

Date: 26/05/2024



# Aakash

Medical | IIT-JEE | Foundations

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Time : 3 hrs.

## Answers & Solutions

Max. Marks: 180

for

## JEE (Advanced)-2024 (Paper-2)

### PART-I : MATHEMATICS

#### SECTION 1 (Maximum Marks : 12)

- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:

Full Marks : +3 If **ONLY** the correct option is chosen;

Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);

Negative Marks : -1 In all other cases.

1. Considering only the principal values of the inverse trigonometric functions, the value of

$$\tan\left(\sin^{-1}\left(\frac{3}{5}\right) - 2\cos^{-1}\left(\frac{2}{\sqrt{5}}\right)\right)$$
 is

(A)  $\frac{7}{24}$

(B)  $-\frac{7}{24}$

(C)  $-\frac{5}{24}$

(D)  $\frac{5}{24}$

Answer (B)

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4 Year Classroom



**Tanishka Kabra**  
4 Year Classroom  
ALL INDIA RANK 1 (Female)  
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**Chirag Falor**  
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**Sol.**  $\tan\left(\sin^{-1}\left(\frac{3}{5}\right) - 2\cos^{-1}\left(\frac{2}{\sqrt{5}}\right)\right)$

Let  $\sin^{-1}\frac{3}{5} = \alpha$ ,  $2\cos^{-1}\frac{2}{\sqrt{5}} = \beta \Rightarrow \cos\frac{\beta}{2} = \frac{2}{\sqrt{5}}$

$\therefore \sin\alpha = \frac{3}{5} \Rightarrow \tan\alpha = \frac{3}{4}$   $\tan\beta = \frac{2\tan\frac{\beta}{2}}{1 - \tan^2\frac{\beta}{2}} = \frac{2 \times \frac{1}{2}}{1 - \frac{1}{4}} = \frac{4}{3}$

$\Rightarrow \tan(\alpha - \beta) = \frac{\tan\alpha - \tan\beta}{1 + \tan\alpha\tan\beta} = \frac{\frac{3}{4} - \frac{4}{3}}{1 + 1} = -\frac{7}{24}$

2. Let  $S = \{(x, y) \in \mathbb{R} \times \mathbb{R} : x \geq 0, y \geq 0, y^2 \leq 4x, y^2 \leq 12 - 2x \text{ and } 3y + \sqrt{8}x \leq 5\sqrt{8}\}$ . If the area of the region S is  $\alpha\sqrt{2}$ , then  $\alpha$  is equal to

(A)  $\frac{17}{2}$

(B)  $\frac{17}{3}$

(C)  $\frac{17}{4}$

(D)  $\frac{17}{5}$

**Answer (B)**

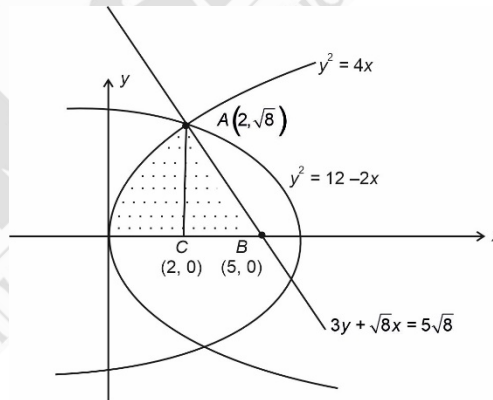
**Sol.**  $y^2 = 4x, y^2 = 12 - 2x \Rightarrow x = 2, y = \sqrt{8}$

$A = \int_0^2 2\sqrt{x}dx + \frac{1}{2} \times 3 \times \sqrt{8}$

$= \left[ 2 \times \frac{2}{3} x^{\frac{3}{2}} \right]_0^2 + 3\sqrt{2} = \frac{4}{3} \times 2\sqrt{2} + 3\sqrt{2} = \frac{17}{3}\sqrt{2}$

$\therefore A = \alpha\sqrt{2} \Rightarrow \alpha = \frac{17}{3}$

Option (B) is correct.



3. Let  $k \in \mathbb{R}$ . If  $\lim_{x \rightarrow 0^+} (\sin(\sin kx) + \cos x + x)^{\frac{2}{x}} = e^6$ , then the value of  $k$  is

(A) 1

(B) 2

(C) 3

(D) 4

**Answer (B)**

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**Sol.**  $I = \lim_{x \rightarrow 0^+} (\sin(\sin kx) + \cos x + x)^{\frac{2}{x}} = e^6$

$$\Rightarrow \ln I = \lim_{x \rightarrow 0^+} \frac{2}{x} (\sin(\sin kx) + \cos x + x - 1)$$

$$\Rightarrow \ln I = \lim_{x \rightarrow 0^+} 2 \left( \frac{\sin(\sin kx)}{\sin kx} \cdot \frac{\sin kx}{kx} \cdot \frac{kx}{x} + 1 - \frac{(1 - \cos x)}{x^2} \cdot x \right)$$

$$\Rightarrow \ln I = 2(k + 1) \quad \Rightarrow \quad I = e^{2(k+1)} = e^6$$

$$k + 1 = 3 \quad \Rightarrow \quad k = 2$$

4. Let  $f : \mathbb{R} \rightarrow \mathbb{R}$  be a function defined by

$$f(x) = \begin{cases} x^2 \sin\left(\frac{\pi}{x^2}\right), & \text{if } x \neq 0, \\ 0, & \text{if } x = 0. \end{cases}$$

Then which of the following statements is TRUE?

(A)  $f(x) = 0$  has infinitely many solutions in the interval  $\left[\frac{1}{10^{10}}, \infty\right)$ .

(B)  $f(x) = 0$  has no solutions in the interval  $\left[\frac{1}{\pi}, \infty\right)$ .

(C) The set of solutions of  $f(x) = 0$  in the interval  $\left(0, \frac{1}{10^{10}}\right)$  is finite.

(D)  $f(x) = 0$  has more than 25 solutions in the interval  $\left(\frac{1}{\pi^2}, \frac{1}{\pi}\right)$ .

**Answer (D)**

**Sol.**  $f(x) = \begin{cases} x^2 \sin\left(\frac{\pi}{x^2}\right), & \text{if } x \neq 0, \\ 0, & \text{if } x = 0. \end{cases}$

$$f(x) = 0 \Rightarrow \sin\left(\frac{\pi}{x^2}\right) = 0$$

$$\Rightarrow \frac{\pi}{x^2} = n\pi$$

$$\Rightarrow x^2 = \frac{1}{n}$$

$$\Rightarrow x = \frac{1}{\sqrt{n}}$$

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$$\text{If } x \in \left[ \frac{1}{10^{10}}, \infty \right)$$

$$\frac{1}{\sqrt{n}} \in \left[ \frac{1}{10^{10}}, \infty \right)$$

$$\sqrt{n} \in (0, 10^{10}]$$

$$n \in (0, (10^{10})^2]$$

Finite values of  $n$

$$\text{If } x \in \left[ \frac{1}{\pi}, \infty \right)$$

$$\frac{1}{\sqrt{n}} \in \left[ \frac{1}{\pi}, \infty \right)$$

$$\sqrt{n} \in (0, \pi]$$

$$n \in (0, \pi^2]$$

$n = 1, 2, 3 \dots 9$

$$\text{If } x \in \left( 0, \frac{1}{10^{10}} \right)$$

$$\sqrt{n} \in (10^{10}, \infty)$$

$n$  infinite

$$\text{If } x \in \left( \frac{1}{\pi^2}, \frac{1}{\pi} \right)$$

$$\sqrt{n} \in (\pi, \pi^2)$$

$$n \in (\pi^2, \pi^4)$$

$$n \in (9.8, 97.2 \dots)$$

More than 25 solutions

**SECTION 2 (Maximum Marks : 12)**

- This section contains **THREE (03)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

**Full Marks** : +4 **ONLY** if (all) the correct option(s) is(are) chosen;

**Partial Marks** : +3 If all the four options are correct but **ONLY** three options are chosen;

**Partial Marks** : +2 If three or more options are correct but **ONLY** two options are chosen, both of which are correct;

**Partial Marks** : +1 If two or more options are correct but **ONLY** one option is chosen and it is a correct option;

**Zero Marks** : 0 If unanswered;

**Negative Marks** : -2 In all other cases.

5. Let  $S$  be the set of all  $(\alpha, \beta) \in \mathbb{R} \times \mathbb{R}$  such that

$$\lim_{x \rightarrow \infty} \frac{\sin(x^2)(\log_e x)^\alpha \sin\left(\frac{1}{x^2}\right)}{x^{\alpha\beta}(\log_e(1+x))^\beta} = 0$$

Then which of the following is (are) correct?

(A)  $(-1, 3) \in S$

(B)  $(-1, 1) \in S$

(C)  $(1, -1) \in S$

(D)  $(1, -2) \in S$

**Answer (B, C)**

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**Sol.** 
$$\lim_{x \rightarrow \infty} \frac{\sin(x^2) \sin\left(\frac{1}{x^2}\right) (\ln x)^\alpha}{x^{\alpha\beta} (\ln(1+x))^\beta} = 0$$

$$= \lim_{x \rightarrow \infty} \frac{(\sin x^2) \sin\left(\frac{1}{x^2}\right) \frac{1}{x^2}}{\left(\frac{1}{x^2}\right) x^{\alpha\beta} (\ln(1+x))^\beta} = 0$$

It is possible if  $\alpha\beta + 2 > 0$

$\alpha\beta > -2$

- (A)  $\alpha\beta = -3$
- (B)  $\alpha\beta = -1$
- (C)  $\alpha\beta = -1$
- (D)  $\alpha\beta = -2$

6. A straight line drawn from the point  $P(1,3,2)$ , parallel to the line  $\frac{x-2}{1} = \frac{y-4}{2} = \frac{z-6}{1}$ , intersects the plane  $L_1 : x - y + 3z = 6$  at the point  $Q$ . Another straight line which passes through  $Q$  and is perpendicular to the plane  $L_1$  intersects the plane  $L_2 : 2x - y + z = -4$  at the point  $R$ . Then which of the following statements is(are) TRUE?
- (A) The length of the line segment  $PQ$  is  $\sqrt{6}$
  - (B) The coordinates of  $R$  are  $(1,6,3)$
  - (C) The centroid of the triangle  $PQR$  is  $\left(\frac{4}{3}, \frac{14}{3}, \frac{5}{3}\right)$
  - (D) The perimeter of the triangle  $PQR$  is  $\sqrt{2} + \sqrt{6} + \sqrt{11}$

**Answer (A, C)**

**Sol.** Equation of line parallel to  $\frac{x-2}{1} = \frac{y-4}{2} = \frac{z-6}{1}$  through  $P(1,3,2)$  is  $\frac{x-1}{1} = \frac{y-3}{2} = \frac{z-2}{1} = \lambda$  (let)

Now, putting any point  $(\lambda + 1, 2\lambda + 3, \lambda + 2)$  in  $L_1$

$\lambda = 1$

$\Rightarrow$  Point  $Q(2,5,3)$

Equation of line through  $Q(2,5,3)$  perpendicular to  $L_1$  is

$\frac{x-2}{1} = \frac{y-5}{-1} = \frac{z-3}{3} = \mu$  (Let)

Putting any point  $(\mu + 2, -\mu + 5, 3\mu + 3)$  in  $L_2$

$\mu = -1$

$\Rightarrow$  Point  $R(1, 6, 0)$

- (A)  $PQ = \sqrt{1+4+1} = \sqrt{6}$
- (B)  $R(1, 6, 0)$
- (C) Centroid  $\left(\frac{4}{3}, \frac{14}{3}, \frac{5}{3}\right)$
- (D)  $PQ + QR + PR = \sqrt{6} + \sqrt{11} + \sqrt{13}$

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7. Let  $A_1, B_1, C_1$  be three points in the  $xy$ -plane. Suppose that the lines  $A_1C_1$  and  $B_1C_1$  are tangents to the curve  $y^2 = 8x$  at  $A_1$  and  $B_1$ , respectively. If  $O = (0,0)$  and  $C_1 = (-4,0)$ , then which of the following statements is (are) TRUE?

- (A) The length of the line segment  $OA_1$  is  $4\sqrt{3}$       (B) The length of the line segment  $A_1B_1$  is 16  
 (C) The orthocentre of the triangle  $A_1B_1C_1$  is  $(0, 0)$       (D) The orthocentre of the triangle  $A_1B_1C_1$  is  $(1, 0)$

**Answer (A, C)**

Let  $A_1 = (2t_1^2, 4t_1)$  and  $B_1 = (2t_2^2, 4t_2)$

$C_1 = (-4, 0) = (2t_1t_2, 2(t_1 + t_2))$

$\Rightarrow t_2 = -t_1$  and  $t_1(-t_1) = -2$

$t_1 = \sqrt{2}, t_2 = -\sqrt{2}$

$A_1 = (4, 4\sqrt{2}), B_1 = (4, -4\sqrt{2})$

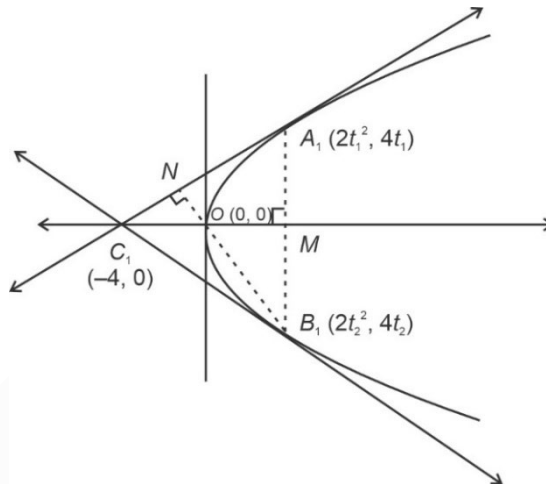
$\therefore OA_1 = \sqrt{4^2 + (4\sqrt{2})^2} = 4\sqrt{3}$

$A_1B_1 = 8\sqrt{2}$

Altitude  $C_1M : y = 0$       ... (i)

Altitude  $B_1N : \sqrt{2}x + y = 0$       ... (ii)

$\therefore$  Orthocentre  $\equiv (0, 0)$



**SECTION 3 (Maximum Marks : 24)**

- This section contains **SIX (06)** questions.
- The answer to each question is a **NON-NEGATIVE INTEGER**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:

Full Marks : +4 If **ONLY** the correct integer is entered;

Zero Marks : 0 In all other cases.

8. Let  $f : \mathbb{R} \rightarrow \mathbb{R}$  be a function such that  $f(x+y) = f(x) + f(y)$  for all  $x, y \in \mathbb{R}$ , and  $g : \mathbb{R} \rightarrow (0, \infty)$  be a function such that  $g(x+y) = g(x)g(y)$  for all  $x, y \in \mathbb{R}$ . If  $f\left(\frac{-3}{5}\right) = 12$  and  $g\left(\frac{-1}{3}\right) = 2$ , then the value of

$\left(f\left(\frac{1}{4}\right) + g(-2) - 8\right)g(0)$  is \_\_\_\_\_.

**Answer (51)**

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Sol.  $f(x + y) = f(x) + f(y)$

$\Rightarrow f(x) = kx$

$f\left(\frac{-3}{5}\right) = 12 \Rightarrow k = -20$

$\therefore f(x) = -20x$

$g(x + y) = g(x)g(y) \Rightarrow g(x) = a^x$

$g\left(\frac{-1}{3}\right) = 2 \Rightarrow a = \frac{1}{8}$

$\therefore g(x) = \left(\frac{1}{8}\right)^x$

$\left(f\left(\frac{1}{4}\right) + g(-2) - 8\right)g(0) = (-5 + 64 - 8) \times 1 = 51$

9. A bag contains  $N$  balls out of which 3 balls are white, 6 balls are green, and the remaining balls are blue. Assume that the balls are identical otherwise. Three balls are drawn randomly one after the other without replacement. For  $i = 1, 2, 3$ , let  $W_i, G_i$ , and  $B_i$  denote the events that the ball drawn in the  $i^{\text{th}}$  draw is a white ball, green ball, and blue ball, respectively, If the probability  $P(W_1 \cap G_2 \cap B_3) = \frac{2}{5N}$  and the conditional probability

$P(B_3 | W_1 \cap G_2) = \frac{2}{9}$ , then  $N$  equals \_\_\_\_\_.

**Answer (11)**

Sol.  $N$  Balls =  $3W + 6G + (N - 9)B$

$P(W_1 \cap G_2 \cap B_3) = \frac{2}{5N}$

$\Rightarrow \frac{3}{N} \times \frac{6}{N-1} \times \frac{N-9}{N-2} = \frac{2}{5N}$

$\Rightarrow N^2 - 48N + 407 = 0$

$\Rightarrow N = 11$  or  $37$

$P(B_3 | W_1 \cap G_2) = \frac{2}{9}$

$\Rightarrow \frac{P(W_1 \cap G_2 \cap B_3)}{P(W_1 \cap G_2)} = \frac{2}{9}$

$\Rightarrow \frac{\frac{2}{5N}}{\frac{3}{N} \times \frac{6}{N-1}} = \frac{2}{9}$

$\Rightarrow \frac{N-1}{45} = \frac{2}{9}$

$\Rightarrow N = 11$

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
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10. Let the function  $f : \mathbb{R} \rightarrow \mathbb{R}$  be defined by

$$f(x) = \frac{\sin x (x^{2023} + 2024x + 2025)}{e^{\pi x} (x^2 - x + 3)} + \frac{2 (x^{2023} + 2024x + 2025)}{e^{\pi x} (x^2 - x + 3)}$$

Then the number of solutions of  $f(x) = 0$  in  $\mathbb{R}$  is \_\_\_\_\_.

**Answer (01)**

**Sol.**  $f(x) = 0$

$$\Rightarrow \frac{x^{2023} + 2024x + 2025}{(x^2 - x + 3)} \left[ \frac{\sin x + 2}{e^{\pi x}} \right] = 0$$

$$\Rightarrow x^{2023} + 2024x + 2025 = 0$$

Let  $g(x) = x^{2023} + 2024x + 2025$

$$g'(x) = 2023x^{2022} + 2024 > 0 \quad \forall x \in \mathbb{R}$$

$\therefore f(x) = 0$  has only one solution

11. Let  $\vec{p} = 2\hat{i} + \hat{j} + 3\hat{k}$  and  $\vec{q} = \hat{i} - \hat{j} + \hat{k}$ . If for some real numbers  $\alpha$ ,  $\beta$  and  $\gamma$ , we have  $15\hat{i} + 10\hat{j} + 6\hat{k} = \alpha(2\vec{p} + \vec{q}) + \beta(\vec{p} - 2\vec{q}) + \gamma(\vec{p} \times \vec{q})$ , then the value of  $\gamma$  is \_\_\_\_\_.

**Answer (2)**

**Sol.**  $2\vec{p} + \vec{q} = 5\hat{i} + \hat{j} + 7\hat{k}$

$$\vec{p} - 2\vec{q} = 0\hat{i} + 3\hat{j} + \hat{k}$$

$$\vec{p} \times \vec{q} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & 1 & 3 \\ 1 & -1 & 1 \end{vmatrix} = \hat{i}(4) - \hat{j}(-1) + \hat{k}(-3)$$

$$= 4\hat{i} + \hat{j} - 3\hat{k}$$

$$15\hat{i} + 10\hat{j} + 6\hat{k} = \alpha(5\hat{i} + \hat{j} + 7\hat{k}) + \beta(3\hat{j} + \hat{k}) + \gamma(4\hat{i} + \hat{j} - 3\hat{k})$$

$$\therefore 15 = 5\alpha + 4\gamma$$

$$10 = \alpha + 3\beta + \gamma$$

$$6 = 7\alpha + \beta - 3\gamma$$

$$\therefore \alpha = \frac{7}{5}, \beta = \frac{11}{5}, \gamma = 2$$

$$\therefore \gamma = 2$$

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<p><b>Karnataka Topper</b></p>  <p><b>AIR 34</b> ALL INDIA FEMALE TOPPER <b>100</b> PERCENTILE OVERALL <b>Sanvi Jain</b> 4 Year Classroom</p>	<p><b>Telangana Topper</b></p>  <p><b>AIR 15</b> <b>100</b> PERCENTILE OVERALL <b>M. Sai Divya Teja Reddy</b> 2 Year Classroom</p>	<p><b>Telangana Topper</b></p>  <p><b>AIR 19</b> <b>100</b> PERCENTILE OVERALL <b>Rishi Shekher Shukla</b> 2 Year Classroom</p>	<p><b>Punjab Topper</b></p>  <p><b>AIR 25</b> <b>100</b> PERCENTILE OVERALL <b>Rachit Aggarwal</b> 4 Year Classroom</p>	 <p><b>Tanishka Kabra</b> 4 Year Classroom <b>1</b> AIR-16 CRL JEE (Adv.) 2022 ALL INDIA RANK (Female)</p>	 <p><b>Chirag Falor</b> 4 Year Classroom <b>1</b> AIR JEE (Adv.) 2020</p>
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12. A normal with slope  $\frac{1}{\sqrt{6}}$  is drawn from the point  $(0, -\alpha)$  to the parabola  $x^2 = -4ay$ , where  $a > 0$ . Let  $L$  be the line passing through  $(0, -\alpha)$  and parallel to the directrix of the parabola. Suppose that  $L$  intersects the parabola at two points  $A$  and  $B$ . Let  $r$  denote the length of the latus rectum and  $s$  denote the square of the length of the line segment  $AB$ . If  $r : s = 1 : 16$ , then the value of  $24a$  is \_\_\_\_\_.

**Answer (12)**

**Sol.**  $x^2 = -4ay$

Equation of normal

$$y = mx - 2a - \frac{a}{m^2}$$

$$-\alpha = -2a - \frac{a}{\frac{1}{6}} = -8a$$

$$\Rightarrow \alpha = 8a$$

Equation of required line

$$y = -\alpha$$

$$\Rightarrow y = -8a, \text{ solving with } x^2 = -4ay$$

$$\Rightarrow x^2 = 32a^2$$

$$\Rightarrow x = \pm 4\sqrt{2}a$$

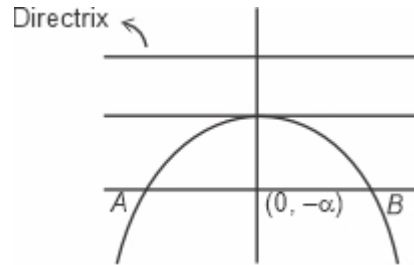
$$= \pm \frac{\alpha}{\sqrt{2}}$$

$$A\left(\frac{\alpha}{\sqrt{2}}, -\alpha\right), B\left(-\frac{\alpha}{\sqrt{2}}, -\alpha\right) \Rightarrow AB = \sqrt{2}\alpha$$

$$\Rightarrow \frac{r}{s} = \frac{4a}{2\alpha^2} = \frac{1}{16} \Rightarrow \frac{4a}{2 \times 64a^2} = \frac{1}{16}$$

$$\Rightarrow a = \frac{1}{2}$$

$$\Rightarrow \boxed{24a = 12}$$



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13. Let the function  $f : [1, \infty) \rightarrow \mathbb{R}$  be defined by

$$f(t) = \begin{cases} (-1)^{n+1}2, & \text{if } t = 2n-1, n \in \mathbb{N}, \\ \frac{(2n+1-t)}{2}f(2n-1) + \frac{(t-(2n-1))}{2}f(2n+1), & \text{if } 2n-1 < t < 2n+1, n \in \mathbb{N}. \end{cases}$$

Define  $g(x) = \int_1^x f(t)dt, x \in (1, \infty)$ . Let  $\alpha$  denote the number of solutions of the equation  $g(x) = 0$  in the interval  $(1, 8]$  and  $\beta = \lim_{x \rightarrow 1^+} \frac{g(x)}{x-1}$ . Then the value of  $\alpha + \beta$  is equal to \_\_\_\_\_.

**Answer (5)**

**Sol.**  $f(t) = \left(\frac{(2n+1)-t}{2}\right)(-1)^{n+1}2 + \left(\frac{t-(2n-1)}{2}\right)(-1)^{n+2}2, t \in (2n-1, 2n+1)$

$$\Rightarrow f(t) = 2(-1)^{n+1}(2n-t), t \in (2n-1, 2n+1)$$

$$\Rightarrow g(x) = \int_1^x f(t)dt, x \in (1, 8]$$

$$= \begin{cases} \int_1^x 2(2-t)dt, 1 < x \leq 3, n=1 \\ \int_1^3 2(2-t)dt + \int_3^x (2t-8)dt, 3 < x \leq 5, n=2 \\ \int_1^3 2(2-t)dt + \int_3^5 (2t-8)dt + \int_5^x 2(6-t)dt, 5 < x \leq 7, n=3 \\ \int_1^3 2(2-t)dt + \int_3^5 (2t-8)dt + \int_5^7 2(6-t)dt + \int_7^x (2t-16)dt, x \in (7, 8], n=4 \end{cases}$$

$$= \begin{cases} -x^2 + 4x - 3, 1 < x \leq 3, \\ x^2 - 8x + 15, 3 < x \leq 5 \\ -x^2 + 12x - 35, 5 < x \leq 7 \\ x^2 - 16x + 63, 7 < x \leq 8 \end{cases} = \begin{cases} -(x-1)(x-3), 1 < x \leq 3 \\ (x-3)(x-5), 3 < x \leq 5 \\ -(x-5)(x-7), 5 < x \leq 7 \\ (x-7)(x-9), 7 < x \leq 8 \end{cases}$$

$$\Rightarrow g(x) = 0 \Rightarrow x = 3, 5, 7 \Rightarrow \alpha = 3$$

$$\beta = \lim_{x \rightarrow 1^+} \left(\frac{g(x)}{x-1}\right) = \lim_{x \rightarrow 1^+} -\frac{(x-1)(x-3)}{x-1} = 2$$

$$\Rightarrow \alpha + \beta = 5$$

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**SECTION 4 (Maximum Marks : 12)**

- This section contains **TWO (02)** paragraphs.
- Based on each paragraph, there are **TWO (02)** questions.
- The answer to each question is a **NUMERICAL VALUE**.
- For each question, enter the correct numerical value of the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- If the numerical value has more than two decimal places, **truncate/round-off** the value to **TWO** decimal places.
- Answer to each question will be evaluated according to the following marking scheme:

**Full Marks** : +3 If **ONLY** the correct numerical value is entered in the designated place;  
**Zero Marks** : 0 In all other cases.

**PARAGRAPH I**

Let  $S = \{1, 2, 3, 4, 5, 6\}$  and  $X$  be the set of all relations  $R$  from  $S$  to  $S$  that satisfy both the following properties:

- $R$  has exactly 6 elements.
- For each  $(a, b) \in R$ , we have  $|a - b| \geq 2$ .

Let  $Y = \{R \in X : \text{The range of } R \text{ has exactly one element}\}$  and  
 $Z = \{R \in X : R \text{ is a function from } S \text{ to } S\}$ .

Let  $n(A)$  denote the number of elements in a set  $A$ .

**(There are two questions based on PARAGRAPH "I", the question given below is one of them)**

14. If  $n(X) = {}^m C_6$ , then the value of  $m$  is \_\_\_\_\_.

**Answer (20)**

**Sol.**  $S = \{1, 2, 3, 4, 5, 6\}$   $R : S \rightarrow S$

Number of elements in  $R = 6$

and for each  $(a, b) \in R ; |a - b| \geq 2$

$X \rightarrow$  set of all relation  $R : S \rightarrow S$

If $a = 1, b = 3, 4, 5, 6 \rightarrow \textcircled{4}$ $a = 2, b = 4, 5, 6 \rightarrow \textcircled{3}$ $a = 3, b = 1, 5, 6 \rightarrow \textcircled{3}$ $a = 4, b = 1, 2, 6 \rightarrow \textcircled{3}$ $a = 5, b = 1, 2, 3 \rightarrow \textcircled{3}$ $a = 6, b = 1, 2, 3, 4 \rightarrow \textcircled{4}$	Total number of ordered pairs $(a, b)$ s.t. $ a - b  \geq 2$ = 20
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$\therefore n(X) =$  number of elements in  $X$   
 $= {}^{20} C_6 \quad \therefore m = 20$

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**PARAGRAPH I**

Let  $S = \{1, 2, 3, 4, 5, 6\}$  and  $X$  be the set of all relations  $R$  from  $S$  to  $S$  that satisfy both the following properties:

- i.  $R$  has exactly 6 elements.
- ii. For each  $(a, b) \in R$ , we have  $|a - b| \geq 2$ .

Let  $Y = \{R \in X : \text{The range of } R \text{ has exactly one element}\}$  and

$Z = \{R \in X : R \text{ is a function from } S \text{ to } S\}$ .

Let  $n(A)$  denote the number of elements in a set  $A$ .

**(There are two questions based on PARAGRAPH "I", the question given below is one of them)**

15. If the value of  $n(Y) + n(Z)$  is  $k^2$ , then  $|k|$  is \_\_\_\_\_.

**Answer (36)**

**Sol.**  $S = \{1, 2, 3, 4, 5, 6\}$                        $R : S \rightarrow S$

Number of elements in  $R = 6$

and for each  $(a, b) \in R; |a - b| \geq 2$

$X \rightarrow$  set of all relation  $R : S \rightarrow S$

If	$a = 1$	$b = 3, 4, 5, 6$	$\rightarrow$	4	} Total number of ordered pairs $(a, b)$ s. t. $ a - b  \geq 2 = 20$
	$a = 2$	$b = 4, 5, 6$	$\rightarrow$	3	
	$a = 3$	$b = 1, 5, 6$	$\rightarrow$	3	
	$a = 4$	$b = 1, 2, 6$	$\rightarrow$	3	
	$a = 5$	$b = 1, 2, 3$	$\rightarrow$	3	
	$a = 6$	$b = 1, 2, 3, 4$	$\rightarrow$	4	

$\therefore n(X) =$  number of elements in  $X$   
 $= {}^{20}C_6 \quad \therefore m = 20$

$Y = \{R \in X : \text{The range of } R \text{ has exactly one element}\}$

From above, if range of  $R$  has exactly one element, then maximum number of elements in  $R$  will be 4.

$\therefore n(Y) = 0$

$Z = \{R \in X : R \text{ is a function from } S \text{ to } S\}$

$n(Z) = {}^4C_1 \times {}^3C_1 \times {}^3C_1 \times {}^3C_1 \times {}^3C_1 \times {}^4C_1$   
 $= (36)^2$

$n(y) + n(z) = 0 + (36)^2 = k^2$

$\Rightarrow |k| = 36$

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PARAGRAPH II

Let  $f : \left[0, \frac{\pi}{2}\right] \rightarrow [0, 1]$  be the function defined by  $f(x) = \sin^2 x$  and let  $g : \left[0, \frac{\pi}{2}\right] \rightarrow [0, \infty)$  be the function defined by  $g(x) = \sqrt{\frac{\pi x}{2} - x^2}$ .

(There are two questions based on PARAGRAPH "II", the question given below is one of them)

16. The value of  $2 \int_0^{\frac{\pi}{2}} f(x)g(x)dx - \int_0^{\frac{\pi}{2}} g(x)dx$  is \_\_\_\_\_.

Answer (0)

Sol.  $f(x) = \sin^2 x$ ,  $g(x) = \sqrt{\frac{\pi x}{2} - x^2}$

Here  $f\left(\frac{\pi}{2} - x\right) = \cos^2 x$ ,  $g\left(\frac{\pi}{2} - x\right) = g(x)$

Let  $I_1 = 2 \int_0^{\frac{\pi}{2}} f(x)g(x)dx = 2 \int_0^{\frac{\pi}{2}} \sin^2 x \cdot g(x)dx$  ... (1)

as  $\int_a^b f(x)dx = \int_a^b f(a+b-x)dx$

$\Rightarrow I_1 = 2 \int_0^{\frac{\pi}{2}} \cos^2 x g(x)dx$  ... (2)

(1) + (2)

$\Rightarrow 2I_1 = 2 \int_0^{\frac{\pi}{2}} g(x)dx$

$\Rightarrow I_1 = \int_0^{\frac{\pi}{2}} g(x)dx$

$\Rightarrow 2 \int_0^{\frac{\pi}{2}} f(x)g(x)dx - \int_0^{\frac{\pi}{2}} g(x)dx = 0$

PARAGRAPH II

Let  $f : \left[0, \frac{\pi}{2}\right] \rightarrow [0, 1]$  be the function defined by  $f(x) = \sin^2 x$  and let  $g : \left[0, \frac{\pi}{2}\right] \rightarrow [0, \infty)$  be the function defined by  $g(x) = \sqrt{\frac{\pi x}{2} - x^2}$ .

(There are two questions based on PARAGRAPH "II", the question given below is one of them)

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17. The value of  $\frac{16}{\pi^3} \int_0^{\frac{\pi}{2}} f(x)g(x)dx$  is \_\_\_\_\_.

**Answer (0.25)**

**Sol.** According to Q.16

$$2 \int_0^{\frac{\pi}{2}} f(x)g(x)dx = \int_0^{\frac{\pi}{2}} g(x)dx = I_1 \text{ (let)}$$

$$\text{Now, } I_1 = \int_0^{\frac{\pi}{2}} g(x)dx = \int_0^{\frac{\pi}{2}} \sqrt{\frac{\pi}{2}x - x^2} dx$$

$$I_1 = \int_0^{\frac{\pi}{2}} \sqrt{\left(\frac{\pi}{4}\right)^2 - \left(\frac{\pi}{4} - x\right)^2} dx$$

$$\text{Put } \frac{\pi}{4} - x = t$$

$$\Rightarrow dx = -dt$$

$$I_1 = - \int_{\frac{\pi}{4}}^{-\frac{\pi}{4}} \sqrt{\left(\frac{\pi}{4}\right)^2 - t^2} dt$$

$$I_1 = \int_{-\frac{\pi}{4}}^{\frac{\pi}{4}} \sqrt{\left(\frac{\pi}{4}\right)^2 - t^2} dt$$

$$I_1 = 2 \int_0^{\frac{\pi}{4}} \sqrt{\left(\frac{\pi}{4}\right)^2 - t^2} dt = 2 \left[ \frac{t}{2} \sqrt{\left(\frac{\pi}{4}\right)^2 - t^2} + \frac{\pi^2}{32} \sin^{-1}\left(\frac{4t}{\pi}\right) \right]_0^{\frac{\pi}{4}}$$

$$I_1 = \frac{\pi^3}{32}$$

$$\text{Now, } I = \frac{8}{\pi^3} I_1$$

$$I = \frac{1}{4} = 0.25$$

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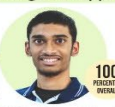
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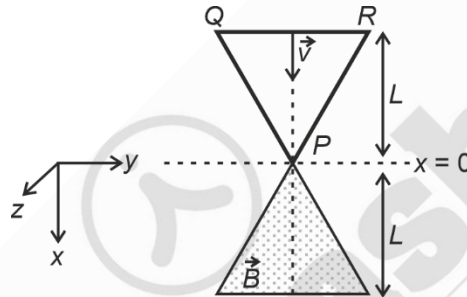
## PART-II : PHYSICS

### SECTION 1 (Maximum Marks : 12)

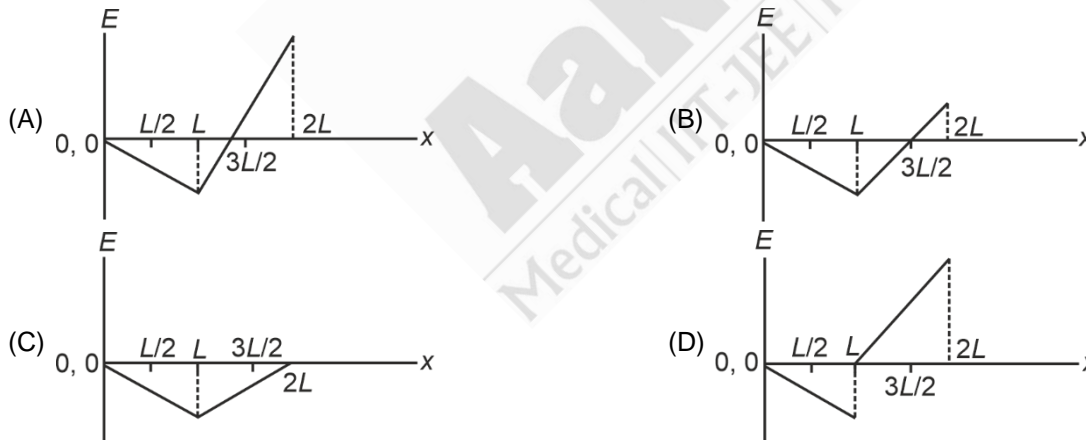
- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:  

Full Marks	:	+3	If <b>ONLY</b> the correct option is chosen;
Zero Marks	:	0	If none of the options is chosen (i.e. the question is unanswered);
Negative Marks	:	-1	In all other cases.

1. A region in the form of an equilateral triangle (in  $x - y$  plane) of height  $L$  has a uniform magnetic field  $\vec{B}$  pointing in the  $+z$ -direction. A conducting loop  $PQR$ , in the form of an equilateral triangle of the same height  $L$ , is placed in the  $x - y$  plane with its vertex  $P$  at  $x = 0$  in the orientation shown in the figure. At  $t = 0$ , the loop starts entering the region of the magnetic field with a uniform velocity  $\vec{v}$  along the  $+x$ -direction. The plane of the loop and its orientation remain unchanged throughout its motion.



Which of the following graph best depicts the variation of the induced emf ( $E$ ) in the loop as a function of the distance ( $x$ ) starting from  $x = 0$ ?



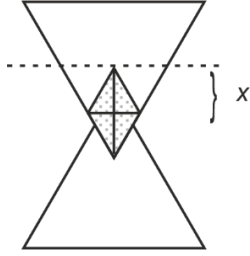
**Answer (A)**

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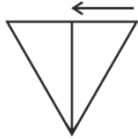
Sol. For  $x < L$



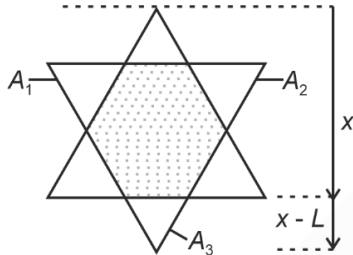
$$\text{Area} = \frac{x}{2} \times \frac{x}{2} \tan 30^\circ \times 4 \times \frac{1}{2} = \frac{1}{2} x^2 \tan 30^\circ$$

$$\phi' = B_0 x \tan 30^\circ \quad \boxed{\varepsilon \propto x}$$

$$L \tan 30^\circ$$



$x \geq L$



$$\begin{aligned} \text{Area} &= A_0 - A_1 - A_2 - A_3 \\ &= A_0 - 2A_1 - (x-L)(x-L) \tan 30^\circ \\ &= A_0 - (x-L)^2 \tan 30^\circ - \left\{ L \tan 30^\circ - (x-L) \tan 30^\circ \right\}^2 \frac{1}{2} \times \frac{1}{2} \tan 60^\circ \times 2 \\ &= A_0 - (x-L)^2 \tan 30^\circ - \tan 30^\circ \{2L-x\}^2 \frac{1}{2} \\ \varepsilon' &= -2(x-L) \tan 30^\circ V - \tan 30^\circ 2(2L-x)(-1)V \\ &= (4L-x-2x+2L) \tan 30^\circ V \\ &= (4L-3x)V \end{aligned}$$

$$\boxed{= 0 \text{ at } x = \frac{4L}{3}}$$

From 1 & 2

1.33 < 1.5

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2. A particle of mass  $m$  is under the influence of the gravitational field of a body of mass  $M$  ( $\gg m$ ). The particle is moving in a circular orbit of radius  $r_0$  with time period  $T_0$  around the mass  $M$ . Then, the particle is subjected to an additional central force, corresponding to the potential energy  $V_c(r) = \alpha/r^3$ , where  $\alpha$  is a positive constant of suitable dimensions and  $r$  is the distance from the center of the orbit. If the particle moves in the same circular orbit of radius  $r_0$  in the combined gravitational potential due to  $M$  and  $V_c(r)$ , but with a new time period  $T_1$ , then  $(T_1^2 - T_0^2) / T_1^2$  is given by

[ $G$  is the gravitational constant.]

(A)  $\frac{3\alpha}{GMr_0^2}$

(B)  $\frac{\alpha}{2GMr_0^2}$

(C)  $\frac{\alpha}{GMr_0^2}$

(D)  $\frac{2\alpha}{GMr_0^2}$

**Answer (A)**

Sol.  $\frac{Gmm}{r_0^2} - \frac{3\alpha m}{r_0^4} = \frac{mv^2}{r_0}$

$$T = \frac{2\pi r_0}{\sqrt{\frac{Gmr_0^2 - 3\alpha}{r_0^3}}}$$

$$T_0^2 = \frac{4\pi^2}{Gm} r_0^3$$

$$\frac{T^2 - T_0^2}{T_1^2} = 1 - \frac{T_0^2}{T_1^2}$$

$$= 1 - \frac{4\pi^2}{Gm} \frac{r_0^3}{4\pi^2 r_0^2} \frac{Gmr_0^2 - 3\alpha}{r_0^3}$$

$$= 1 - 1 + \frac{3\alpha}{Gmr_0^2}$$

$$= \frac{3\alpha}{GMr_0^2}$$

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3. A metal target with atomic number  $Z = 46$  is bombarded with a high energy electron beam. The emission of X-rays from the target is analyzed. The ratio  $r$  of the wavelengths of the  $K_{\alpha}$ -line and the cut-off is found to be  $r = 2$ . If the same electron beam bombards another metal target with  $Z = 41$ , the value of  $r$  will be
- (A) 2.53 (B) 1.27  
(C) 2.24 (D) 1.58

**Answer (A)**

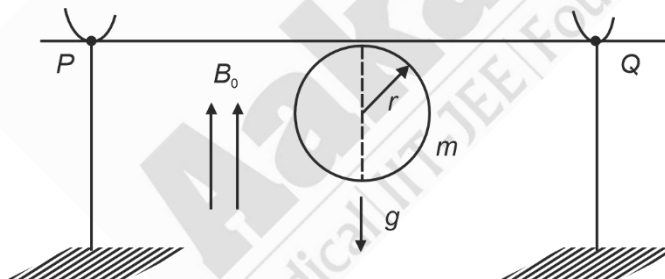
**Sol.**  $\frac{1}{\lambda_{\alpha}} = \frac{3}{4}R(Z-1)^2 p$

$$\lambda_{\text{cut}} = \frac{hc}{eV}$$

$$\Rightarrow \text{Ratio} \propto \frac{1}{(Z-1)^2} \text{ for same beam}$$

$$\frac{Z}{x} = \frac{40^2}{45^2} \Rightarrow x = \frac{45^2}{40^2} \cdot 2 \approx 2.53$$

4. A thin stiff insulated metal wire is bent into a circular loop with its two ends extending tangentially from the same point of the loop. The wire loop has mass  $m$  and radius  $r$  and it is in a uniform vertical magnetic field  $B_0$ , as shown in the figure. Initially, it hangs vertically downwards, because of acceleration due to gravity  $g$ , on two conducting supports at  $P$  and  $Q$ . When a current  $I$  is passed through the loop, the loop turns about the line  $PQ$  by an angle  $\theta$  given by



- (A)  $\tan \theta = \pi r I B_0 / (mg)$   
(B)  $\tan \theta = 2\pi r I B_0 / (mg)$   
(C)  $\tan \theta = \pi r I B_0 / (2mg)$   
(D)  $\tan \theta = mg / (\pi r I B_0)$

**Answer (A)**

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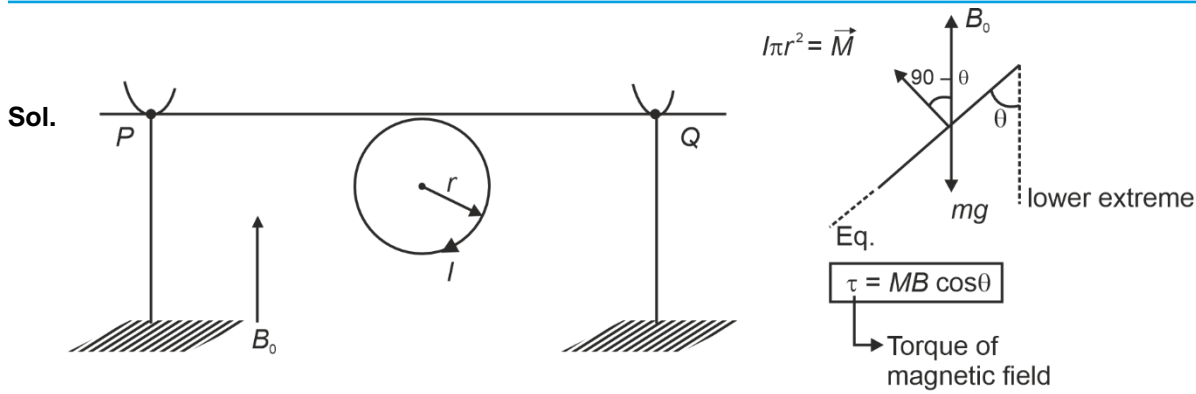
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Now  $\frac{\text{For equilibrium}}{\tau = mg r \sin\theta}$

$$I\pi r^2 B_0 \cos\theta = mgr \sin\theta$$

$$\tan\theta = \frac{I\pi r B_0}{mg}$$

**SECTION 2 (Maximum Marks : 12)**

- This section contains **THREE (03)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks* : +4 **ONLY** if (all) the correct option(s) is(are) chosen;

*Partial Marks* : +3 If all the four options are correct but **ONLY** three options are chosen;

*Partial Marks* : +2 If three or more options are correct but **ONLY** two options are chosen, both of which are correct;

*Partial Marks* : +1 If two or more options are correct but **ONLY** one option is chosen and it is a correct option;

*Zero Marks* : 0 If unanswered;

*Negative Marks* : -2 In all other cases.

5. A small electric dipole  $\vec{p}_0$ , having a moment of inertia  $I$  about its center, is kept at a distance  $r$  from the center of a spherical shell of radius  $R$ . The surface charge density  $\sigma$  is uniformly distributed on the spherical shell. The dipole is initially oriented at a small angle  $\theta$  as shown in the figure. While staying at a distance  $r$ , the dipole is free to rotate about its center.

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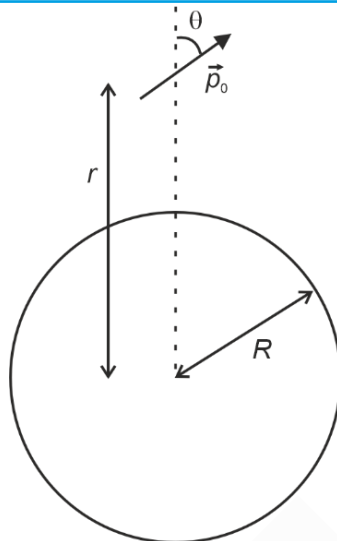
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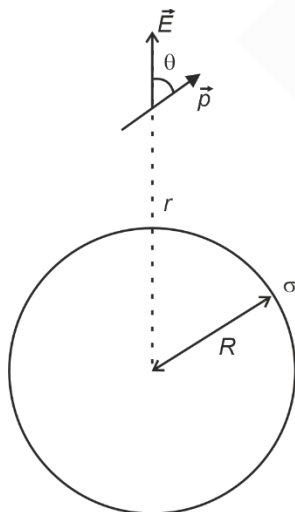
If released from rest, then which of the following statement(s) is (are) correct?

[ $\epsilon_0$  is the permittivity of free space.]

- (A) The dipole will undergo small oscillations at any finite value of  $r$ .
- (B) The dipole will undergo small oscillations at any finite value of  $r > R$ .
- (C) The dipole will undergo small oscillations with an angular frequency of  $\sqrt{\frac{2\sigma\rho_0}{\epsilon_0 l}}$  at  $r = 2R$
- (D) The dipole will undergo small oscillations with an angular frequency of  $\sqrt{\frac{\sigma\rho_0}{100 \epsilon_0 l}}$  at  $r = 10R$

**Answer (B, D)**

**Sol.**



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$$\tau = |\vec{p} \times \vec{E}|$$

$$I\alpha = p_0 E \sin \theta$$

$$\alpha = \frac{p_0 \theta}{I} \left( \frac{1}{4\pi \epsilon_0} \frac{\sigma 4\pi R^2}{r^2} \right)$$

$$\alpha = \left( \frac{p_0 \sigma R^2}{I \epsilon_0 r^2} \right) \cdot \theta$$

$$\therefore \omega = \sqrt{\frac{p_0 \sigma R^2}{I \epsilon_0 r^2}}$$

For  $r = 2R$

$$\omega = \sqrt{\frac{p_0 \sigma}{4I \epsilon_0}} \quad (\text{C is incorrect})$$

Also, for  $r = 10R$

$$\omega = \sqrt{\frac{p_0 \sigma}{4I(100)}} \quad (\text{D is correct})$$

It will oscillate for any finite value of  $r > R$ . (B is correct)

6. A table tennis ball has radius  $(3/2) \times 10^{-2}$  m and mass  $(22/7) \times 10^{-3}$  kg. It is slowly pushed down into a swimming pool to a depth of  $d = 0.7$  m below the water surface and then released from rest. It emerges from the water surface at speed  $v$ , without getting wet, and rises up to a height  $H$ . Which of the following option(s) is (are) correct?

[Given:  $\pi = 22/7$ ,  $g = 10 \text{ ms}^{-2}$ , density of water =  $1 \times 10^3 \text{ kg m}^{-3}$ , viscosity of water =  $1 \times 10^{-3} \text{ Pa-s}$ .]

- (A) The work done in pushing the ball to the depth  $d$  is 0.077 J.  
 (B) If we neglect the viscous force in water, then the speed  $v = 7 \text{ m/s}$ .  
 (C) If we neglect the viscous force in water, then the height  $H = 1.4 \text{ m}$ .  
 (D) The ratio of the magnitudes of the net force excluding the viscous force to the maximum viscous force in water is 500/9.

Answer (A, B, D)

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**Sol.** Work done in pushing the ball

$$W = (v\rho g)d - (v\sigma g)d$$

Where  $\rho \rightarrow$  Density of water

$\sigma \rightarrow$  Density of ball

$$\Rightarrow W = \frac{4}{3}\pi R^3 \times 10 \times 0.7 \left[ 1000 - \frac{3}{4} \times \frac{10^{-3}}{R^3} \right]$$

$$\boxed{W = 0.077 \text{ J}} \quad [\text{A is correct}]$$

$\Rightarrow$  When ball is released at bottom same work (i.e. 0.077 J) is done on ball.

$$\therefore \frac{1}{2}mv^2 = 0.077$$

$$v = \sqrt{\frac{0.077 \times 2}{\frac{22}{7} \times 10^{-3}}}$$

$$= 7 \text{ m/s} \quad [\text{B is correct}]$$

$$\Rightarrow \text{also, } H = \frac{v^2}{2g} = \frac{7 \times 7}{2 \times 10} = 2.45 \text{ m} \quad [\text{C is incorrect}]$$

$$\Rightarrow \text{Net force } F_{\text{net}} = v\sigma g - v\rho g = 0.11 \text{ N}$$

Also, viscous force is maximum when  $v = 7 \text{ m/s}$ .

$$\begin{aligned} \therefore (F_v)_{\text{max}} &= 6\pi\eta rv \\ &= 6 \times \frac{22}{7} \times 10^{-3} \left( \frac{3}{2} \times 10^{-2} \right) \times 7 \\ &= 18 \times 11 \times 10^{-5} \text{ N} \end{aligned}$$

Now,

$$\frac{F_{\text{net}}}{(F_v)_{\text{max}}} = \frac{500}{9} \quad [\text{D is correct}]$$

7. A positive, singly ionized atom of mass number  $A_M$  is accelerated from rest by the voltage 192 V. Thereafter, it enters a rectangular region of width  $w$  with magnetic field  $\vec{B}_0 = 0.1\hat{k}$  Tesla, as shown in the figure. The ion finally hits a detector at the distance  $x$  below its starting trajectory.

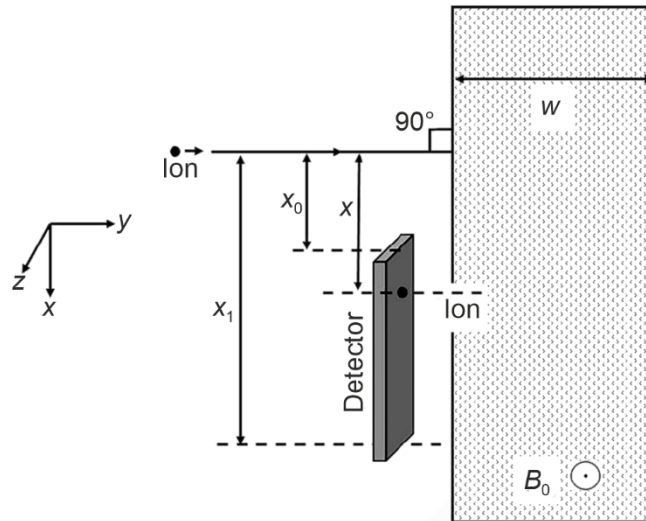
[Given: Mass of neutron/proton =  $(5/3) \times 10^{-27}$  kg, charge of the electron =  $1.6 \times 10^{-19}$  C.]

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Which of the following option(s) is(are) correct?

- (A) The value of  $x$  for  $H^+$  ion is 4 cm.
- (B) The value of  $x$  for an ion with  $A_M = 144$  is 48 cm.
- (C) For detecting ions with  $1 \leq A_M \leq 196$ , the minimum height  $(x_1 - x_0)$  of the detector is 55 cm.
- (D) The minimum width  $w$  of the region of the magnetic field for detecting ions with  $A_M = 196$  is 56 cm.

**Answer (A, B)**

**Sol.**  $x = 2R$

$$= 2 \frac{mv}{qB}$$

$$= 2 \frac{\sqrt{2m(e\Delta V)}}{qB}$$

For  $H^+$  ion

$$x = 3.91 \text{ cm}$$

$$\approx 4 \text{ cm} \quad (\text{A is correct})$$

For  $m = 144$  ( $m_p$ )

$$= 12(x_{H^+})$$

$$= 48 \text{ cm} \quad (\text{B is correct})$$

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For  $1 \leq A_M \leq 196$

$$\begin{aligned} \Rightarrow (x_1 - x_0)_{\min} &= 2R_{196} - 2R_1 \\ &= (14 \times 4) - 4 \\ &= 52 \text{ cm} \quad (\text{C is incorrect}) \end{aligned}$$

For  $A_M = 196$

$$w_{\min} = R_{196} = 28 \text{ cm} \quad (\text{D is incorrect})$$

**SECTION 3 (Maximum Marks : 24)**

- This section contains **SIX (06)** questions.
- The answer to each question is a **NON-NEGATIVE INTEGER**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks* : +4 If **ONLY** the correct integer is entered;

*Zero Marks* : 0 In all other cases.

8. The dimensions of a cone are measured using a scale with a least count of 2 mm. The diameter of the base and the height are both measured to be 20.0 cm. The maximum percentage error in the determination of the volume is \_\_\_\_\_.

**Answer (3)**

**Sol.**  $V = \frac{1}{3} \pi R^2 H$

$$\Rightarrow \frac{dV}{V} = 2 \cdot \frac{dR}{R} + \frac{dH}{H}$$

$\Rightarrow$  % error in measuring volume

$$\begin{aligned} &= \left[ 2 \times \frac{0.2}{20} + \frac{0.2}{20} \right] \times 100 \\ &= 3 \end{aligned}$$

9. A ball is thrown from the location  $(x_0, y_0) = (0,0)$  of a horizontal playground with an initial speed  $v_0$  at an angle  $\theta_0$  from the  $+x$ -direction. The ball is to be hit by a stone, which is thrown at the same time from the location  $(x_1, y_1) = (L, 0)$ . The stone is thrown at an angle  $(180 - \theta_1)$  from the  $+x$ -direction with a suitable initial speed. For a fixed  $v_0$ , when  $(\theta_0, \theta_1) = (45^\circ, 45^\circ)$ , the stone hits the ball after time  $T_1$ , and when  $(\theta_0, \theta_1) = (60^\circ, 30^\circ)$ , it hits the ball after time  $T_2$ . In such a case,  $(T_1/T_2)^2$  is \_\_\_\_\_.

**Answer (2)**

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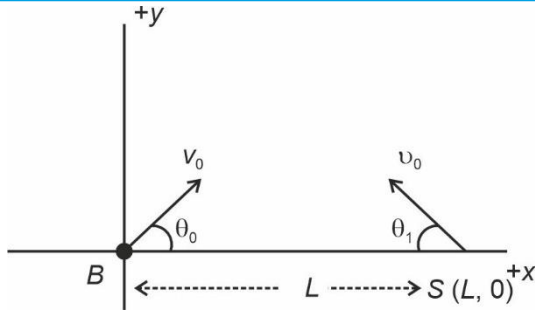
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Sol.



Let  $B$  : Ball

$S$  : Stone

$v_0$  : Initial speed of stone.

Since relative acceleration = zero

⇒ Path seen would be straight line

⇒ To meet,  $v_0 \sin \theta_0 = v_0 \sin \theta_1$

$$\text{And } \Delta t = \frac{L}{v_0 \cos \theta_1 + v_0 \cos \theta_0}$$

$$\text{Case I : } v_0 = v_0 \Rightarrow \Delta t_1 = T_1 = \frac{L}{v_0 \left[ \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}} \right]} = \frac{L}{\sqrt{2}v_0}$$

$$\text{Case II : } \sqrt{3}v_0 = v_0 \Rightarrow \Delta t_2 = T_2 = \frac{L}{\sqrt{3}v_0 \cdot \frac{\sqrt{3}}{2} + \frac{v_0}{2}} = \frac{L}{2v_0}$$

$$\Rightarrow \left( \frac{T_1}{T_2} \right)^2 = (\sqrt{2})^2 = 2$$

10. A charge is kept at the central point  $P$  of a cylindrical region. The two edges subtend a half-angle  $\theta$  at  $P$ , as shown in the figure. When  $\theta = 30^\circ$ , then the electric flux through the curved surface of the cylinder is  $\Phi$ . If  $\theta = 60^\circ$ , then the electric flux through the curved surface becomes  $\Phi / \sqrt{n}$ , where the value of  $n$  is \_\_\_\_\_.

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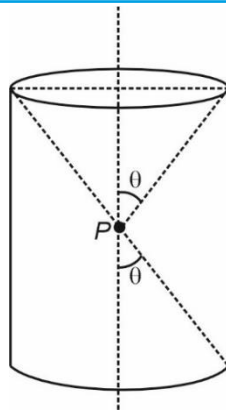
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**Answer (3)**

**Sol.** For any  $\theta$ , let us first find the flux inside a cone of half angle  $\theta$ . we know that for such a cone, solid angle subtended at centre is

$$\Omega = 2\pi [1 - \cos\theta]$$

$$\Rightarrow \text{Flux through 1 cone} = \phi_0 = \frac{\Omega}{4\pi} \cdot \frac{Q}{\epsilon_0} = \frac{Q}{2\epsilon_0} [1 - \cos\theta]$$

$\Rightarrow$  Flux through curved surface

$$= \frac{Q}{\epsilon_0} - 2\phi_0$$

$$= \frac{Q}{\epsilon_0} - \frac{Q}{\epsilon_0} [1 - \cos\theta] = \frac{Q}{\epsilon_0} \cos\theta$$

$$\Rightarrow \phi = \frac{Q}{\epsilon_0} \cdot \frac{\sqrt{3}}{2}$$

And  $\frac{\phi}{\sqrt{n}} = \frac{Q}{\epsilon_0} \cdot \frac{1}{2}$

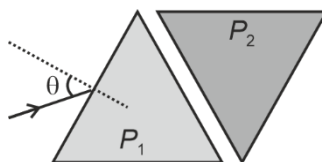
$$\Rightarrow \sqrt{n} = \sqrt{3}$$

$$\Rightarrow n = 3$$

11. Two equilateral-triangular prisms  $P_1$  and  $P_2$  are kept with their sides parallel to each other, in vacuum, as shown in the figure. A light ray enters prism  $P_1$  at an angle of incidence  $\theta$  such that the outgoing ray undergoes minimum

deviation in prism  $P_2$ . If the respective refractive indices of  $P_1$  and  $P_2$  are  $\sqrt{\frac{3}{2}}$  and  $\sqrt{3}$ ,  $\theta = \sin^{-1} \left[ \sqrt{\frac{3}{2}} \sin \left( \frac{\pi}{\beta} \right) \right]$ ,

where the value of  $\beta$  is \_\_\_\_\_.



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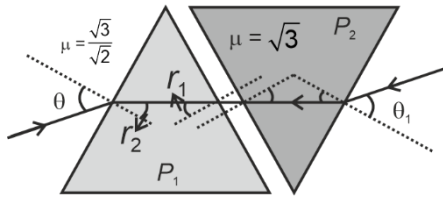
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**Answer (12)**

**Sol.** By using optical reversibility principle



For prism  $P_2$

→ Minimum deviation

$$1 \times \sin \theta_1 = \sqrt{3} \sin r \quad r_1 = r_2 = \frac{A}{2}$$

$$\sin \theta_1 = \sqrt{3} \times \frac{1}{2} \quad r_1 = r_2 = 30^\circ$$

$$\Rightarrow i = e = 60^\circ$$

For prism  $P_1$

Incident angle will be  $60^\circ$

$$1 \times \sin 60^\circ = \frac{\sqrt{3}}{\sqrt{2}} \sin r_1$$

$$\frac{\sqrt{3}}{2} = \frac{\sqrt{3}}{\sqrt{2}} \sin r_1$$

$$r_1 + r_2 = 60^\circ$$

$$\sin r_1 = \frac{1}{\sqrt{2}}$$

$$r_1 = 45^\circ$$

$$r_2 = 15^\circ$$

$$\frac{\sqrt{3}}{\sqrt{2}} \sin(45^\circ) = 1 \times \sin \theta$$

$$15^\circ = \frac{\pi \times 15}{180} \text{ rad} = \frac{\pi}{12} \text{ rad}$$

$$\theta = \sin^{-1} \left[ \frac{\sqrt{3}}{\sqrt{2}} \sin \left( \frac{\pi}{12} \right) \right]$$

$$\beta = 12$$

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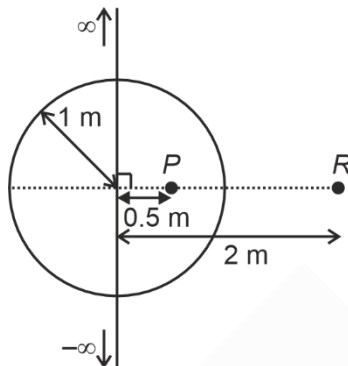
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12. An infinitely long thin wire, having a uniform charge density per unit length of  $5 \text{ nC/m}$ , is passing through a spherical shell of radius  $1 \text{ m}$ , as shown in the figure. A  $10 \text{ nC}$  charge is distributed uniformly over the spherical shell. If the configuration of the charges remains static, the magnitude of the potential difference between points  $P$  and  $R$ , in Volt, is \_\_\_\_\_.

[Given: In SI units  $\frac{1}{4\pi\epsilon_0} = 9 \times 10^9$ ,  $\ln 2 = 0.7$ . Ignore the area pierced by the wire.]



**Answer (171)**

**Sol.**  $E_{\text{Line charge}} = \frac{\lambda}{2\pi\epsilon_0 r}$

$$\Rightarrow \Delta V_{\text{Line charge}} = \int_{0.5}^2 \frac{\lambda}{2\pi\epsilon_0 r} dr = \frac{\lambda}{2\pi\epsilon_0} \ln 4 \quad \dots(i)$$

$$\begin{aligned} \Delta V_{\text{Sphere}} &= \frac{1}{4\pi\epsilon_0} \frac{Q}{R} - \frac{1}{4\pi\epsilon_0} \frac{Q}{2R} \\ &= \frac{1}{4\pi\epsilon_0} \frac{Q}{2} \quad \dots(ii) \end{aligned}$$

$$\begin{aligned} \Rightarrow \Delta V_{\text{Net}} &= \frac{\lambda}{2\pi\epsilon_0} \ln 4 + \frac{1}{4\pi\epsilon_0} \frac{Q}{2} \\ &= 171 \text{ Volts} \end{aligned}$$

13. A spherical soap bubble inside an air chamber at pressure  $P_0 = 10^5 \text{ Pa}$  has a certain radius so that the excess pressure inside the bubble is  $\Delta P = 144 \text{ Pa}$ . Now, the chamber pressure is reduced to  $8P_0/27$  so that the bubble radius and its excess pressure change. In this process, all the temperatures remain unchanged. Assume air to be an ideal gas and the excess pressure  $\Delta P$  in both the cases to be much smaller than the chamber pressure. The new excess pressure  $\Delta P$  in Pa is

**Answer (96)**

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Sol. Since the situation follow isothermal condition.

$$P_1 V_1 = P_2 V_2$$

$$V_1 = \frac{4}{3} \pi R_1^3, V_2 = \frac{4}{3} \pi R_2^3$$

$$P_1 = P_0 + \Delta P_1, \Delta P_1 = \frac{4T}{R_1}$$

$$\text{and } P_2 = \frac{8P_0}{27} + \Delta P_2, \Delta P_2 = \frac{4T}{R_2}$$

So for isothermal condition

$$(P_0 + \Delta P_1) \times \frac{4}{3} \pi R_1^3 = \left( \frac{8P_0}{27} + \Delta P_2 \right) \times \frac{4}{3} \pi R_2^3$$

$$\text{here } P_0 = 10^5 \text{ Pa}$$

$$\Delta P_1 = 144 \text{ Pa}$$

$$\text{and } \Delta P_1 \ll P_0$$

$$\text{So } (P_0 + \Delta P_1) \left( \frac{4T}{\Delta P_1} \right)^3 = \left( \frac{8P_0}{27} + \Delta P_2 \right) \left( \frac{4T}{\Delta P_2} \right)^3$$

$$\frac{P_0}{(\Delta P_1)^3} \approx \frac{8P_0}{27} \times \frac{1}{(\Delta P_2)^3}$$

$$\Delta P_2 = \frac{2}{3} \Delta P_1 = \frac{2}{3} \times (144 \text{ Pa})$$

$$\Delta P_2 = 96 \text{ Pa}$$

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**SECTION 4 (Maximum Marks : 12)**

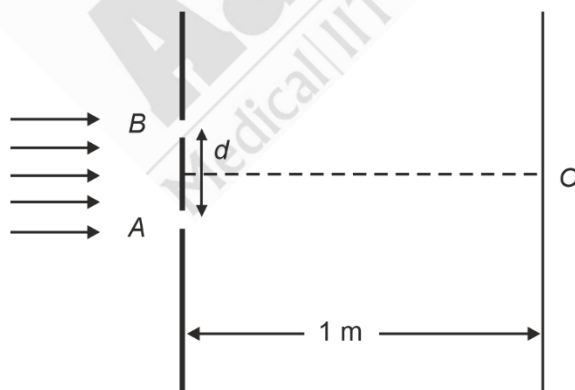
- This section contains **TWO (02)** paragraphs.
- Based on each paragraph, there are **TWO (02)** questions.
- The answer to each question is a **NUMERICAL VALUE**.
- For each question, enter the correct numerical value of the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- If the numerical value has more than two decimal places, **truncate/round-off** the value to **TWO** decimal places.
- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks* : +3 If **ONLY** the correct numerical value is entered in the designated place;

*Zero Marks* : 0 In all other cases.

PARAGRAPH I

In a Young's double slit experiment, each of the two slits *A* and *B*, as shown in the figure, are oscillating about their fixed center and with a mean separation of 0.8 mm. The distance between the slits at time *t* is given by  $d = (0.8 + 0.04 \sin \omega t)$  mm, where  $\omega = 0.08 \text{ rad s}^{-1}$ . The distance of the screen from the slits is 1 m and the wavelength of the light used to illuminate the slits is  $6000 \text{ \AA}$ . The interference pattern on the screen changes with time, while the central bright fringe (zeroth fringe) remains fixed at point *O*.



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14. The 8<sup>th</sup> bright fringe above the point O oscillates with time between two extreme positions. The separation between these two extreme positions, in micrometer ( $\mu\text{m}$ ), is \_\_\_\_\_.

**Answer (601.50)**

**Sol.** As central bright fringe position is not changing, the two slits are oscillating with a phase diff of  $\pi$ .

For 8<sup>th</sup> bright fringe

$$y = \frac{8\lambda D}{(0.8 + 0.04 \sin \omega t)} \times 10^3$$

$$= \frac{8 \times 6000 \times 10^{-10} \times 10^3}{(0.8 + 0.04 \sin \omega t)}$$

$$y = \frac{48 \times 10^{-4}}{(0.8 + 0.04 \sin \omega t)}$$

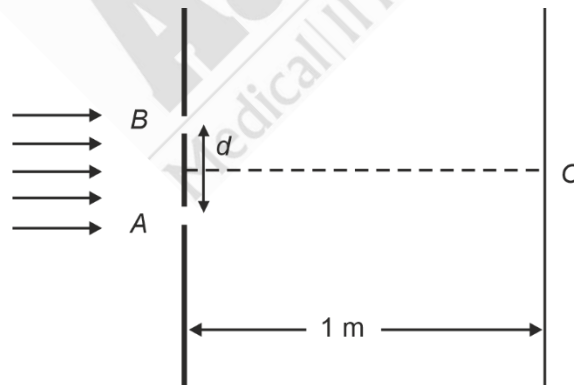
$d$  varies from 0.84 mm to 0.76 mm

$$\Delta y = 6.015 \times 10^{-4}$$

$$= 601.50 \mu\text{m}$$

PARAGRAPH I

In a Young's double slit experiment, each of the two slits A and B, as shown in the figure, are oscillating about their fixed center and with a mean separation of 0.8 mm. The distance between the slits at time  $t$  is given by  $d = (0.8 + 0.04 \sin \omega t)$  mm, where  $\omega = 0.08 \text{ rad s}^{-1}$ . The distance of the screen from the slits is 1 m and the wavelength of the light used to illuminate the slits is  $6000 \text{ \AA}$ . The interference pattern on the screen changes with time, while the central bright fringe (zeroth fringe) remains fixed at point O.



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15. The maximum speed in  $\mu$  m/s at which the 8<sup>th</sup> bright fringe will move is \_\_\_\_\_.

**Answer (24.00)**

**Sol.** Finding speed

$$\frac{\delta y}{\delta t} = \frac{\delta}{\delta t} \left( \frac{8\lambda D}{d} \right)$$

$$= -\frac{8\lambda D}{d^2} \frac{\delta d}{(\delta t)}$$

$$v = -\frac{8\lambda D}{d^2} (0.04\omega \cos \omega t) \times 10^{-3}$$

$$v_{\max} = \frac{8\lambda D}{d^2} \times 4\omega \times 10^{-5}$$

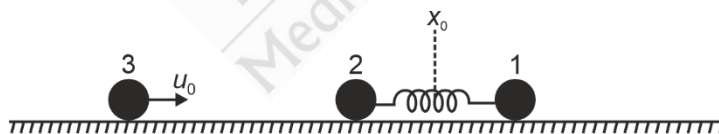
$$= \frac{8 \times 6 \times 10^{-7} \times 1 \times 4 \times 8 \times 10^{-7}}{64 \times 10^{-8}}$$

$$= 24 \times 10^{-6}$$

$$= 24 \mu\text{m/s}$$

PARAGRAPH II

Two particles, 1 and 2, each of mass  $m$ , are connected by a massless spring, and are on a horizontal frictionless plane, as shown in the figure. Initially, the two particles, with their center of mass at  $x_0$ , are oscillating with amplitude  $a$  and angular frequency  $\omega$ . Thus, their positions at time  $t$  are given by  $x_1(t) = (x_0 + d) + a \sin \omega t$  and  $x_2(t) = (x_0 - d) - a \sin \omega t$ , respectively, where  $d > 2a$ . Particle 3 of mass  $m$  moves towards this system with speed  $u_0 = a\omega/2$ , and undergoes instantaneous elastic collision with particle 2, at time  $t_0$ . Finally, particles 1 and 2 acquire a center of mass speed  $v_{\text{cm}}$  and oscillate with amplitude  $b$  and the same angular frequency  $\omega$ .



16. If the collision occurs at time  $t_0 = 0$ , the value of  $v_{\text{cm}}/(a\omega)$  will be \_\_\_\_\_.

**Answer (00.75)**

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Sol. At  $t = 0$ , 2 is at mean position

$\therefore u_2 = a\omega$  towards left after collision, velocity will exchange

$\therefore v_2 = \frac{a\omega}{2}$  towards right

$u_1 = a\omega$  towards right

$\therefore v_{cm} = \frac{3a\omega}{4}$

$$\frac{v_{cm}}{a\omega} = \frac{3}{4} = 0.75$$

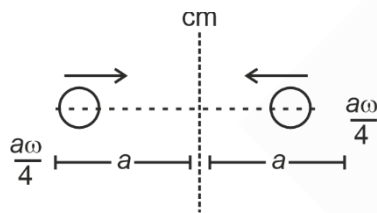
At  $t = \frac{\pi}{2\omega}$ ,  $u_2 = 0$

After collision,  $v_2 = \frac{a\omega}{2}$  towards right

$u_1 = 0$

$\therefore v_{cm} = \frac{a\omega}{4}$  towards right

w.r.t. centre of mass



$$v = \omega\sqrt{A^2 - x^2}$$

$$\frac{a\omega}{4} = \omega\sqrt{A^2 - a^2}$$

$$\frac{a^2}{16} + a^2 = A^2$$

$$\frac{17}{16}a^2 = A^2 = b^2$$

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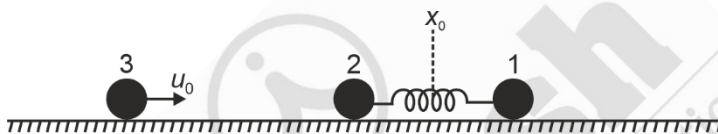
$$\therefore b^2 = \frac{17}{16}a^2$$

$$\frac{4b^2}{a^2} = \frac{17}{4}$$

$$= 4.25$$

PARAGRAPH II

Two particles, 1 and 2, each of mass  $m$ , are connected by a massless spring, and are on a horizontal frictionless plane, as shown in the figure. Initially, the two particles, with their center of mass at  $x_0$ , are oscillating with amplitude  $a$  and angular frequency  $\omega$ . Thus, their positions at time  $t$  are given by  $x_1(t) = (x_0 + d) + a \sin \omega t$  and  $x_2(t) = (x_0 - d) - a \sin \omega t$ , respectively, where  $d > 2a$ . Particle 3 of mass  $m$  moves towards this system with speed  $u_0 = a\omega/2$ , and undergoes instantaneous elastic collision with particle 2, at time  $t_0$ . Finally, particles 1 and 2 acquire a center of mass speed  $v_{cm}$  and oscillate with amplitude  $b$  and the same angular frequency  $\omega$ .



17. If the collision occurs at time  $t_0 = \pi/(2\omega)$ , then the value of  $4b^2/a^2$  will be \_\_\_\_\_.

**Answer (04.25)**

**Sol.** At  $t = 0$ , 2 is at mean position

$\therefore u_2 = a\omega$  towards left after collision, velocity will exchange

$\therefore v_2 = \frac{a\omega}{2}$  towards right

$u_1 = a\omega$  towards right

$\therefore v_{cm} = \frac{3a\omega}{4}$

$\frac{v_{cm}}{a\omega} = \frac{3}{4} = 0.75$

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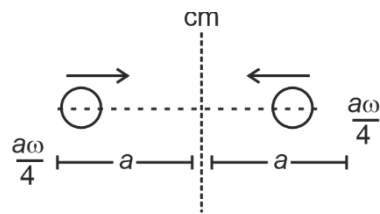
At  $t = \frac{\pi}{2\omega}$ ,  $u_2 = 0$

After collision,  $v_2 = \frac{a\omega}{2}$  towards right

$u_1 = 0$

$\therefore v_{cm} = \frac{a\omega}{4}$  towards right

w.r.t.



$v = \omega\sqrt{A^2 - x^2}$

$\frac{a\omega}{4} = \omega\sqrt{A^2 - a^2}$

$\frac{a^2}{16} + a^2 = A^2$

$\frac{17}{16}a^2 = A^2 = b^2$

$\therefore b^2 = \frac{17}{16}a^2$

$\frac{4b^2}{a^2} = \frac{17}{4}$

$= 4.25$

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## PART-III : CHEMISTRY

### SECTION 1 (Maximum Marks : 12)

- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks* : +3 If **ONLY** the correct option is chosen;

*Zero Marks* : 0 If none of the options is chosen (i.e. the question is unanswered);

*Negative Marks* : -1 In all other cases.

1. According to Bohr's model, the highest kinetic energy is associated with the electron in the
- First orbit of H atom
  - First orbit of He<sup>+</sup>
  - Second orbit of He<sup>+</sup>
  - Second orbit of Li<sup>2+</sup>

#### Answer (B)

**Sol.** K.E. of electron in n<sup>th</sup> Bohr's orbit,

$$\text{K.E.} = 13.6 \frac{Z^2}{n^2} \text{ eV/atom}$$

$$n = 1 \text{ (H-atom)} \rightarrow \text{K.E.} \propto \frac{1^2}{1^2} = 1$$

$$n = 1 \text{ (He}^+ \text{ ion)} \rightarrow \text{K.E.} \propto \frac{2^2}{1^2} = 4$$

$$n = 2 \text{ (He}^+ \text{ ion)} \rightarrow \text{K.E.} \propto \frac{2^2}{2^2} = 1$$

$$n = 2 \text{ (Li}^{2+} \text{ ion)} \rightarrow \text{K.E.} \propto \frac{3^2}{2^2} = \frac{9}{4}$$

Highest for  $\rightarrow n = 1$  of He<sup>+</sup> ion.

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2. In a metal deficient oxide sample,  $M_xY_2O_4$  ( $M$  and  $Y$  are metals),  $M$  is present in both +2 and +3 oxidation states and  $Y$  is in +3 oxidation state. If the fraction of  $M^{2+}$  ions present in  $M$  is  $\frac{1}{3}$ , the value of  $X$  is \_\_\_\_\_.

- (A) 0.25 (B) 0.33  
(C) 0.67 (D) 0.75

**Answer (D)**

**Sol.**  $M_xY_2O_4$

$$M^{+2} = \frac{X}{3}, M^{+3} = \frac{2X}{3}$$

So, total of O.N. of all atoms

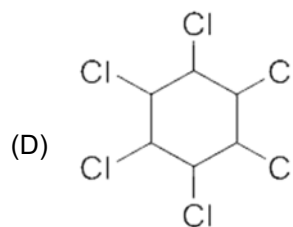
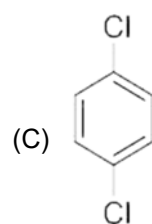
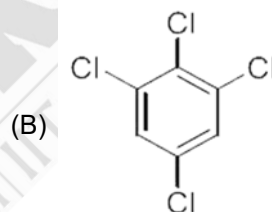
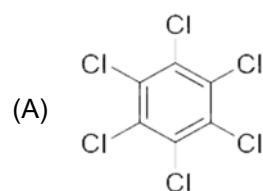
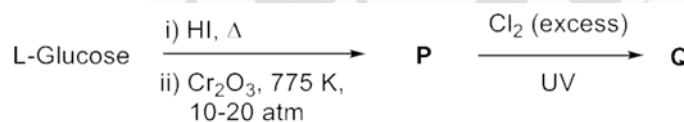
$$\frac{2X}{3} + 3\left(\frac{2X}{3}\right) + 2(+3) + 4(-2) = 0$$

$$\frac{2X}{3} + 2X + 6 - 8 = 0$$

$$\frac{8X}{3} = 2$$

$$X = \frac{6}{8} = \frac{3}{4} = 0.75$$

3. In the following reaction sequence, the major product **Q** is



**Answer (D)**

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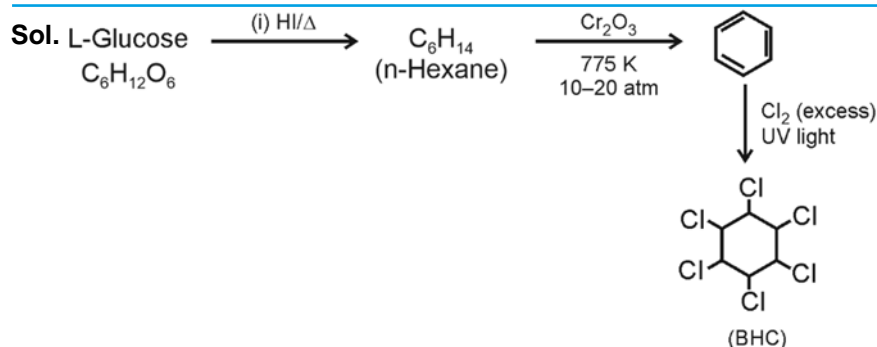
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4. The species formed on fluorination of phosphorus pentachloride in a polar organic solvent are

- (A)  $[\text{PF}_4]^+[\text{PF}_6]^-$  and  $[\text{PCl}_4]^+[\text{PF}_6]^-$   
 (B)  $[\text{PCl}_4]^+[\text{PCl}_4\text{F}_2]^-$  and  $[\text{PCl}_4]^+[\text{PF}_6]^-$   
 (C)  $\text{PF}_3$  and  $\text{PCl}_3$   
 (D)  $\text{PF}_5$  and  $\text{PCl}_3$

**Answer (B)**

Sol. If  $\text{PCl}_5$  is fluorinated in a polar solvent, ionic isomers are formed. e.g.:-

$[\text{PCl}_4]^+[\text{PCl}_4\text{F}_2]^-$  (colourless crystals)  
 and  $[\text{PCl}_4]^+[\text{PF}_6]^-$  (white crystals)

**SECTION 2 (Maximum Marks : 12)**

- This section contains **THREE (03)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONE OR MORE THAN ONE** of these four option(s) is(are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

*Full Marks* : +4 **ONLY** if (all) the correct option(s) is(are) chosen;

*Partial Marks* : +3 If all the four options are correct but **ONLY** three options are chosen;

*Partial Marks* : +2 If three or more options are correct but **ONLY** two options are chosen, both of which are correct;

*Partial Marks* : +1 If two or more options are correct but **ONLY** one option is chosen and it is a correct option;

*Zero Marks* : 0 If unanswered;

*Negative Marks* : -2 In all other cases.

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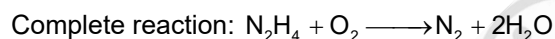
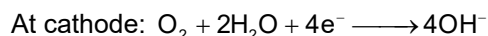
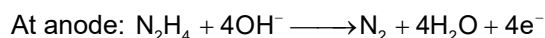
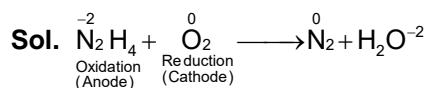
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5. An aqueous solution of hydrazine ( $N_2H_4$ ) is electrochemically oxidized by  $O_2$ , thereby releasing chemical energy in the form of electrical energy. One of the products generated from the electrochemical reaction is  $N_2(g)$ .

Choose the correct statement(s) about the above process

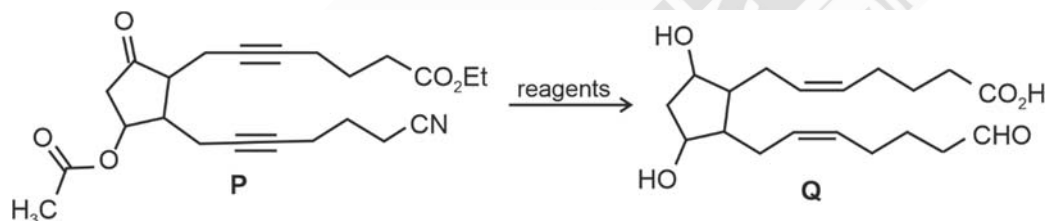
- (A)  $OH^-$  ions react with  $N_2H_4$  at the anode to form  $N_2(g)$  and water, releasing 4 electrons to the anode.  
 (B) At the cathode,  $N_2H_4$  breaks to  $N_2(g)$  and nascent hydrogen released at the electrode reacts with oxygen to form water.  
 (C) At the cathode, molecular oxygen gets converted to  $OH^-$ .  
 (D) Oxides of nitrogen are major by-products of the electrochemical process.

**Answer (A, C)**



Statements (A) and (C) are correct.

6. The option(s) with correct sequence of reagents for the conversion of **P** to **Q** is(are)



- (A) i) Lindlar's catalyst,  $H_2$ ; ii)  $SnCl_2/HCl$ ; iii)  $NaBH_4$ ; iv)  $H_3O^+$   
 (B) i) Lindlar's catalyst,  $H_2$ ; ii)  $H_3O^+$ ; iii)  $SnCl_2/HCl$ ; iv)  $NaBH_4$   
 (C) i)  $NaBH_4$ ; ii)  $SnCl_2/HCl$ ; iii)  $H_3O^+$ ; iv) Lindlar's catalyst,  $H_2$   
 (D) i) Lindlar's catalyst,  $H_2$ ; ii)  $NaBH_4$ ; iii)  $SnCl_2/HCl$ ; iv)  $H_3O^+$

**Answer (A, C, D)**

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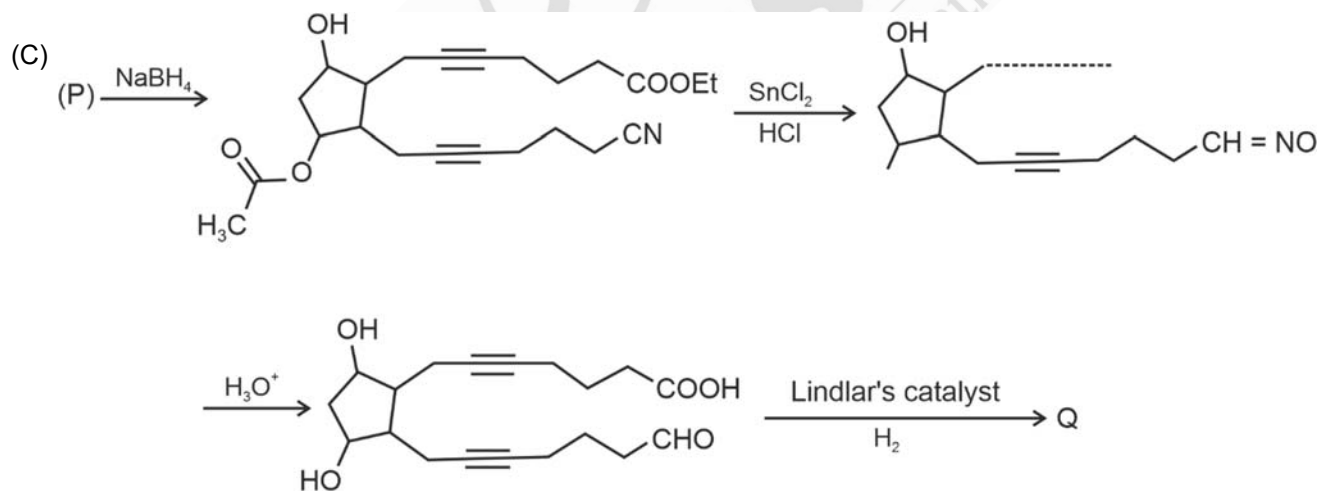
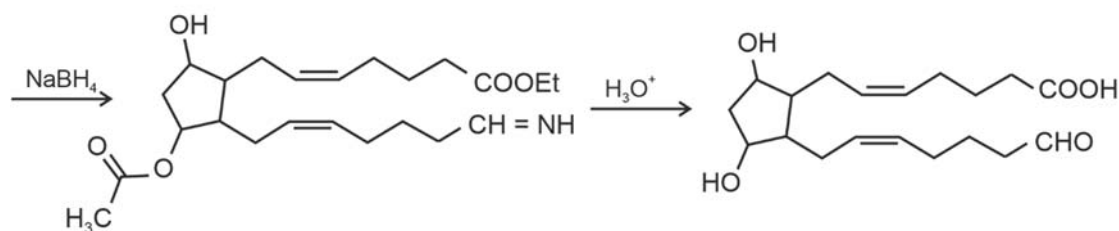
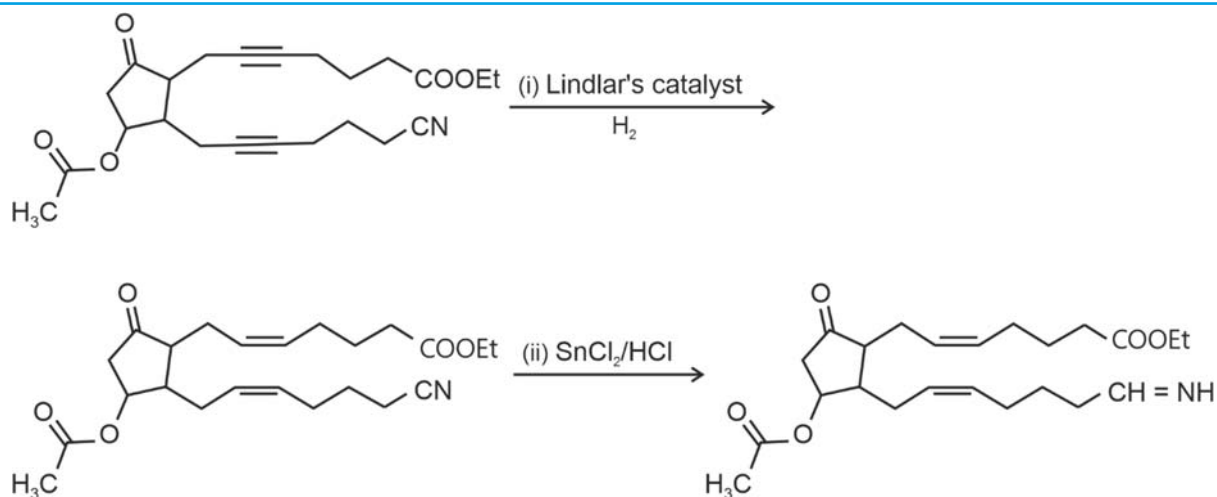


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Sol. (A)



(D) (P)  $\xrightarrow{\text{(i) Lindlar's catalyst, } H_2; \text{ (ii) } NaBH_4; \text{ (iii) } SnCl_2/HCl; \text{ (iv) } H_3O^+}$  (Q)

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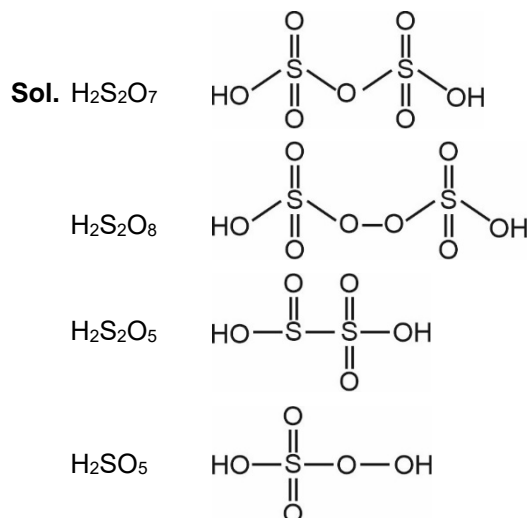
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7. The compound(s) having peroxide linkage is(are)

- (A)  $\text{H}_2\text{S}_2\text{O}_7$  (B)  $\text{H}_2\text{S}_2\text{O}_8$   
 (C)  $\text{H}_2\text{S}_2\text{O}_5$  (D)  $\text{H}_2\text{SO}_5$

Answer (B, D)



### SECTION 3 (Maximum Marks : 24)

- This section contains **SIX (06)** questions.
- The answer to each question is a **NON-NEGATIVE INTEGER**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated according to the following marking scheme:

Full Marks : +4 If **ONLY** the correct integer is entered;

Zero Marks : 0 In all other cases.

8. To form a complete monolayer of acetic acid on 1 g of charcoal, 100 mL of 0.5 M acetic acid was used. Some of the acetic acid remained unadsorbed. To neutralize the unadsorbed acetic acid, 40 mL of 1 M NaOH solution was required. If each molecule of acetic acid occupies  $P \times 10^{-23} \text{ m}^2$  surface area on charcoal, the value of P is \_\_\_\_\_.

[Use given data : Surface area of charcoal =  $1.5 \times 10^2 \text{ m}^2 \text{ g}^{-1}$ ; Avogadro's number ( $N_A$ ) =  $6.0 \times 10^{23} \text{ mol}^{-1}$ ]

Answer (2500)

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**Sol.** Number of moles of unadsorbed  $\text{CH}_3\text{COOH} = \frac{40 \times 1}{1000} = 4 \times 10^{-2} \text{ mol}$

$$\begin{aligned} \text{Number of moles of adsorbed } \text{CH}_3\text{COOH} &= \frac{100 \times 0.5}{1000} - 4 \times 10^{-2} \\ &= 10^{-2} \text{ mol} \end{aligned}$$

Surface area occupied by one molecule of

$$\text{CH}_3\text{COOH} = \frac{1.5 \times 10^2}{10^{-2} \times 6 \times 10^{23}} = \frac{150 \times 10^2 \times 10^{-23}}{6}$$

$$= 2500 \times 10^{-23} \text{ m}^2$$

$\therefore$  As per question  $P = 2500$

9. Vessel-1 contains  $w_2$  g of a non-volatile solute **X** dissolved in  $w_1$  g of water. Vessel-2 contains  $w_2$  g of another non-volatile solute **Y** dissolved in  $w_1$  g of water. Both the vessels are at the same temperature and pressure. The molar mass of **X** is 80% of that of **Y**. The van't Hoff factor for **X** is 1.2 times of that of **Y** for their respective concentrations.

The elevation of boiling point for solution in Vessel-1 is \_\_\_\_\_ % of the solution in Vessel-2.

**Answer (150)**

**Sol. Vessel-I**

$$(\Delta T_B)_I = i_X \frac{w_2}{M_X} \cdot \frac{1}{w_1} \times 1000 \times K_b$$

$M_X$  = Molar mass of 'X'

**Vessel-II**

$$(\Delta T_B)_{II} = i_Y \frac{w_2}{M_Y} \cdot \frac{1}{w_1} \times 1000 \times K_B$$

$M_Y$  = Molar mass of 'Y'

$$\begin{aligned} \frac{(\Delta T_b)_I}{(\Delta T_b)_{II}} \times 100 &= \frac{i_X \cdot M_Y}{i_Y \cdot M_X} \times 100 \\ &= 1.2 \times \frac{100}{80} \times 100 \\ &= 150\% \end{aligned}$$

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10. For a double strand DNA, one strand is given below:



The amount of energy required to split the double strand DNA into two single strands is \_\_\_\_\_ kcal mol<sup>-1</sup>.

[Given: Average energy per H-bond for A-T base pair = 1.0 kcal mol<sup>-1</sup>, G-C base pair = 1.5 kcal mol<sup>-1</sup>, and A-U base pair = 1.25 kcal mol<sup>-1</sup>. Ignore electrostatic repulsion between the phosphate groups.]

**Answer (41)**



Total energy = [BE H-bond A – T × No. of A = T pair × 2 ] + [BE H-bond G – C × No. of G ≡ C pair × 3]

= [1 × 7 × 2] + [1.5 × 6 × 3]

= 14 + 27

= 41 kcal

11. A sample initially contains only U-238 isotope of uranium. With time, some of the U-238 radioactively decays into Pb-206 while the rest of it remains undisintegrated.

When the age of the sample is **P** × 10<sup>8</sup> years, the ratio of mass of Pb-206 to that of U-238 in the sample is found to be 7. The value of **P** is\_\_\_\_\_.

[Given : Half-life of U-238 is 4.5 × 10<sup>9</sup> years; log<sub>e</sub>2 = 0.693]

**Answer (143)**

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Sol. Life of sample  $\rightarrow t$  years

$[A]_0 \propto$  Initial mole of U-238

$[A]_t \propto$  Final mole of U-238

$$\frac{[A]_0}{[A]_t} = \frac{\frac{1}{238} + \frac{7}{206}}{\frac{1}{238}}$$

$$= \frac{0.0042 + 0.0340}{0.0042}$$

$$= 9.1$$

$$= \frac{2.303 \log 2 \times t}{4.5 \times 10^9} = 2.303 \log 9.1$$

$$t = 14.27 \times 10^9 \text{ years}$$

$$= 142.7 \times 10^9 \text{ years}$$

$$P = 142.7$$

$$P \approx 143$$

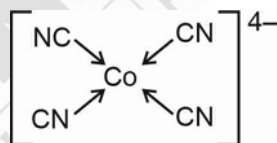
12. Among  $[\text{Co}(\text{CN})_4]^{4-}$ ,  $[\text{Co}(\text{CO})_3(\text{NO})]$ ,  $\text{XeF}_4$ ,  $[\text{PCl}_4]^+$ ,  $[\text{PdCl}_4]^{2-}$ ,  $[\text{ICl}_4]^-$ ,  $[\text{Cu}(\text{CN})_4]^{3-}$  and  $\text{P}_4$  the total number of species with tetrahedral geometry is \_\_\_\_\_.

Answer (3)

Sol.  $[\text{Co}(\text{CN})_4]^{4-} \Rightarrow \text{Co}^0 \Rightarrow 3d^7 4s^2$

Due to SFL,  $\text{CN}^-$  pairing and transference of electron takes place and hybridisation is  $dsp^2$

Geometry  $\Rightarrow$  Square planer

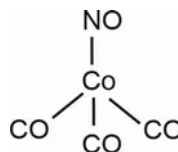


$[\text{Co}(\text{CO})_3\text{NO}]$

$\text{Co}^{-1} \Rightarrow 3d^{10}$  due to SFL CO and NO

$sp^3$  hybridisation

Geometry = Tetrahedral



$\text{XeF}_4 \Rightarrow 4bp + 2lp \Rightarrow sp^3d^2$

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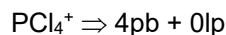
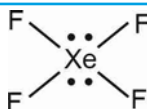


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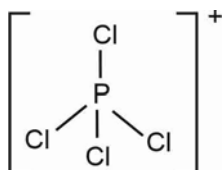


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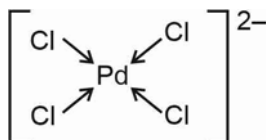
Square planer



$sp^3 \Rightarrow$  tetrahedral

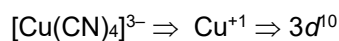
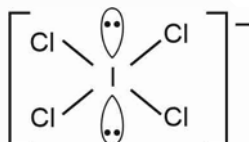


$\text{Pd}^{2+} \Rightarrow 4d^8 \Rightarrow dsp^2 \Rightarrow$  square planer



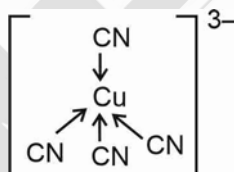
$sp^3d^2$

square planer



$\Rightarrow sp^3$

Tetrahedral



13. An organic compound **P** having molecular formula  $\text{C}_6\text{H}_6\text{O}_3$  gives ferric chloride test and does not have intramolecular hydrogen bond. The compound **P** reacts with 3 equivalents of  $\text{NH}_2\text{OH}$  to produce oxime **Q**. Treatment of **P** with excess methyl iodide in the presence of  $\text{KOH}$  produces compound **R** as the major product. Reaction of **R** with excess *iso*-butylmagnesium bromide followed by treatment with  $\text{H}_3\text{O}^+$  gives compound **S** as the major product.

The total number of methyl ( $-\text{CH}_3$ ) group(s) in compound **S** is \_\_\_\_\_.

Answer (12)

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Karnataka Topper

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4 Year Classroom

Telangana Topper

**15**  
AIR 15  
100 PERCENTILE OVERALL  
**M. Sai Divya Teja Reddy**  
2 Year Classroom

Telangana Topper

**19**  
AIR 19  
100 PERCENTILE OVERALL  
**Rishi Shekher Shukla**  
2 Year Classroom

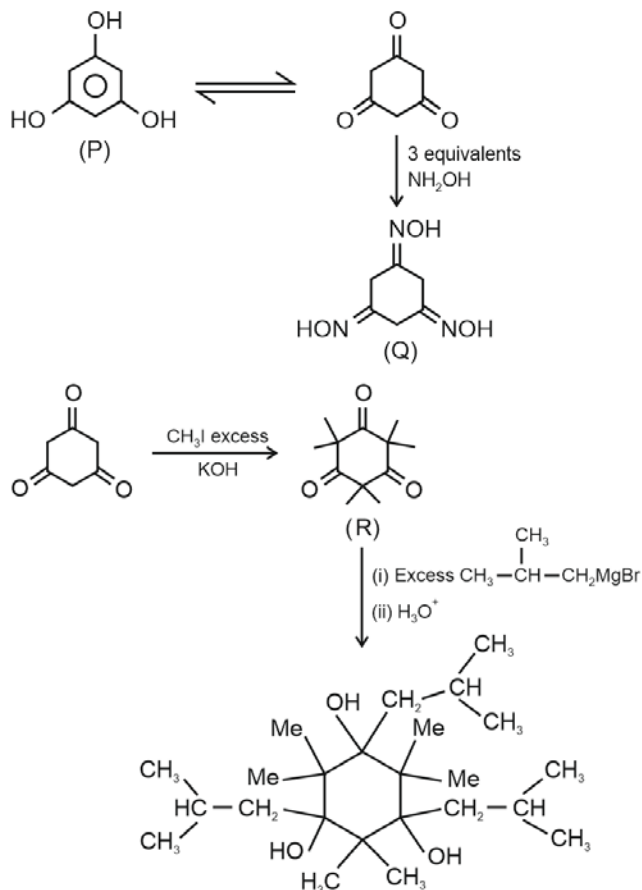
Punjab Topper

**25**  
AIR 25  
100 PERCENTILE OVERALL  
**Rachit Aggarwal**  
4 Year Classroom

**Tanishka Kabra**  
4 Year Classroom  
ALL INDIA RANK (Previous)  
**1**  
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JEE (Adv.)  
2022

**Chirag Falor**  
4 Year Classroom  
**1**  
AIR  
JEE (Adv.)  
2020

Sol.



Number of  $\text{CH}_3$  groups = 12

**SECTION 4 (Maximum Marks : 12)**

- This section contains **TWO (02)** paragraphs.
- Based on each paragraph, there are **TWO (02)** questions.
- The answer to each question is a **NUMERICAL VALUE**.
- For each question, enter the correct numerical value of the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- If the numerical value has more than two decimal places, **truncate/round-off** the value to **TWO** decimal places.
- Answer to each question will be evaluated according to the following marking scheme:

Full Marks : +3 If **ONLY** the correct numerical value is entered in the designated place;  
Zero Marks : 0 In all other cases.

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Telangana Topper



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4 Year Classroom



**Tanishka Kabra**  
4 Year Classroom  
**1**  
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2022



**Chirag Falor**  
4 Year Classroom  
**1**  
AIR JEE (Adv.)  
2020

## PARAGRAPH I

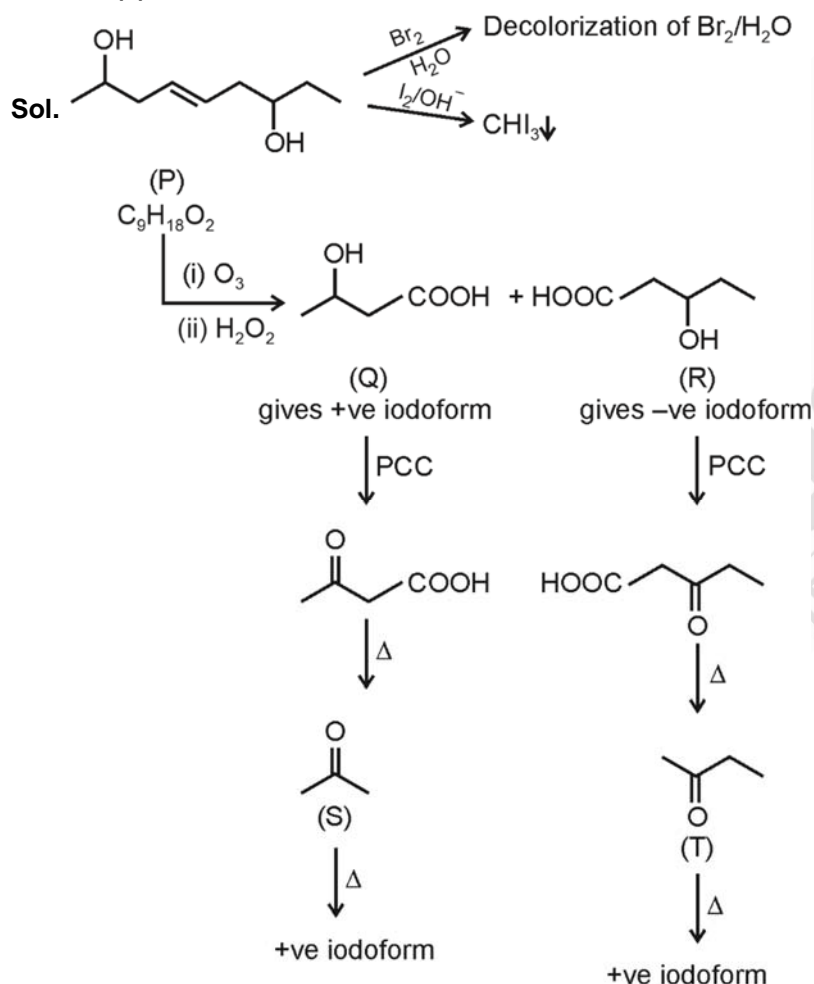
An organic compound **P** with molecular formula  $C_9H_{18}O_2$  decolorizes bromine water and also shows positive iodoform test. **P** on ozonolysis followed by treatment with  $H_2O_2$  gives **Q** and **R**. While compound **Q** shows positive iodoform test, compound **R** does not give positive iodoform test. **Q** and **R** on oxidation with pyridinium chlorochromate (PCC) followed by heating give **S** and **T**, respectively. Both **S** and **T** show positive iodoform test.

Complete copolymerization of 500 moles of **Q** and 500 moles of **R** gives one mole of a single acyclic copolymer **U**.

[Given, atomic mass: H = 1, C = 12, O = 16]

14. Sum of number of oxygen atoms in **S** and **T** is \_\_\_\_\_.

Answer (2)



Sum of number of O-atoms in **S** and **T** = 1 + 1 = 2

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AIR 25  
  
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Rachit Aggarwal  
4 Year Classroom



**Tanishka Kabra**  
4 Year Classroom  
ALL INDIA RANK (overall)  
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JEE (Adv.)  
2022



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JEE (Adv.)  
2020

PARAGRAPH I

An organic compound **P** with molecular formula  $C_9H_{18}O_2$  decolorizes bromine water and also shows positive iodoform test. **P** on ozonolysis followed by treatment with  $H_2O_2$  gives **Q** and **R**. While compound **Q** shows positive iodoform test, compound **R** does not give positive iodoform test. **Q** and **R** on oxidation with pyridinium chlorochromate (PCC) followed by heating give **S** and **T**, respectively. Both **S** and **T** show positive iodoform test.

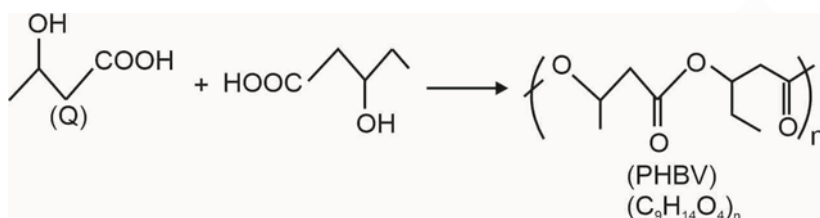
Complete copolymerization of 500 moles of **Q** and 500 moles of **R** gives one mole of a single acyclic copolymer **U**.

[Given, atomic mass: H = 1, C = 12, O = 16]

15. The molecular weight of **U** is \_\_\_\_\_.

**Answer (102018)**

**Sol.**



$$\begin{aligned} \text{Mol. wt. of polymer} &= (104 \times 500) + (118 \times 500) - 18 \times 499 \\ &= 52000 + 59000 - 8982 \\ &= 102018 \text{ g} \end{aligned}$$

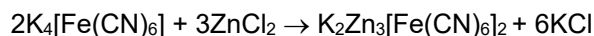
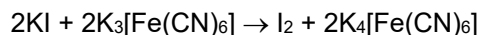
PARAGRAPH II

When potassium iodide is added to an aqueous solution of potassium ferricyanide, a reversible reaction is observed in which a complex **P** is formed. In a strong acidic medium, the equilibrium shifts completely towards **P**. Addition of zinc chloride to **P** in a slightly acidic medium results in a sparingly soluble complex **Q**.

16. The number of moles of potassium iodide required to produce two moles of **P** is \_\_\_\_\_.

**Answer (2)**

**Sol.** From this equation we need 2 mol of KI



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 <p><b>Tanishka Kabra</b> 4 Year Classroom <b>1</b> ALL INDIA RANK (Previous) AIR-16 CRL JEE (Adv.) 2022</p>	 <p><b>Chirag Falor</b> 4 Year Classroom <b>1</b> AIR JEE (Adv.) 2020</p>		



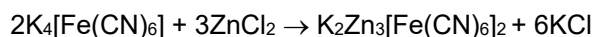
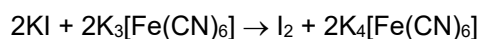
## PARAGRAPH II

When potassium iodide is added to an aqueous solution of potassium ferricyanide, a reversible reaction is observed in which a complex **P** is formed. In a strong acidic medium, the equilibrium shifts completely towards **P**. Addition of zinc chloride to **P** in a slightly acidic medium results in a sparingly soluble complex **Q**.

17. The number of zinc ions present in the molecular formula of **Q** is \_\_\_\_\_.

**Answer (3)**

**Sol.** From this equation we need 2 mol of KI



□ □ □

  
**Aakash**  
 Medical IIT-JEE Foundations

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## JEE (MAIN) 2024

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