

# CBSE Class 10 Mathematics Standard Answer Key 2022

## (May 5, Set 2 - 30/1/2)

Strictly Confidential : (For Internal and Restricted use only)

Secondary School Examination

Term-II, 2022

Marking Scheme : MATHEMATICS (Standard) (Subject Code : 041)

[ Paper Code : 30/1/2 ]

### General Instructions :

1. You are aware that evaluation is the most important process in the actual and correct assessment of the candidates. A small mistake in evaluation may lead to serious problems which may affect the future of the candidates, education system and teaching profession. To avoid mistakes, it is requested that before starting evaluation, you must read and understand the spot evaluation guidelines carefully.
2. **“Evaluation policy is a confidential policy as it is related to the confidentiality of the examinations conducted, evaluation done and several other aspects. Its leakage to public in any manner could lead to derailment of the examination system and affect the life and future of millions of candidates. Sharing this policy/document to anyone, publishing in any magazine and printing in Newspaper/ Website, etc., may invite action under IPC.”**
3. Evaluation is to be done as per instruction provided in the Marking Scheme. It should not be done according to one’s own interpretation or any other consideration. Marking Scheme should be strictly adhered to and religiously followed. **However, while evaluating, answers which are based on latest information or knowledge and/or are innovative, they may be assessed for their correctness otherwise and marks be awarded to them. In Class-X, while evaluating two competency based questions, please try to understand given answer and even if reply is not from marking scheme but correct competency is enumerated by the candidate, marks should be awarded.**
4. The Head-Examiner must go through the first five answer books evaluated by each evaluator on the first day, to ensure that evaluation has been carried out as per the instructions given in the Marking Scheme. The remaining answer books meant for evaluation shall be given only after ensuring that there is no significant variation in the marking of individual evaluators.
5. Evaluators will mark (3) wherever answer is correct. For wrong answer ‘7’ be marked. Evaluators will not put right kind of mark while evaluating which gives an impression that answer is correct and no marks are awarded. **This is most common mistake which evaluators are committing.**
6. If a question has parts, please award marks on the right-hand side for each part. Marks awarded for different parts of the question should then be totalled up and written in the left-hand margin and encircled. This may be followed strictly.
7. If a question does not have any parts, marks must be awarded in the left-hand margin and encircled. This may also be followed strictly.

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8. If a student has attempted an extra question, answer of the question deserving more marks should be retained and the other answer scored out.
9. No marks to be deducted for the cumulative effect of an error. It should be penalized only once.
10. A full scale of marks \_\_\_\_\_ (example 0–100 marks as given in Question Paper) has to be used. Please do not hesitate to award full marks if the answer deserves it.
11. Every examiner has to necessarily do evaluation work for full working hours, i.e., 8 hours everyday and evaluate 20 answer books per day in main subjects and 25 answer books per day in other subjects (Details are given in Spot Guidelines).
12. Ensure that you do not make the following common types of errors committed by the Examiner in the past :
  - Leaving answer or part thereof unassessed in an answer book
  - Giving more marks for an answer than assigned to it
  - Wrong totalling of marks awarded on a reply
  - Wrong transfer of marks from the inside pages of the answer book to the title page
  - Wrong questionwise totalling on the title page
  - Wrong totalling of marks of the two columns on the title page
  - Wrong grand total
  - Marks in words and figures not tallying
  - Wrong transfer of marks from the answer book to online award list
  - Answers marked as correct, but marks not awarded. (Ensure that the right tick mark is correctly and clearly indicated. It should merely be a line. Same is with the 7 for incorrect answer).
  - Half or a part of answer marked correct and the rest as wrong, but no marks awarded.
13. While evaluating the answer books if the answer is found to be totally incorrect, it should be marked as (7) and awarded zero (0) Mark.
14. Any unassessed portion, non-carrying over of marks to the title page, or totalling error detected by the candidates shall damage the prestige of all the personnel engaged in the evaluation work as also of the Board. Hence, in order to uphold the prestige of all concerned, it is again reiterated that the instructions be followed meticulously and judiciously.
15. The examiners should acquaint themselves with the guidelines given in the guidelines for spot evaluation before starting the actual evaluation.
16. Every examiner shall also ensure that all the answers are evaluated, marks carried over to the title page, correctly totalled and written in figures and words.
17. The Board permits candidates to obtain photocopy of the Answer Book on request in an RTI application and also separately as a part of the re-evaluation process on payment of the processing charges.



## MARKING SCHEME

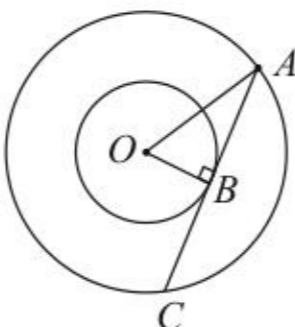
Secondary School Examination TERM-II, 2022

### MATHEMATICS (Standard) (Subject Code-041)

[ Paper Code : 30/1/2 ]

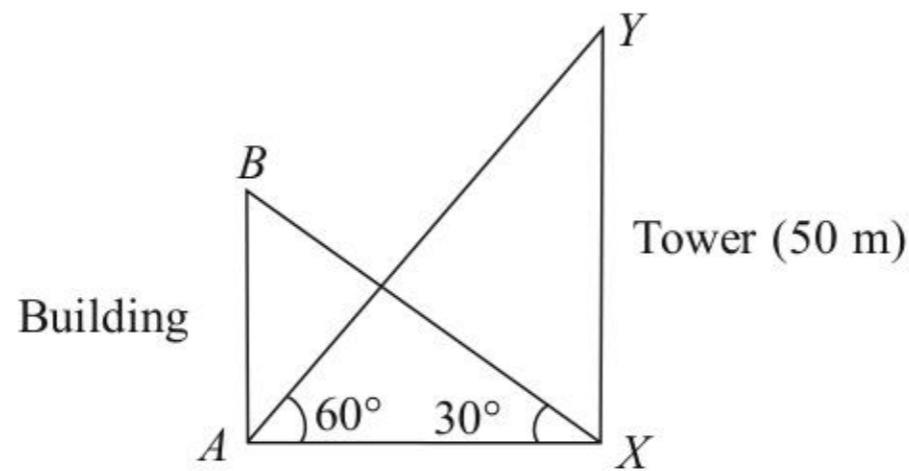
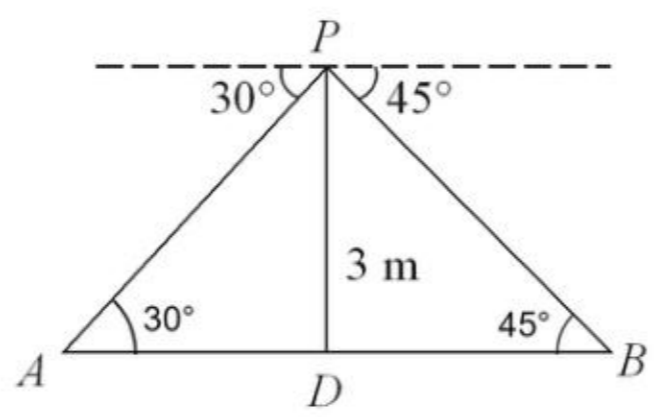
**General Instructions:**

1. The Marking Scheme provides general guidelines to reduce subjectivity in the marking. The answers given in the Marking Scheme are suggested answers. The content is thus indicative. If a student has given any other answer which is different from the one given in the Marking Scheme, but conveys the meaning, such answers should be given full weightage.
2. Evaluation is to be done as per instructions provided in the marking scheme. It should not be done according to one's own interpretation or any other consideration — Marking Scheme should be strictly adhered to and religiously followed.
3. Alternative methods are accepted. Proportional marks are to be awarded.
4. If a candidate has attempted an extra question, marks obtained in the question attempted first should be retained and the other answer should be scored out.
5. A full scale of marks - 0 to 40 has to be used. Please do not hesitate to award full marks if the answer deserves it.
6. Separate Marking Scheme for all the three sets has been given.
7. As per orders of the Hon'ble Supreme Court. The candidates would now be permitted to obtain photocopy of the Answer book on request on payment of the prescribed fee. All examiners/Head Examiners are once again reminded that they must ensure that evaluation is carried out strictly as per value points for each answer as given in the Marking Scheme.

Q. No.	EXPECTED ANSWER / VALUE POINTS	Marks												
SECTION—A														
1.	<p>Find the mode of the following frequency distribution :</p> <table border="1" style="margin-left: auto; margin-right: auto; border-collapse: collapse;"> <thead> <tr> <th style="padding: 2px;">Class</th> <th style="padding: 2px;">10 – 20</th> <th style="padding: 2px;">20 – 30</th> <th style="padding: 2px;">30 – 40</th> <th style="padding: 2px;">40 – 50</th> <th style="padding: 2px;">50 – 60</th> </tr> </thead> <tbody> <tr> <td style="padding: 2px;"><i>Frequency</i></td> <td style="padding: 2px; text-align: center;">15</td> <td style="padding: 2px; text-align: center;">10</td> <td style="padding: 2px; text-align: center;">12</td> <td style="padding: 2px; text-align: center;">17</td> <td style="padding: 2px; text-align: center;">4</td> </tr> </tbody> </table>	Class	10 – 20	20 – 30	30 – 40	40 – 50	50 – 60	<i>Frequency</i>	15	10	12	17	4	
Class	10 – 20	20 – 30	30 – 40	40 – 50	50 – 60									
<i>Frequency</i>	15	10	12	17	4									
Sol.	<p>Modal class is 40–50</p> $\text{Mode} = 40 + 10 \times \frac{17 - 12}{34 - 12 - 4}$ $= 42.7 \text{ or } 42\frac{7}{9}$	<p>½</p> <p>1</p> <p>½</p>												
2.	<p>Two concentric circles are of radii 4 cm and 3 cm. Find the length of the chord of the larger circle which touches the smaller circle.</p>													
Sol.	<div style="display: flex; align-items: center;"> <div style="flex: 1;">  </div> <div style="flex: 2;"> <p style="text-align: center;">For correct figure</p> <p>Here <math>OB = 3 \text{ cm}</math>, <math>OA = 4 \text{ cm}</math></p> <p style="text-align: center;"><math>OB \perp AC</math></p> <p><math>\therefore AB = \sqrt{4^2 - 3^2} = \sqrt{7} \text{ cm}</math></p> <p>Hence <math>AC = 2\sqrt{7} \text{ cm}</math></p> </div> </div>	<p>½</p> <p>1</p> <p>½</p>												

3.a	Find the sum of first 30 terms of AP : $-30, -24, -18, \dots$ .	
Sol.	Here $a = -30, d = 6, n = 30$ $S_{30} = \frac{30}{2}[-60 + 29 \times 6]$ $= 1710$ <p style="text-align: center;"><b>Or</b></p> In an AP if $S_n = n(4n + 1)$ , then find the AP.	1  $\frac{1}{2}$  $\frac{1}{2}$
(b)	$a = S_1 = 1(4 \times 1 + 1) = 5$	$\frac{1}{2}$
Sol.	$a + (a + d) = S_2 = 2(4 \times 2 + 1) = 18$ $\therefore d = 8$ Hence, AP is $5, 13, 21, \dots$	1  $\frac{1}{2}$
4.	A cone of height 28 cm and radius of base 7 cm is made up of modelling clay. A child reshapes it in the form of a sphere. Find the radius of the sphere.	
Sol.	$\frac{1}{3} \pi \times 7 \times 7 \times 28 = \frac{4}{3} \pi r^3$ $\Rightarrow r = 7 \text{ cm}$	1  1
5.a.	Find the value of m for which the quadratic equation $(m - 1)x^2 + 2(m - 1)x + 1 = 0$ has two real and equal roots.	
Sol.	For real and equal roots $4(m - 1)^2 - 4(m - 1) = 0$ $\Rightarrow m = 1 \text{ or } m = 2$ $m \neq 1 \Rightarrow m = 2$ <p style="text-align: center;"><b>Or</b></p>	$\frac{1}{2}$  1
b.	Solve the following quadratic equation for x : $\sqrt{3}x^2 + 10x + 7\sqrt{3} = 0$	
Sol.	$\sqrt{3}x^2 + 10x + 7\sqrt{3} = 0$ $\text{or } \sqrt{3}x^2 + 3x + 7x + 7\sqrt{3} = 0$ $\text{or } (\sqrt{3}x + 7)(x + \sqrt{3}) = 0$ $\Rightarrow x = -\frac{7}{\sqrt{3}}, -\sqrt{3} \text{ or } -\frac{7}{3}\sqrt{3}, -\sqrt{3}$	1  1



6.	<p>The product of Rehan's age (in years) 5 years ago and his age 7 years from now, is one more than twice his present age. Find his present age.</p>	
Sol.	<p>Let Rehan's present age be <math>x</math> years</p> $\therefore (x-5)(x+7) = 2x+1$ $\Rightarrow x^2 = 36$ $\Rightarrow x = 6$	<p>1 ½ ½</p>
<b>SECTION—B</b>		
7.a.	<p>The angle of elevation of the top of a building from the foot of the tower is <math>30^\circ</math> and the angle of elevation of the top of the tower from the foot of the building is <math>60^\circ</math>. If the tower is 50 m high, then find the height of the building.</p>	
Sol.	<p style="text-align: right;">For correct figure</p>  <p style="text-align: right;"><math>\tan 30^\circ = \frac{AB}{AX}</math> and <math>\tan 60^\circ = \frac{50}{AX}</math></p> $\Rightarrow AB = \frac{1}{\sqrt{3}} AX \text{ and } AX = \frac{50}{\sqrt{3}}$ $\therefore AB = \frac{1}{\sqrt{3}} \cdot \frac{50}{\sqrt{3}} = \frac{50}{3} \text{ m}$	<p>1 ½+½ 1</p>
<b>OR</b>		
b.	<p>From a point on a bridge across a river, the angles of depression of the banks on opposite sides of the river are <math>30^\circ</math> and <math>45^\circ</math> respectively. If the bridge is at a height of 3 m from the banks, then find the width of the river.</p>	
Sol.	<p style="text-align: right;">For correct figure</p>  <p>Here, <math>\frac{PD}{AD} = \tan 30^\circ = \frac{1}{\sqrt{3}} \Rightarrow AD = 3\sqrt{3} \text{ m}</math></p> <p>and <math>\frac{PD}{BD} = \tan 45^\circ = 1 \Rightarrow BD = 3 \text{ m}</math></p> <p>So, <math>AB = AD + BD = (3\sqrt{3} + 3) \text{ m} = 3(\sqrt{3} + 1) \text{ m}</math></p>	<p>1 ½ ½ 1</p>

8. Following is the daily expenditure on lunch by 30 employees of a company :

Daily Expenditure (in Rupees)	Number of Employees
100 – 120	8
120 – 140	3
140 – 160	8
160 – 180	6
180 – 200	5

Find the mean daily expenditure of the employees.

Sol.

Class	$x$	$f$	$d$	$f.d$
100–120	110	8	–40	–320
120–140	130	3	–20	–60
140–160	150	8	0	0
160–180	170	6	20	120
180–200	190	5	40	200
		30		–60

For correct table

$$\text{Mean} = 150 + \frac{-60}{30} = 148$$

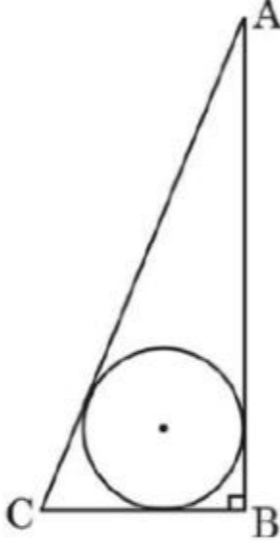
Therefore, mean expenditure = Rs. 148

2

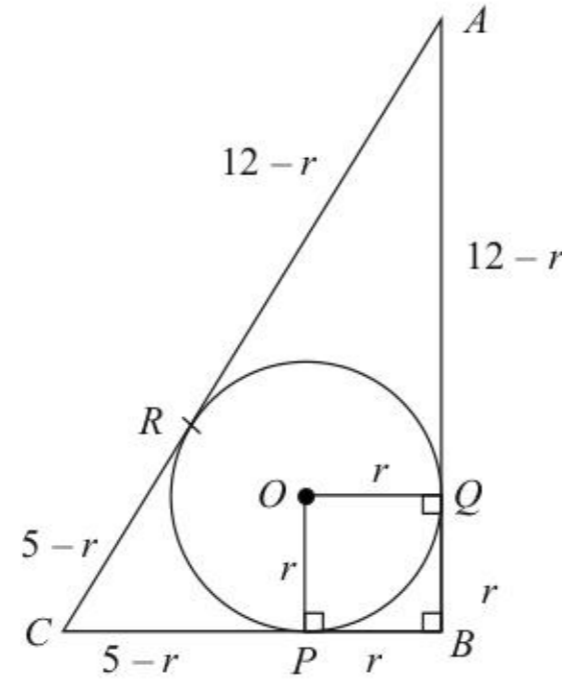
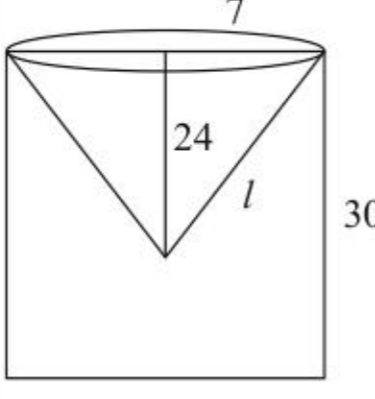
1

9. If the median of the following data is 33 then, find the value of m :

Class	0 – 15	15 – 30	30 – 45	45 – 60	60 – 75	75 – 90
Frequency	17	35	40	18	m	2

<b>Sol.</b>	<i>Class</i>	<i>f</i>	<i>c.f.</i>	
	0–15	17	17	
	15–30	35	52	
	30–45	40	92	
	45–60	18	110	
	60–75	<i>m</i>	110 + <i>m</i>	
	75–90	2	112 + <i>m</i>	
			For correct table	1
	Median class is 30–45			½
	$33 = 30 + \frac{15}{40} \left( \frac{112 + m}{2} - 52 \right)$			1
	$\Rightarrow m = 8$			½
<b>10.</b>	Construct a pair of tangents to a circle of radius 5 cm, which are inclined to each other at an angle of 60°.			
<b>Sol.</b>	Correct construction			3
<b>SECTION—C</b>				
<b>11.</b>	In Figure 1, a right triangle ABC in which $\angle B = 90^\circ$ , AB = 12 cm and BC = 5 cm is shown. Find the radius of the circle inscribed in the triangle ABC.			
				
	<i>Figure 1</i>			



<p><b>Sol.</b></p>		<p><math>OPBQ</math> is a square of side <math>r</math></p> <p><math>\therefore AQ = AR = 12 - r</math></p> <p><math>CP = CR = 5 - r</math></p> <p><math>\Rightarrow AC = (12 - r) + (5 - r) = 17 - 2r</math></p> <p>Also <math>AC = \sqrt{5^2 + 12^2} = 13</math></p> <p><math>\Rightarrow 17 - 2r = 13</math></p> <p><math>\Rightarrow r = 2</math></p> <p><math>\therefore</math> Radius of circle is 2 cm</p>	<p>1</p> <p>1</p> <p>1</p> <p>1</p>
<p><b>12.</b> <b>a.</b></p>	<p>From a solid cylinder of height 30 cm and radius 7 cm, a conical cavity of height 24 cm and same radius is hollowed out. Find the total surface area of the remaining solid.</p>	<p><math>l = \sqrt{576 + 49} = 25 \text{ cm}</math></p>  <p>TSA = <math>2\pi rh + \pi r^2 + \pi rl</math></p> <p><math>= \frac{22}{7} \times 7 [60 + 7 + 25]</math></p> <p><math>= 2024 \text{ cm}^2</math></p>	<p>1</p> <p>2</p> <p>1</p>
<p><b>b.</b></p>	<p><b>Or</b></p> <p>Water in a canal, 8 m wide and 6 m deep, is flowing with a speed of 12 km/hour. How much area will it irrigate in one hour, if 0.05 m of standing water is required ?</p>	<p><b>Sol.</b> Distance covered by water in 1 hr = 12000 m</p> <p><math>\therefore</math> Volume of water flown in 1 hr</p> <p><math>= 8 \times 6 \times 12000 \text{ m}^3</math></p> <p>Hence area of field <math>\times 0.05 = 8 \times 6 \times 12000</math></p> <p><math>\Rightarrow</math> Area of field = <math>1152 \times 10^4 \text{ m}^2</math> or <math>11520000 \text{ m}^2</math></p>	<p><math>\frac{1}{2}</math></p> <p><math>1\frac{1}{2}</math></p> <p><math>1\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p>



13.

In Mathematics, relations can be expressed in various ways. The matchstick patterns are based on linear relations. Different strategies can be used to calculate the number of matchsticks used in different figures.

One such pattern is shown below. Observe the pattern and answer the following questions using Arithmetic Progression :



Figure 1



Figure 2

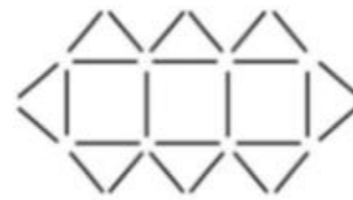


Figure 3



- (a) Write the AP for the number of triangles used in the figures. Also, write the  $n^{\text{th}}$  term of this AP.
- (b) Which figure has 61 matchsticks ?

**Sol.**

- (a) Number of triangles in figures are 4, 6, 8, ...

This is an A.P. with  $a = 4$ ,  $d = 2$

$$\therefore a_n = 4 + (n - 1) \times 2 = 2n + 2$$

$\frac{1}{2}$

1

$\frac{1}{2}$

- (b) Number of matchsticks in figures are 12, 19, 26, ...

This is an A.P. with  $a = 12$ ,  $d = 7$

$$\therefore 61 = 12 + (n - 1) \times 7$$

$$\Rightarrow n = 8$$

$\frac{1}{2}$

1

$\frac{1}{2}$

**14. Case Study—2**

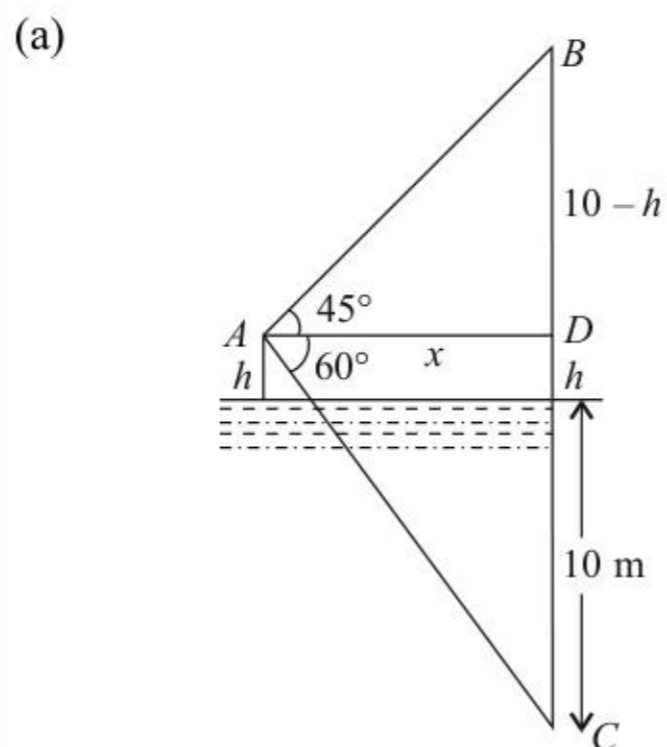
Gadisar Lake is located in the Jaisalmer district of Rajasthan. It was built by the King of Jaisalmer and rebuilt by Gadsis Singh in 14<sup>th</sup> century. The lake has many Chhatris. One of them is shown below :



Observe the picture. From a point A  $h$  m above from water level, the angle of elevation of top of Chhatri (point B) is  $45^\circ$  and angle of depression of its reflection in water (point C) is  $60^\circ$ . If the height of Chhatri above water level is (approximately) 10 m, then

- draw a well-labelled figure based on the above information;
- find the height ( $h$ ) of the point A above water level.  
(Use  $\sqrt{3} = 1.73$ )

**Sol.**



Correct Figure

2

(b)  $\tan 45^\circ = 1 = \frac{10-h}{x}$   
 $\Rightarrow x = 10 - h$  ... (i)

$\tan 60^\circ = \sqrt{3} = \frac{10+h}{x}$

$\frac{1}{2}$



	$\Rightarrow x = \frac{10+h}{\sqrt{3}} \quad \dots \text{ (ii)}$	
	Solving (i) and (ii) $10(\sqrt{3}-1) = h(\sqrt{3}+1)$	$\frac{1}{2}$
	$\Rightarrow h = \frac{10(\sqrt{3}-1)^2}{2}$	
	$= 2.67 \text{ m or } 2.7\text{m}$	1

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