- $(2) \left(-\infty, 0\right)$
- $(3) \left(-\infty, \infty\right) \left\{0\right\} \qquad (4) \left(-\infty, \infty\right)$
- If the angle between the line  $x = \frac{y-1}{2} = \frac{z-3}{\lambda}$  and the plane x + 2y + 3z = 4 is  $\cos^{-1}\left(\sqrt{\frac{5}{14}}\right)$ , then  $\lambda$ 
  - equals
  - $(1) \frac{3}{2}$
- (2)  $\frac{2}{5}$
- (3)  $\frac{5}{3}$



- 45. If  $\vec{a} = \frac{1}{\sqrt{10}} \left( 3\hat{i} + \hat{k} \right)$  and  $\vec{b} = \frac{1}{7} \left( 2\hat{i} + 3\hat{j} 6\hat{k} \right)$ , then the value of  $\left( 2\vec{a} \vec{b} \right) \cdot \left[ \left( \vec{a} \times \vec{b} \right) \times \left( \vec{a} + 2\vec{b} \right) \right]$  is (1) -3 (2) 5 (3) 3 (4) -5
- Equation of the ellipse whose axes are the axes of coordinates and which passes through the point (-3,1) and has eccentricity  $\sqrt{\frac{2}{5}}$  is
  - $(1) \ 5x^2 + 3y^2 48 = 0 \quad (2) \ 3x^2 + 5y^2 15 = 0 \quad (3) \ 5x^2 + 3y^2 32 = 0 \quad (4) \ 3x^2 + 5y^2 32 = 0$
- Let I be the purchase value of an equipment and V(t) be the value after it has been used for t years. The value V(t) depreciates at a rate given by differential equation  $\frac{dV(t)}{dt} = -k(T-t)$ , where k > 0 is a constant and T is the total life in years of the equipment. Then the scrap value V(T) of the equipment is
  - (1)  $I \frac{kT^2}{2}$  (2)  $I \frac{k(T-t)^2}{2}$  (3)  $e^{-kT}$  (4)  $T^2 \frac{1}{k}$
- 48. The vector  $\vec{a}$  and  $\vec{b}$  are not perpendicular and  $\vec{c}$  and  $\vec{d}$  are two vectors satisfying:  $\vec{b} \times \vec{c} = \vec{b} \times \vec{d}$  and  $\vec{a} \cdot \vec{d} = 0$ . Then the vector  $\vec{d}$  is equal to
  - $(1) \ \vec{c} + \left(\frac{\vec{a}.\vec{c}}{\vec{a}.\vec{b}}\right) \vec{b} \qquad \qquad (2) \ \vec{b} + \left(\frac{\vec{b}.\vec{c}}{\vec{a}.\vec{b}}\right) \vec{c} \qquad \qquad (3) \ \vec{c} \left(\frac{\vec{a}.\vec{c}}{\vec{a}.\vec{b}}\right) \vec{b} \qquad \qquad (4) \ \vec{b} \left(\frac{\vec{b}.\vec{c}}{\vec{a}.\vec{b}}\right) \vec{c}$
- 49. The two circles  $x^2 + y^2 = ax$  and  $x^2 + y^2 = c^2(c > 0)$  touch each other if

  (1) |a| = c (2) a = 2c (3) |a| = 2c (4) 2|a| = c
- If C and D are two events such that  $C \subset D$  and  $P(D) \neq 0$ , then the correct statement among the following is  $(1) \ P(C \mid D) \geq P(C) \qquad (2) \ P(C \mid D) < P(C) \qquad (3) \ P(C \mid D) = \frac{P(D)}{P(C)} \qquad (4) \ P(C \mid D) = P(C)$
- 51. The number of values of k for which the linear equations 4x + ky + 2z = 0; kx + 4y + z = 0; 2x + 2y + z = 0 possess a non-zero solution is
- (1) 2 (2) 1 (3) zero (4) 3
- 52. Consider the following statements
  - P: Suman is brilliant Q: Suman is rich
  - R : Suman is honest

The negation of the statement "Suman is brilliant and dishonest if and only if Suman is rich" can be expressed as

- $(1) \sim (Q \leftrightarrow (P \land \sim R)) \quad (2) \sim Q \leftrightarrow \sim P \land R \qquad (3) \sim (P \land \sim R) \leftrightarrow Q \qquad (4) \sim P \land (Q \leftrightarrow \sim R)$
- 53. The shortest distance between line y x = 1 and curve  $x = y^2$  is
  - (1)  $\frac{3\sqrt{2}}{8}$  (2)  $\frac{8}{3\sqrt{2}}$  (3)  $\frac{4}{\sqrt{3}}$  (4)  $\frac{\sqrt{3}}{4}$



- 54. If the mean deviation about the median of the numbers a, 2a, ..., 50a is 50, then |a| equals
  - (1) 3

(2) 4

- (3)5
- (4) 2
- Statement -1: The point A(1, 0, 7) is the mirror image of the point B(1, 6, 3) in the line 55.  $\frac{x}{1} = \frac{y-1}{2} = \frac{z-2}{2}$ .

The line:  $\frac{x}{1} = \frac{y-1}{2} = \frac{z-2}{3}$  bisects the line segment joining A(1, 0, 7) and B(1, 6, 3).

- (1) Statement 1 is true, Statement–2 is true; Statement–2 is not a correct explanation for Statement 1
- (2) Statement 1 is true, Statement 2 is false.
- (3) Statement 1 is false, Statement 2 is true.
- (4) Statement − 1 is true, Statement − 2 is true; Statement − 2 is a correct explanation for Statement − 1
- 56. Let A and B be two symmetric matrices of order 3.

Statement -1: A(BA) and (AB)A are symmetric matrices.

Statement – 2 : AB is symmetric matrix if matrix multiplication of A and B is commutative.

- (1) Statement 1 is true, Statement 2 is true; Statement 2 is not a correct explanation for Statement -1
- (2) Statement 1 is true, Statement 2 is false.
- (3) Statement 1 is false, Statement 2 is true.
- (4) Statement − 1 is true, Statement − 2 is true; Statement − 2 is a correct explanation for Statement − 1
- If  $\omega(\neq 1)$  is a cube root of unity, and  $(1+\omega)^7=A+B\omega$ . Then (A,B) equals 57.
  - (1)(1,1)
- (2)(1,0)
- (3) (-1, 1) (4) (0, 1)
- The value of p and q for which the function  $f\left(x\right) = \begin{cases} \frac{sin(p+1)x + sinx}{x} &, & x < 0 \\ q &, & x = 0 \\ \frac{\sqrt{x + x^2} \sqrt{x}}{\sqrt{3/2}} &, & x > 0 \end{cases}$ 58.

is continuous for all x in R, is

- (1)  $p = \frac{5}{2}$ ,  $q = \frac{1}{2}$  (2)  $p = -\frac{3}{2}$ ,  $q = \frac{1}{2}$  (3)  $p = \frac{1}{2}$ ,  $q = \frac{3}{2}$
- The area of the region enclosed by the curves y = x, x = e,  $y = \frac{1}{x}$  and the positive x-axis is 59.

- (1) 1 square units (2)  $\frac{3}{2}$  square units (3)  $\frac{5}{2}$  square units (4)  $\frac{1}{2}$  square units
- For  $x \in \left(0, \frac{5\pi}{2}\right)$ , define  $f(x) = \int_{0}^{x} \sqrt{t} \sin t \, dt$ . Then f has 60.
  - (1) local minimum at  $\pi$  and  $2\pi$
  - (2) local minimum at  $\pi$  and local maximum at  $2\pi$
  - (3) local maximum at  $\pi$  and local minimum at  $2\pi$
  - (4) local maximum at  $\pi$  and  $2\pi$



# PART C: CHEMISTRY

61.	Among the following th (1) SnCl <sub>2</sub>	e maximum covalent cha (2) AICI <sub>3</sub>	racter is shown by the co (3) MgCl <sub>2</sub>	ompound : (4) FeCl <sub>2</sub>
62.	The presence or abser	ice of hydroxyl group on	which carbon atom of su	ugar differentiates RNA and DNA
	(1) 2 <sup>nd</sup>	(2) 3 <sup>rd</sup>	(3) 4 <sup>th</sup>	(4) 1 <sup>st</sup>
63.	products contains sodiu (1) Trichloromethanol	기가 있다 하는 것 "	another compound. The panol	ing NaOH. The mixture of the other compound is:
64.	Sodium ethoxide has reaction is :	reacted with ethanoyl c	chloride. The compound	d that is produced in the above
		(2) Ethyl chloride	(3) Ethyl ethanoate	(4) Diethyl ether
65.	(1) $p(H_2) = 1$ atm and		(2) $p(H_2)=2$ atm and [	
	(3) $p(H_2) = 2$ atm and	$\left[H^{+}\right] = 2.0 \text{ M}$	(4) $p(H_2)=1$ atm and [	$[H^+] = 2.0 \text{ M}$
66.	The strongest acid amount (1) HCOOH (3) CICH <sub>2</sub> CH <sub>2</sub> CH <sub>2</sub> COC	ongst the following composite	ounds is: (2) $CH_3CH_2CH(CI)CO$ (4) $CH_3COOH$	<sub>2</sub> H
67.	expression:	8 (2)	lectrolyte, $A_x B_y$ is relation $(3)  \alpha = \frac{x + y + 1}{i - 1}$	ed to van't Hoff factor (i) by the $(4) \alpha = \frac{i-1}{(x+y-1)}$
68.	(1) a and b for $Cl_2 < a$ (2) a for $Cl_2 < a$ for $C_2$	and b for $C_2H_6$ $H_6$ but b for $Cl_2 > b$ for $C_2H_6$ but b for $Cl_2 < b$ for $C$	$C_2H_6$	sily liquefied than ethane because
69.		STANDARD OF STANDARD STANDARD STANDARD	re of 0.5 atm. Some of tequilibrium is 0.8 atm, the (3) 0.18 atm	the CO <sub>2</sub> is converted into CO on e value of K is (4) 1.8 atm
70.	Boron cannot form whice (1) BH <sub>4</sub>	ch one of the following ar (2) $B(OH)_4^-$		(4) BF <sub>6</sub> <sup>3-</sup>
71.	<ul><li>(1) The complex is par</li><li>(3) The complex gives</li></ul>	amagnetic white precipitate with sil	$\left[ \text{Cr} \left( \text{NH}_3 \right)_6 \right] \text{Cl}_3 \text{ s wrong } 3$ (2) The complex is an ver nitrate solution and is octahedral in shape	outer orbital complex



72.	added to 4 kg of water	er to prevent it from free		s of ethylene glycol wh $I = 62a \text{ mol}^{-1}$	ich should be
	(1) 204.30g	(2) 400.00 g		(4) 804.32g	
73.	Which one of the folgiven oxides? (1) MgO < K <sub>2</sub> O < Al <sub>2</sub> (3) K <sub>2</sub> O < Na <sub>2</sub> O < A	O <sub>3</sub> < Na <sub>2</sub> O	s the correct sequence (2) Na <sub>2</sub> O < K <sub>2</sub> O < (4) Al <sub>2</sub> O <sub>3</sub> < MgO <		nature of the
74.		the reaction increases		perature. If the temperature (4) 10 times	ature is raised
75.		nt (spin only) of $[NiCl_4]$ (2) 2.83 BM		(4) 1.82 BM	
76.			$O_3^-$ , $NO_2^+$ and $NH_4^+$ are re (3) sp <sup>2</sup> , sp <sup>3</sup> , sp		
77.	<ul> <li>In context of the lanthanoids, which of the following statements is not correct?</li> <li>(1) All the members exhibit +3 oxidation state</li> <li>(2) Because of similar properties the separation of lanthanoids is not easy.</li> <li>(3) Availability of 4f electrons results in the formation of compounds in +4 state for all the members of the series.</li> <li>(4) There is a gradual decrease in the radii of the members with increasing atomic number in the series.</li> </ul>				
78.	alcohol in the solutio	n ?	90	d. What is the mole frac	ction of methyl
	(1) 0.190	(2) 0.086	(3) 0.050	(4) 0.100	
79.	<ul><li>(1) Nitrogen cannot</li><li>(2) Single N- N bond</li><li>(3) N<sub>2</sub>O<sub>4</sub> has two re</li></ul>	l is weaker than the sin sonance structures	gle P – P bond, $NH_3$ to $BiH_3$ in group 15	of the periodic table	
80.		onfiguration of Gd (Aton (2) 4f <sup>4</sup> 5d <sup>4</sup> 6s <sup>2</sup>	nic No : 64 is : (3) 4f <sup>7</sup> 5d <sup>1</sup> 6s <sup>2</sup>	(4) 4f³ 4d⁵ 6s²	
81.	(1) The vapour at 20 (2) At 600°C the ga		f S <sub>8</sub> rings	ounds	
82.	The structure of IF, i		(3) pentagonal bip	yramid (4) square	pyramid



83.	Ozonolysis of an orga presence of :	nic compound gives fo	rmaldehyde as one of	the products. This confirms the
	<ul><li>(1) a vinyl group</li><li>(3) an acetylenic triple I</li></ul>	bond	(2) an isopropyl group (4) two ethylenic double	
84.	A gas absorbs a photor 680 nm, the other is at		two wavelengths. If one	e of the emissions is at
	(1) 325 nm	(2) 743 nm	(3) 518 nm	(4) 1035 nm
85.	Silver Mirror test is give (1) Acetone	en by which one of the fo (2) Formaldehyde	llowing compounds ? (3) Benzophenone	(4) Acetaldehyde
86.	[경우 : [경기 : 10] : [경기 : 10] : [경기 : [경기 : 10] : [경기 : [경기 : [경기 : 10] : [경기 : [경기 : [경기 : 10] : [경기 : [경기 : [경기 : [경기 : [경기 : [] : [] : [] : [] : [] : [] : [] : [		distinguish between phe (3) Neutral FeCl <sub>3</sub>	
87.	Phenol is heated with a reaction is	a solution of mixture of h	KBr and KBrO <sub>3</sub> . The ma	jor product obtained in the above
	(1) 3-Bromophenol	(2) 4-Bromophenol	(3) 2, 4, 6- Tribromoph	nenol (4) 2-Bromophenol
88.		[하님] [2017년 1일		d atom B occupies the face centre is, the formula of the compound is
	(1) AB <sub>2</sub>	(2) A <sub>2</sub> B <sub>3</sub>	(3) A <sub>2</sub> B <sub>5</sub>	(4) A <sub>2</sub> B
89.		volved in the isotherma volume of 100 dm³ at 2	•	f 2 moles of an ideal gas from a
	(1) 35.8J mol <sup>-1</sup> K <sup>-1</sup>	(2) 32.3J mol <sup>-1</sup> K <sup>-1</sup>	(3) 42.3J mol <sup>-1</sup> K <sup>-1</sup>	(4) 38.3J mol <sup>-1</sup> K <sup>-1</sup>
90.	되는 생님은 아이지 않아서 하는데 이 경에 가로워 된 맛있다면 하게 하나 하나 하나 하나 아이라고 있다.	that exhibits tautomerism		
	(1) Lactic acid	(2) 2-Pentanone	(3) Phenol	(4) 2- Butene



### READ THE FOLLOWING INSTRUCTIONS CAREFULLY

- 1. The candidates should fill in the required particulars on the Test Booklet and Answer Sheet (Side–1) with Blue/Black Ball Point Pen.
- 2. For writing/marking particulars on Side-2 of the Answer Sheet, use Blue/Black Ball Point Pen only.
- 3. The candidates should not write their Roll Numbers anywhere else (except in the specified space) on the Test Booklet/Answer Sheet.
- 4. Out of the four options given for each question, only one option is the correct answer.
- 5. For each incorrect response, one-fourth (1/4) of the total marks allotted to the question would be deducted from the total score. No deduction from the total score, however, will be made if no response is indicated for an item in the Answer Sheet.
- 6. Handle the Test Booklet and Answer Sheet with care, as under no circumstances (except for discrepancy in Test Booklet Code and Answer Sheet Code), will another set be provided.
- 7. The candidates are not allowed to do any rough work or writing work on the Answer Sheet. All calculations/writing work are to be done in the space provided for this purpose in the Test Booklet itself, marked 'Space for Rough Work'. This space is given at the bottom of each page and in 4 pages (Pages 20 23) at the end of the booklet.
- 8. On completion of the test, the candidates must hand over the Answer Sheet to the Invigilator on duty in the Room/Hall. However, the candidates are allowed to take away this Test Booklet with them.
- 9. Each candidate must show on demand his/her Admit Card to the Invigilator.
- 10. No candidate, without special permission of the Superintendent or Invigilator, should leave his/her seat.
- 11. The candidates should not leave the Examination Hall without handing over their Answer Sheet to the Invigilator on duty and sign the Attendance Sheet again. Cases where a candidate has not signed the Attendance Sheet a second time will be deemed not to have handed over the Answer Sheet and dealt with as an unfair means case. The candidates are also required to put their left hand THUMB impression in the space provided in the Attendance Sheet.
- 12. Use of Electronic/Manual Calculator and any Electronic Item like mobile phone, pager etc. is prohibited.
- 13. The candidates are governed by all Rules and Regulations of the Board with regard to their conduct in the Examination Hall. All cases of unfair means will be dealt with as per Rules and Regulations of the Board.
- 14. No part of the Test Booklet and Answer Sheet shall be detached under any circumstances.
- 15. Candidates are not allowed to carry any textual material, printed or written, bits of papers, pager, mobile phone, electronic device or any other material except the Admit Card inside the examination hall/room.



## SOLUTIONS

# PART A **PHYSICS**

1.

$$\textbf{Sol.} \qquad \textbf{y}_{(x,t)} = e \ \left( \sqrt{a} \ x + \sqrt{b} \ t \right)^2 \ \textbf{V} = \sqrt{\frac{b}{a}}$$

Wave moving in - ve x -direction.

2.

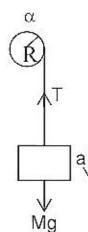
Diameter of wire =  $\frac{1}{100} \times 52 = 0.52$ mm = 0.052cm Sol.

3. Sol.

$$T \times R = I\alpha = \frac{1}{2}MR^2\alpha$$

$$T = \frac{1}{2}Ma$$
  $(a = \alpha R)$  ..... (2)

From (1) and (2) 
$$a = \frac{2g}{3}$$



4.

Sol. 
$$W = T \times \Delta A = T \times 8\pi (r_2^2 - r_1^2) = 0.4\pi mJ$$

5.

Sol.  $\tau = 0$ 

Angular momentum is conserve

$$l_1\omega_1 = l_2\omega_2 \Rightarrow \omega_2 = \frac{l_1\omega_1}{l_2}$$

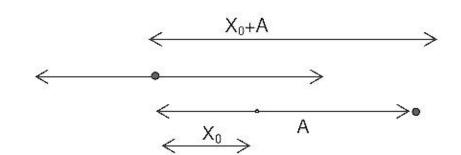
l<sub>2</sub> first decreases and then increases

∴ω first increases and then decreases.

6.

Sol. 
$$\phi_1 = 0$$

$$\phi_2 = \frac{\pi}{2}$$



7.

**Sol.** Position of the null point from mass m, 
$$x = \frac{r}{1 + \sqrt{\frac{4m}{m}}} = \frac{r}{3}$$

$$V = -Gm \left(\frac{3}{r} + \frac{12}{2r}\right) = -9\frac{Gm}{r}$$

At any instant of separation between charges is x. Sol.

equilibrium condition = 
$$K \frac{Q^2}{x^2} = \omega \frac{x}{2\ell}$$

$$\Rightarrow Q^2 = Cx^3$$

$$\Rightarrow 2Q \frac{dQ}{dt} = C3x^2 \frac{dx}{dt}$$

$$\Rightarrow \frac{dx}{dt} \propto \frac{x^{3/2}}{x^2} \propto x^{-1/2}$$

9. 3 Sol. 
$$E = B_H \ell V = 0.15 mV$$

**Sol.** 
$$\frac{dv}{dt} = -2.5\sqrt{v}$$

Integrating the above equation.

$$\Rightarrow 2\sqrt{v} = -2.5t + C$$

at 
$$t = 0, v = 6.25 \Rightarrow C = 5$$

at 
$$v = 0 \Rightarrow t = \frac{5}{2.5} = 2s$$

11.

Charge oscillates simple harmonic motion  $q = q_0 \sin \omega t$ ,  $U = \frac{1}{2} \frac{q^2}{C}$ Sol.

$$q = \frac{q_0}{\sqrt{2}} \Rightarrow \omega t = \frac{\pi}{4}$$

$$\Rightarrow t = \frac{T}{8} = \frac{2\pi}{8} \sqrt{LC} = \frac{\pi}{4} \sqrt{LC}$$

12.

Sol. Normal to the plane is z -axis

$$\cos \theta_1 = \frac{A_z}{A} = \frac{10}{20} = \frac{1}{2}, \theta_1 = 60$$

$$\mu_1 \sin \theta_1 = \mu_2 \sin \theta_2 \Rightarrow \sqrt{2} \times \frac{\sqrt{3}}{2} = \sqrt{3} \sin \theta_2 \Rightarrow \theta_2 = 45^{\circ}$$

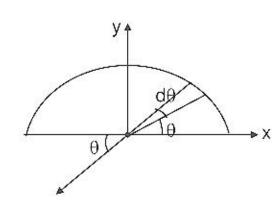
13.

**Sol.** 
$$d\vec{B} = \frac{\mu_0 di}{2\pi R} \left[ -\cos\theta \, \hat{i} - \sin\theta \, \hat{j} \right]$$

$$di = \frac{T}{\pi R} R d\theta$$

$$=\frac{1}{\pi}d\theta$$

$$d\vec{B} = \frac{\mu_0 I}{2\pi^2 R} \left( -\cos\theta \,\hat{i} - \sin\theta \,\hat{j} \right)$$



$$\vec{B} = -\frac{\mu_0 I}{\pi^2 R} \hat{j}$$

14. 3 Sol. 
$$W = \Delta U$$

$$\frac{1}{2}mv^2 = nC_v dT$$

$$=\frac{m}{M}\frac{R}{\gamma-1}dT$$

$$dT = \frac{M(\gamma - 1)v^2}{2B}K$$

Energy of simple harmonic oscillator is constant. Sol.

$$\Rightarrow \frac{1}{2}M\omega^2 A_1^2 = \frac{1}{2}(m+M)\omega^2 A_2^2$$

$$\frac{A_1^2}{A_2^2} = \frac{M+m}{M}$$

$$\therefore \frac{A_1}{A_2} = \sqrt{\frac{M+m}{M}}$$

Equation of continuity Sol.

$$\Rightarrow$$
  $(a \times v)$ top =  $(a \times v)$ bottom

$$v_b^2 - (0.4)^2 = 2 \times 9.8 \times 0.2 [v^2 - u^2 = 2gh \text{ is used}]$$

$$v_b = 2m/s \text{ (nearly)}$$

$$\pi \left[ 8 \times 10^{-3} \right] \times 0.4 = \pi d^2 \times 4$$

$$d\approx 3.6\times 10^{-3} m$$

17.

Since ionospheric properties change with time, these signals are in general less stable than ground wave Sol. signals.

**Sol.** Data 
$$\Rightarrow$$
 n,k,t<sub>1</sub> + n<sub>2</sub>kT<sub>2</sub> + n<sub>3</sub>kT<sub>3</sub> =  $(n_1 + n_2 + n_3)$ kT

$$\therefore T = \frac{n_1 T_1 + n_2 T_2 + n_3 T_3}{n_1 + n_2 + n_3}$$

**Sol.** 
$$r \times F = I \times \alpha$$

$$2(20t - 5t^2) = 10\alpha \Rightarrow \alpha = 4t - t^2$$

$$\frac{d\omega}{dt} = 4t - t^2$$

$$d\omega = \left(4t^2 - t^2\right)dt$$

$$\omega = 2t^2 - \frac{t^3}{3}$$
 (on integration)

$$\omega=0 \Rightarrow t=6s$$



$$\omega = \frac{d\theta}{dt} = 2t^2 - \frac{t^3}{3}$$

$$d\theta = \left(2t^2 - \frac{t^3}{3}\right)dt$$

$$\Rightarrow \theta = \frac{2t^3}{3} - \frac{t^4}{12} \text{ (on integration)}$$

$$\theta \text{ (in 6s)} = 36 \text{ rad}$$

$$\Rightarrow 2\pi n = 36$$

$$n = \frac{36}{2\pi} = 6$$

20. 2
Sol. 
$$V_c = E(1-e^{-t/Rc})$$

$$1-e^{-t/Rc} = \frac{120}{200} = \frac{3}{5}$$

$$\Rightarrow R = \frac{5}{1.84 \times 10^{-6}} = 2.7 \times 10^6 \Omega$$

21. 4

Sol. 
$$\eta_1 = \frac{T_1 - T_2}{T_1} = \frac{1}{6}$$
 $\eta_2 = \frac{T_1 - (T_2 - 62)}{T_1} = \frac{1}{3}$ 
 $\Rightarrow \frac{T_1 - T_2}{T_1} + \frac{62}{T_1} = \frac{1}{3}$ 
 $\frac{1}{6} + \frac{62}{T_1} = \frac{1}{3}$ 
 $\frac{62}{T_1} = \frac{1}{6}$ 
 $\therefore T_1 = 62 \times 6 = 372K$ 
 $\frac{T_1 - T_2}{T_1} = \frac{1}{6}$ 
 $1 - \frac{T_2}{T_1} = \frac{1}{6}$ 
 $\frac{T_2}{372} = \frac{5}{6}$ 
 $\Rightarrow T_2 = 310K$ 

22. 1

Sol. 
$$R \propto \ell^2$$
 (for a given volume)
$$\Rightarrow \frac{\Delta R}{R} \% = \frac{2\Delta \ell}{\ell} \%$$
Thus when wire is stretched by 0.1% resistance increases by 0.2%

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- 23.
- Sol. As light enters from air to glass it suffers a phase change on  $\pi$  and therefore at centre there will be destructive interference.
- 24.
- **Sol.**  $\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$  $-\frac{1}{v^2}\frac{dv}{dt} - \frac{1}{u^2}\frac{du}{dt} = 0$ 
  - $\frac{dv}{dt} = -\frac{v^2}{u^2} \left( \frac{du}{dt} \right)$
  - f = 20 cm
  - $\frac{1}{u} + \frac{1}{-280} = \frac{1}{20}$
  - $\Rightarrow$  v =  $\frac{280}{15}$  cm
  - $v_1 = -\left(\frac{280}{15 \times 280}\right)^2 \times 15$  $=\frac{1}{15}$ m/s
- 25.
- **Sol.**  $E_n = -13.6 \frac{Z^2}{n^2}$ 
  - $E_{L_1}^{++} = -13.6 \times \frac{9}{1} = -122.4 eV$
  - $E_{L_1}^{+++} = -13.6 \times \frac{9}{9} = -13.6 \text{ eV}$
  - $\Delta E = -13.6 (-122.4)$
  - = 108.8 eV
- 26.
- Potential inside  $(\phi) = ar^2 + b$ Sol.

$$\therefore E_r = -\frac{\delta v}{\delta r} = -2ar$$

Electric field inside uniformly charged solid volume varies with 'r'. So charge density is constant  $\phi_{net} = \left(-2ar\right)4\pi r^2 = -8\pi ar^3$ 

$$\sigma \times \frac{4}{\pi} r^3$$

$$-8\pi a r^3 = \frac{\sigma \times \frac{4}{3}\pi r^3}{\varepsilon_0}$$

- $\therefore \sigma = -6a\epsilon_0$
- 27.
- Max. range =  $\frac{u^2}{q}$  i.e.,  $\frac{v^2}{q}$  (radius of circle) Sol.
  - Area occupied =  $\pi \left(\frac{v^2}{g}\right)^2 = \frac{\pi v^4}{g^2}$



**Sol.** 
$$\Delta Q = \Delta U + \Delta W$$
 (ignoring expansion)  $\Delta U = ms\Delta T = 0.1 \times 4.184 \times 20 = 8.368 \text{kJ}$ 

**Sol.** 
$$t_{\frac{1}{2}} = 20$$
 minutes

$$N=N_0e^{-\lambda t_2}-\lambda t_1=ln3$$

$$\frac{2}{3}N_0 = N_0 e^{-\lambda t_2} t_1 = \frac{1}{\lambda} ln3$$

$$\frac{2}{3}N_0 = N_0 e^{-\lambda t_2}$$

$$t_2 = \frac{1}{\lambda} \ln \frac{3}{2}$$

$$t_2 - t_1 = \frac{1}{\lambda} \left[ \ln \frac{3}{2} - \ln 3 \right]$$

$$= \frac{1}{\lambda} \ln \left[ \frac{1}{2} \right] = \frac{0.693}{\lambda}$$
$$= 20 \text{ min}$$

**Sol.** 
$$KE_{max} = h\upsilon - h\upsilon_0$$

$$h\upsilon - h\upsilon_0 = e \times \Delta v$$

$$V_0 = \frac{hv}{e} - \frac{hv_0}{e}$$

'υ' is doubled

$$KE_{max} = 2h\upsilon - h\upsilon_0$$

$$V_0' = (\Delta V)' = \frac{2h\upsilon}{e} - \frac{h\upsilon_0}{e}$$

$$\frac{KE_{max}}{KE_{max}}$$
 may not be equal to 2

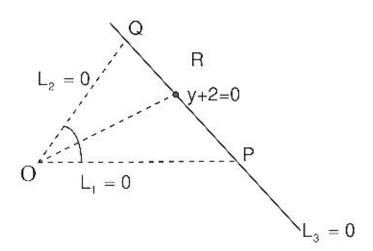
$$\Rightarrow \frac{V_0'}{V_0}$$
 may not equal to 2

$$V = \frac{h\upsilon}{e} - \frac{h\upsilon_0}{e}$$

### PART B: MATHEMATICS

31. 2

Sol:



$$P(-2, -2); Q = (1, -2)$$

Equation of angular bisector  $\overline{OR}$  is  $(\sqrt{5} + 2\sqrt{2})x = (\sqrt{5} - \sqrt{2})y$ 

$$\therefore PR : RQ = 2\sqrt{2} : \sqrt{5}$$

**Sol**: 
$$A = \sin^2 x + \cos^4 x = \frac{7 + \cos 4x}{8} \Rightarrow \frac{3}{4} \le A \le 1$$

$$\begin{aligned} \textbf{SoI:} & & \left[1-x-x^2\left(1-x\right)\right]^6 = \left(1-x\right)^6\left(1-x^2\right)^6 \\ & = \left[{}^6C_0 - {}^6C_1x + {}^6C_2x^2 - {}^6C_3x^3 + {}^6C_4x^4 - {}^6C_5x^5 + {}^6C_6x^6\right] \times \left[{}^6C_0 - {}^6C_1x^2 + {}^6C_2x^4 - {}^6C_3x^6 + ....\right] \\ & & \text{Coefficient of } & x^7 = {}^6C_1 \, {}^6C_3 - {}^6C_3 \, {}^6C_2 + {}^6C_5 \, {}^6C_1 = 120 - 300 + 36 = -144 \end{aligned}$$

Sol: 
$$\lim_{x\to 2} \frac{\sqrt{2\sin^2(x-2)}}{x-2}$$
$$\lim_{x\to 2} \frac{\sqrt{2}\left|\sin(x-2)\right|}{x-2}$$
$$R.H.L. = \sqrt{2}, L.H.L. = -\sqrt{2}$$
Limit does not exist.

**Sol**: 
$${}^{(n-1)}C_{(r-1)} = {}^{(10-1)}C_{(4-1)} = {}^{9}C_{3}$$

Statement 1 is correct

Statement 2 is also correct

From 9 we can select 3 in  ${}^9\mathrm{C}_3$  ways. It is correct explanation.



Sol: 
$$\frac{d}{dy} \left( \frac{dx}{dy} \right) = \frac{d}{dy} \left( \frac{1}{\begin{pmatrix} dy \\ dx \end{pmatrix}} \right) = -\frac{1}{\begin{pmatrix} \frac{dy}{dx} \end{pmatrix}^2} \frac{d}{dy} \left( \frac{dy}{dx} \right)$$
$$= -\left( \frac{dy}{dx} \right)^{-2} \frac{1}{\begin{pmatrix} \frac{dy}{dx} \end{pmatrix}} \frac{d}{dx} \left( \frac{dy}{dx} \right) = -\left( \frac{d^2y}{dx^2} \right) \left( \frac{dy}{dx} \right)^{-3}$$

Sol: 
$$\frac{dy}{dx} = y + 3 \Rightarrow \frac{dy}{y + 3} = dx$$

$$ln(y + 3) = x + c$$

$$x = 0 \Rightarrow y = 2$$

$$\Rightarrow ln5 = 0 + c$$

$$c = ln5$$

$$ln(y + 3) = x + ln5$$

$$y + 3 = e^{x + ln5} \Rightarrow y + 3 = e^{ln2 + ln5}$$

$$y + 3 = 10 \Rightarrow y = 7$$

Sol: 
$$x - y$$
 is an integer

$$x - x = 0$$
 is an integer  $\Rightarrow A$  is Reflexive

$$x - y$$
 is an integer  $\Rightarrow y - x$  is an integer  $\Rightarrow A$  is symmetric

$$x - y$$
,  $y - z$  are integers

As sum of two integers is an integer.

$$\Rightarrow$$
  $(x-y)+(y-z)=x-z$  is an integer

Also 
$$\frac{x}{x} = 1$$
 is a rational number  $\Rightarrow B$  is reflexive

$$\frac{x}{v} = \alpha$$
 is rational  $\Rightarrow \frac{y}{x}$  need not be rational

i.e., 
$$\frac{0}{1}$$
 is rational  $\Rightarrow \frac{1}{0}$  is not rational

Hence B is not symmetric

⇒ B is not an equivalence relation.



Sol: 
$$I = 8 \int_{0}^{1} \frac{\log(1+x)}{1+x^{2}} dx$$

$$= 8 \int_{0}^{4} \frac{\log(1+\tan\theta)}{1+\tan^{2}\theta} \sec^{2}\theta d\theta \text{ (let } x = \tan\theta)$$

$$= 8 \int_{0}^{4} \log\left(1+\tan\left(\frac{\pi}{4}-\theta\right)\right) d\theta = 8 \int_{0}^{4} \log\left(1+\frac{1-\tan\theta}{1+\tan\theta}\right) d\theta = 8 \int_{0}^{4} \log 2 d\theta - 8 \int_{0}^{4} \log(1+\tan\theta) d\theta$$

$$= 8 \log 2 \frac{\pi}{4} - I$$

$$2I = 2\pi \log 2$$

$$I = \pi \log 2$$

Sol: Suppose roots are 
$$1+pi$$
,  $1+qi$   
Sum of roots  $1+pi+1+qi=-\alpha$  which is real  
 $\Rightarrow$  roots of  $1+pi$ ,  $1-pi$   
Product of roots  $=\beta=1+p^2\in (1,\infty)$   
 $p\neq 0$  since roots are distinct.

41. 2
Sol: 
$$n = 5$$
Success = p
Failure = q
P (at least one failure)  $\geq \frac{31}{32}$ 
 $1 - P$  (no failure)  $\geq \frac{31}{32}$ 

$$1 - P(x = 5) \ge \frac{31}{32}$$
$$1 - {}^{5}C_{5}p^{5} \ge \frac{31}{32}$$

$$-p^5 \ge -\frac{1}{32}$$
$$p^5 \le \frac{1}{32}$$

$$p \le \frac{1}{2}$$

$$p \in \left[0, \frac{1}{2}\right]$$



Sol:

Sum = 11040

$$120 + 80 + 160 + 40 + 200 + 240 + ... = 11040$$

$$\frac{n}{2}$$
[2a+(n-1)d]+80+40 = 11040

$$\frac{n}{2}[240+(n-1)40]=10920$$

$$n\lceil 6+n-1\rceil = 546$$

$$n(n+5) = 546$$

$$n = 21$$

43. 2

Sol: 
$$\frac{1}{\sqrt{|x|-x}} \Rightarrow |x|-x > 0 \Rightarrow |x| > x \Rightarrow x \text{ is negative}$$
$$x \in (-\infty, 0)$$

44.

Sol: 
$$\cos \theta = \sqrt{\frac{5}{14}}$$

$$\sin \theta = \frac{3}{\sqrt{14}}$$

$$\sin \theta = \frac{1+4+3\lambda}{\sqrt{1+4+\lambda^2}\sqrt{1+4+9}}$$

$$\frac{3}{\sqrt{14}} = \frac{5+3\lambda}{\sqrt{5+\lambda^2}\sqrt{14}} \Rightarrow \lambda = \frac{2}{3}$$

45.

Sol: 
$$(2\overline{a} - \overline{b}) \cdot \{(\overline{a} \times \overline{b}) \times (\overline{a} + 2\overline{b})\} = (2\overline{a} - \overline{b}) \cdot \{[\overline{a} \cdot (\overline{a} + 2\overline{b})]\overline{b} - [\overline{b} \cdot (\overline{a} + 2\overline{b})\overline{a}]\}$$
  
=  $-5(\overline{a})^2 (\overline{b})^2 + 5(\overline{a}.\overline{b})^2 = -5$ 

46.

Sol: 
$$b^2 = a^2 (1 - e^2) = a^2 (1 - \frac{2}{5}) = a^2 \frac{3}{5} = \frac{3a^2}{5}$$
  
 $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1 \Rightarrow \frac{9}{a^2} + \frac{5}{3a^2} = 1$   
 $a^2 = \frac{32}{3}$   
 $b^2 = \frac{32}{5}$ 

 $\therefore$  Required equation of ellipse  $3x^2 + 5y^2 - 32 = 0$ 



47. 1

Sol: 
$$\frac{dV}{dt} = -k(T-t) \Rightarrow dV = -k(T-t)dt$$
Integrate
$$V = \frac{-k(T-t)^2}{(-2)} + c \Rightarrow V = \frac{k(T-t)^2}{2} + c$$
at  $t = 0 \Rightarrow V = 1$ 

$$I = \frac{kT^2}{2} + c \Rightarrow c = I - \frac{kT^2}{2} \Rightarrow c = V(T) = I - \frac{kT^2}{2}$$

48. 3
Sol: 
$$\overline{b} \times \overline{c} = \overline{b} \times \overline{d}$$

$$\Rightarrow \overline{a} \times (\overline{b} \times \overline{c}) = \overline{a} \times (\overline{b} \times \overline{d})$$

$$\Rightarrow (\overline{a}.\overline{c})\overline{b} - (\overline{a}.\overline{b})\overline{c} = (\overline{a}.\overline{d})\overline{b} - (\overline{a}.\overline{b})\overline{d}$$

$$\Rightarrow (\overline{a}.\overline{c})\overline{b} - (\overline{a}.\overline{b})\overline{c} = -(\overline{a}.\overline{b})\overline{d}$$

$$\therefore \overline{d} = \overline{c} - (\overline{a}.\overline{b})\overline{b}$$

49. 1

Sol: 
$$c_1 = \left(\frac{a}{2}, 0\right); c_2 = (0, 0)$$
 $r_1 = \frac{a}{2}; r_2 = c$ 
 $c_1c_2 = r_1 - r_2 \Rightarrow \frac{a}{2} = c - \frac{a}{2} \Rightarrow c = a$ 

50. 1

Sol: 
$$C \cap D = C \Rightarrow P(C \cap D) = P(C) \Rightarrow P\left(\frac{C}{D}\right) = \frac{P(C \cap D)}{P(D)} \ge P(C)$$

51. 1

Sol: 
$$\begin{vmatrix} 4 & k & 2 \\ k & 4 & 1 \\ 2 & 2 & 1 \end{vmatrix} = 0 \Rightarrow k^2 - 6k + 8 = 0 \Rightarrow k = 4, 2$$

52. 1 Sol: 
$${}^{\sim} \{(P \land {}^{\sim} R) \leftrightarrow Q\} = {}^{\sim} \{Q \leftrightarrow (P \land {}^{\sim} R)\}$$

Sol: 
$$P = (y^2, y)$$

Perpendicular distance from P to x - y + 1 = 0 is  $\frac{\left|y^2 - y + 1\right|}{\sqrt{2}}$ 

$$y^2 - y + 1 > 0 \ \forall y \in R$$

$$\therefore$$
 Coefficient  $y^2 > 0$ 

$$\therefore \text{ Min value } = \frac{1}{\sqrt{2}} \left( \frac{4ac - b^2}{4a} \right) = \frac{3}{4\sqrt{2}}$$

Sol: 
$$\frac{1}{n}\sum |x_i - A|$$

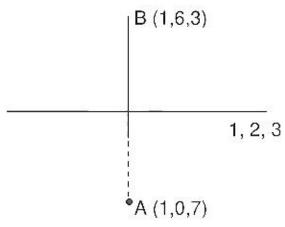
A = Median = 
$$\frac{25a + 26a}{2}$$
 = 25.5a

 $\text{Mean deviation } = \frac{1}{50} \Big\{ \Big| a - 25.5a \Big| + \Big| 2a - 25.5a \Big| \Big\} = \frac{2}{50} \Big\{ \Big( 24.5a + 23.5a \Big) + ... \Big( 0.5a \Big) \Big\}$ 

$$=\frac{2}{50}\{312.5a\}=50$$
 (Given)

$$\Rightarrow$$
 625a = 2500  $\Rightarrow$  a = 4

Sol:



Statement – 1: AB is perpendicular to given line and mid point of AB lies on line Statement – 2 is true but it is not correct explanation as it is bisector only. If it is perpendicular bisector then only statement – 2 is correct explanation.

Sol: 
$$A^T = A, B^T = B$$

$$\left(A\left(BA\right)\right)^{T}=\left(BA\right)^{T}A^{T}=\left(A^{T}B^{T}\right)A=\left(AB\right)A=A\left(BA\right)$$

$$\left(\left(\mathsf{A}\mathsf{B}\right)\mathsf{A}\right)^\mathsf{T} = \mathsf{A}^\mathsf{T}\left(\mathsf{A}\mathsf{B}\right)^\mathsf{T} = \mathsf{A}\left(\mathsf{B}^\mathsf{T}\mathsf{A}^\mathsf{T}\right) = \mathsf{A}\left(\mathsf{B}\mathsf{A}\right) = \left(\mathsf{A}\mathsf{B}\right)\mathsf{A}$$

:. Statement – 1 is correct

Statement - 2

$$(AB)^T = B^TA^T = BA = AB$$

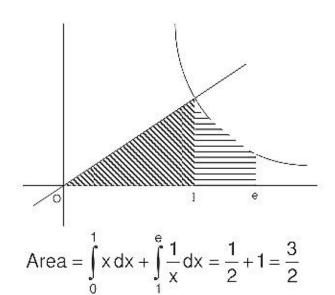
Statement - 2 is also correct but it is not correct explanation of Statement - 1



58.  $\lim_{x \to 0} \frac{\sin(p+1) + \sin x}{x} = q = \lim_{x \to 0} \frac{\sqrt{x + x^2} - \sqrt{x}}{x^{3/2}}$  $\lim_{x \to 0} (p+1)\cos(p+1)x + \cos x = q = \frac{1}{2}$  $\Rightarrow p+1+1 = \frac{1}{2} \Rightarrow p = -\frac{3}{2}; q = \frac{1}{2}$ 

59. **2** 

Sol:



60.

**Sol:**  $f'(x) = \sqrt{x} \sin x$ 

Given  $x \in \left(0, \frac{5\pi}{2}\right)$ 

f'(x) changes sign from +ve to -ve at  $\pi$ 

f'(x) changes sign from -ve to +ve at  $2\pi$ 

f has local max at  $\pi$  , local min at  $2\pi$ 



### PART C: CHEMISTRY

61. (2

Sol: Greater charge and small size of cation cause more polarization and more covalent is that compound

62. (1)

**Sol:** In RNA, the sugar is  $\beta - D - Ribose$ , where as in DNA the Sugar is  $\beta - D - 2$ -deoxy Ribose

63. (4)

**Sol**: 
$$2CCl_3CHO \xrightarrow{OH^{(-)}} CCl_3COONa + CCl_3CH_2OH$$

Cannizaro reaction is a disproportionation reaction

One aldehyde molecule is oxidized to salt of the carboxylic Acid, other one is reduced to

Alcohol. So the compound is CCI<sub>3</sub>CH<sub>2</sub>OH

IUPAC Name is 2, 2, 2, - Trichloro ethanol

64. (3

Sol: 
$$C_2H_5$$
 O N a + CH<sub>3</sub> - C-Cl  $\rightarrow$  CH<sub>3</sub> - C-O-C<sub>2</sub>H<sub>5</sub> Ethyl ethanoate  $\parallel$  O

65. (2)

**Sol:** 
$$2H^+ + 2e^- \rightarrow H_2(g)$$

$$E = E^{\circ} - 0.059 \log \left( \frac{P_{H_2}}{\left[H^{+}\right]^2} \right) \text{ (here E is -ve when } P_{H_2} > \left[H^{+}\right]^2 \text{)}$$

$$=\frac{-0.0591}{2}\log_{10}\left(\frac{2}{1}\right)=\frac{-.0591}{2}\times.3010$$
 = negative value

66. (2)

**Sol**: Electron releasing groups (Alkyl groups) de stabilizes conjugate base.

The +I effect of C<sub>3</sub>H<sub>7</sub> is less than - I effect of CI

 $K_a$  of HCOOH is  $17.9 \times 10^{-5}$ 

$$\overset{\circ}{\mathrm{K_{a}}}$$
 of  $\mathrm{CH_{3}CH_{2}}$  CH-COOH is  $139\times10^{-5}$  CI

67. (4)

**Sol**: 
$$i = 1 - \alpha + n\alpha = 1 + \alpha (n-1)$$

$$\frac{i-1}{n-1} = \alpha$$

$$A_x B_y \rightarrow x A^{-y} + y B^{-x}$$

$$n = x + y$$

So 
$$\alpha = \frac{i-1}{x+y-1}$$



#### AIEEE-ZUTT-Z8

68.

**Sol**: ease of liquefaction  $\propto \frac{a}{b}$ for ethane a = 5.49, b=0.0638for  $Cl_2$  a = 6.49, b = 0.0562

69.

Sol:

Initial moles Equilibriumm moles p-x

 $\begin{array}{lll} \hbox{ial moles} & \hbox{$p$} & \hbox{$O$} \\ \hbox{uillibriumm moles $p$-x} & \hbox{$2x$} \\ \hbox{Total pressure at equilibrium} & = 0.8 \ \hbox{atm} \ ; \hbox{Total no.of moles} & = p + x. \\ \end{array}$ 

Therefore  $p \propto n$ ;  $\frac{0.5}{0.8} = \frac{p}{p+x} \Rightarrow x = 0.3$ 

$$K_p = \frac{P_{CO}^2}{P_{CO_2}} = \frac{0.6 \times 0.6}{0.2} = 1.8 \text{ atm}$$

70.

As Boron has only four orbitals in the valence shell (i.e. 2s, 2px, 2py & 2pz) it can show a maximum valency of four only.

Therefore  $\left[BF_{6}\right]^{3-}$  is not possible

71.

 $\left[ \text{Cr} \left( \text{NH}_3 \right)_6 \right] \text{CI}_3$  involves  $d^2 \text{sp}^3$  hybridization and it is an inner orbital complex.

72.

Sol:  $\Delta T_f = K_f \times m = K_f \times \frac{W_2 \times 1000}{W_1 \times m_2}$ 

w<sub>1</sub> & w<sub>2</sub> = wt of solvent & solute respecting

 $m_2 = mw \text{ of solute}$ 

$$\Delta T_f = 0^\circ - (-6^\circ) = 6 = 1.86 \times \frac{W_2 \times 1000}{4000 \times 62}$$

Therefore  $w_2 = 800g$ 

73.

Across a period metallic strength decreases & down the group it increases

74.

Temperature coefficient  $\mu$  =2; Sol:

$$\mu^{\frac{\Delta T}{10}} = \frac{k_2}{k_1}$$

$$2^{\frac{50}{10}} = 2^5 = 32 = \frac{k_2}{k_1}$$

Therefore  $32k_1 = k_2$ 



Sol: 
$$\ln \left[ \text{NiCl}_4 \right]^{2^-}$$
,  $n = 2$   
 $\mu = \sqrt{n(n+2)}$  BM  
 $= \sqrt{2(2+2)} = 2.82$ BM

76. (1)

Sol:

77.

The general o.s of lanthanides is +3, only few elements exhibit +4 o.s.

78.

78. (2)

Sol: Molefraction of solute 
$$(X_2)$$
 in aqueous solution = 
$$\frac{m}{m + \frac{1000}{18}}$$

$$= \frac{5.2}{5.2 + \frac{1000}{18}} = 0.09$$

79.

Stability of hydrides decreases down the group from NH3 to BiH3 as M-H bond energy decreases. Sol:

80. (3)

81.

'S' can exhibit a minimum oxidation state of -2 Sol:  $(Ex. H_2S)$ 

82.

In IF<sub>7</sub>, I undergoes sp<sup>3</sup>d<sup>3</sup> hybridisation

83.

Sol: Vinyl group

$$\left( CH_{2} - CH - \right)$$

on ozonolosys give formaldehyde

84. (2)

Sol: 
$$\frac{1}{\lambda_{absorbed}} = \frac{1}{\lambda_1} + \frac{1}{\lambda_2}$$

$$\Rightarrow \frac{1}{355} = \frac{1}{680} + \frac{1}{\lambda_2}$$

$$\Rightarrow \lambda_2 = 742.8 \cong 743 \text{ nm}$$

(2, 4)85.

Formaldehyde and Acetaldehyde can be oxidized by tollen's reagent to give silver mirror. Sol:



#### AIEEE-2011-30

86. (3

**Sol:** Phenol gives violet coloured comlex compound with neutral FeCl<sub>3</sub>, benzoic acid gives pale dull yellow ppt. with neutral FeCl<sub>3</sub>

87. (3)

Sol: In acidic medium, KBr + KBrO<sub>3</sub> in turn produces Br<sub>2</sub>. Phenol reacts with Br<sub>2</sub> (aq) to give 2, 4, 6-trinitrophenol

88. (3)

**Sol :** Effective no.of A atoms =  $\frac{1}{8} \times 8 = 1$ Effective no.of B atoms =  $\frac{1}{2} \times 5$  (One is missing) =  $\frac{5}{2}$ Therefore formula is  $A_1B_5 = A_2B_5$ 

89. (4)

Sol: For an ideal gas, for isothermal reversible process,

$$\Delta S = 2.303 \text{ nR log} \left( \frac{V_2}{V_1} \right)$$
  
= 2.303×2×8.314×log $\left( \frac{100}{10} \right)$   
= 38.3 J mol <sup>1</sup>.k <sup>1</sup>

90. 2, (2, 3)

Sol: both 2-pentanone, phenol can exhibit tautomerism

