CBSE Class 12 Mathematics Answer Key 2024 (Set 2 - 65/3/2) Marking Scheme

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Senior School Certificate Examination, 2024

NAATHENAATICS DADED CODE 65/2/2

	MATHEMATICS PAPER CODE 65/3/2	
Gene	ral Instructions:	
1	You are aware that evaluation is the most important process in the actual and correct assessment of the candidates. A small mistake in evaluation may lead to serious problems which may affect the future of the candidates, education system and teaching profession. To avoid mistakes, it is requested that before starting evaluation, you must read and understand the spot evaluation guidelines carefully.	
2	"Evaluation policy is a confidential policy as it is related to the confidentiality of the examinations conducted, Evaluation done and several other aspects. Its' leakage to public in any manner could lead to derailment of the examination system and affect the life and future of millions of candidates. Sharing this policy/document to anyone, publishing in any magazine and printing in News Paper/Website etc may invite action under various rules of the Board and IPC."	
3	Evaluation is to be done as per instructions provided in the Marking Scheme. It should not be done according to one's own interpretation or any other consideration. Marking Scheme should be strictly adhered to and religiously followed. However, while evaluating, answers which are based on latest information or knowledge and/or are innovative, they may be assessed for their correctness otherwise and due marks be awarded to them.	
4	The Marking scheme carries only suggested value points for the answers. These are Guidelines only and do not constitute the complete answer. The students can have their own expression and if the expression is correct, the due marks should be awarded accordingly.	
5	The Head-Examiner must go through the first five answer books evaluated by each evaluator on the first day, to ensure that evaluation has been carried out as per the instructions given in the Marking Scheme. If there is any variation, the same should be zero after delibration and discussion. The remaining answer books meant for evaluation shall be given only after ensuring that there is no significant variation in the marking of individual evaluators.	
6	Evaluators will mark ($\sqrt{\ }$) wherever answer is correct. For wrong answer CROSS 'X" be marked. Evaluators will not put right ($\sqrt{\ }$) while evaluating which gives an impression that answer is correct and no marks are awarded. This is most common mistake which evaluators are committing.	
7	If a question has parts, please award marks on the right-hand side for each part. Marks awarded for different parts of the question should then be totaled up and written in the left-hand margin and encircled. This may be followed strictly.	
8	If a question does not have any parts, marks must be awarded in the left-hand margin and encircled. This may also be followed strictly.	
9	In Q1-Q20, if a candidate attempts the question more than once (without canceling the previous attempt), marks shall be awarded for the first attempt only and the other answer scored out with a note "Extra Question".	





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Q. NO. EXPECTED ANSWER / VALUE POINT **MARKS SECTION A** Questions no. 1 to 18 are multiple choice questions (MCQs) of 1 mark each. Q1 If $k = \pm 6$, then the value of k is: (A) Ans (\mathbf{D}) ∓ 2 Q2 The derivative of 5^x w.r.t. e^x is: (C) $\left(\frac{5}{e}\right)^{x} \log 5$ (D) $\left(\frac{e}{5}\right)^x \log 5$ Ans (C) $\left(\frac{5}{e}\right)^{x} \log 5$ Q3 If $|\overrightarrow{a}| = 2$ and $-3 \le k \le 2$, then $|\overrightarrow{ka}| \in :$ (A) [-6, 4](C) [4, 6] [0, 4][0, 6]Ans [0, 6]Q4 If a line makes an angle of $\frac{\pi}{4}$ with the positive directions of both x-axis and z-axis, then the angle which it makes with the positive direction of y-axis is: Ans





Q5 Of the following, which group of constraints represents the feasible region given below? (A) $x + 2y \le 76$, $2x + y \ge 104$, $x, y \ge 0$ (B) $x + 2y \le 76$, $2x + y \le 104$, $x, y \ge 0$ (C) $x + 2y \ge 76$, $2x + y \le 104$, $x, y \ge 0$ (D) $x + 2y \ge 76$, $2x + y \ge 104$, $x, y \ge 0$ Ans (C) $x + 2y \ge 76$, $2x + y \le 104$, $x, y \ge 0$ Q6 If $A = \begin{bmatrix} 2 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 5 \end{bmatrix}$, then A^{-1} is : (A) (B) Ans (A)





07		
Q7	For any square matrix A , $(A - A')$ is always	
	(A) an identity matrix	
	(B) a null matrix	
	(C) a skew symmetric matrix	
	(D) a symmetric matrix	
Ans	(C) a skew symmetric matrix	1
Q8	A function $f: R \to A$ defined as $f(x) = x^2 + 1$ is onto, if A is	•
	$(A) (-\infty, \infty) \tag{B}$	
	(C) $[1, \infty)$ (D) $[-1, \infty)$	
Ans	(C) [1, ∞)	1
Q9	Let $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$ be a square matrix such that adj $A =$	A. Then,
	(a + b + c + d) is equal to:	
	(A) 2a (B) 2b	
	(C) 2c (D) 0	
Ans	(A) 2a	1
Q10	A function $f(x) = 1 - x + x $ is:	
	(A) discontinuous at $x = 1$ only (B) discontinuous a	at x = 0 only
	(C) discontinuous at $x = 0, 1$ (D) continuous even	
Ans	(D) continuous everywhere	1
Q11	The point of inflexion of a function f(x) is the point where	
	(A) $f'(x) = 0$ and $f'(x)$ changes its sign from positive to no left to right of that point.	egative from
	(B) $f'(x) = 0$ and $f'(x)$ changes its sign from negative to p left to right of that point.	ositive from
	(C) $f'(x) = 0$ and $f'(x)$ does not change its sign from left to point.	right of that
	(D) $f'(x) \neq 0$.	
Ans	(C) $f'(x) = 0$ and $f'(x)$ does not change its sign from left to right of that point.	1





012		
Q12	If $g(x)$ is a continuous function satisfying $g(-x) = -g(x)$, then	$\int_{0}^{2a} g(x) dx$
	is equal to:	U
	(A) 0 (B) $2 \int_{0}^{a} g(x) dx$	
	(C) $\int_{-a}^{a} g(x) dx$ (D) $-\int_{-2a}^{0} g(x) dx$	
Ans	D) $-\int_{-2a}^{0} g(x) dx$	1
Q13	$x \log x \frac{dy}{dx} + y = 2 \log x$ is an example of a:	
	(A) variable separable differential equation.	
	(B) homogeneous differential equation.	
	(C) first order linear differential equation.	
	(D) differential equation whose degree is not defined.	
Ans	(C) first order linear differential equation.	1
Q14	If $\overrightarrow{a} = 2\overrightarrow{i} - \overrightarrow{j} + \overrightarrow{k}$ and $\overrightarrow{b} = \overrightarrow{i} + \overrightarrow{j} - \overrightarrow{k}$, then \overrightarrow{a} and \overrightarrow{b} are	•
	(A) collinear vectors which are not parallel	
	(B) parallel vectors	
	(C) perpendicular vectors	
	(D) unit vectors	
Ans	(C) perpendicular vectors	1
Q15	If α , β and γ are the angles which a line makes with positive of	lirections of
	${\bf x},{\bf y}$ and ${\bf z}$ axes respectively, then which of the following is ${\it not}$	true?
	(A) $\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 1$	
	(B) $\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma = 2$	
	(C) $\cos 2\alpha + \cos 2\beta + \cos 2\gamma = -1$	
	(D) $\cos \alpha + \cos \beta + \cos \gamma = 1$	
Ans	(D) $\cos \alpha + \cos \beta + \cos \gamma = 1$	1

^{*}These answers are meant to be used by evaluators.



Q16	The restrictions imposed on decision variables involved in an objective function of a linear programming problem are called: (A) feasible solutions (B) constraints		
	(C) optimal solutions (D) infeasible solution	S	
Ans	(B) constraints	1	
Q17	Let E and F be two events such that $P(E) = 0.1$, $P(F) = 0.3$, $P(E) = 0.1$, $P(F \mid E)$ is : (A) 0.6 (B) 0.4 (C) 0.5 (D)	∪ F) = 0·4, 0	
Ans	(D) 0	1	
Q18	If $A = [a_{ij}]$ is an identity matrix, then which of the followin	g is true ?	
	(A) $a_{ij} = \begin{cases} 0, & \text{if } i = j \\ 1, & \text{if } i \neq j \end{cases}$ (B) $a_{ij} = 1, \forall i, j$		
	(C) $a_{ij} = 0, \forall i, j$ (D) $a_{ij} = \begin{cases} 0, & \text{if } i = 0, \\ 1, & \text{if } i = 0, \end{cases}$	≠ j = j	
Ans	(D) $a_{ij} = \begin{cases} 0, & \text{if } i \neq j \\ 1, & \text{if } i = j \end{cases}$	1	
stateme (R). Sel	ons number 19 and 20 are Assertion and Reason based questions are given, one labelled Assertion (A) and the other labellect the correct answer from the codes (A), (B), (C) and (D) as given. A) Both Assertion (A) and Reason (R) are true and Reason.	lled Reason ven below.	
	correct explanation of the Assertion (A).	11 (10) 15 0110	
((B) Both Assertion (A) and Reason (R) are true, but Reason (R) is not the correct explanation of the Assertion (A).		
(C) Assertion (A) is true, but Reason (R) is false.		
(D) Assertion (A) is false, but Reason (R) is true.		
Q19	Assertion (A): Projection of \overrightarrow{a} on \overrightarrow{b} is same as projection of Reason (R): Angle between \overrightarrow{a} and \overrightarrow{b} is same as ang \overrightarrow{b} and \overrightarrow{a} numerically.		
Ans	(D) Assertion (A) is false, but Reason (R) is true.	1	





Q20	Assertion (A) : Every scalar matrix is a diagonal matrix.		
	Reason (R): In a diagonal matrix, all the diagonal elements are 0.		
Ans	(C) Assertion (A) is true, but Reason (R) is false.	1	
Que	SECTION B Questions no. 21 to 25 are very short answer (VSA) type questions, carrying 2 marks each.		
Q21(a)	Evaluate:		
	$\pi/2$		
	sin 2x cos 3x dx		
	0		
Ans	$I = \int_{0}^{\frac{\pi}{2}} \sin 2x \cos 3x dx$		
	$=\frac{1}{2}\int_{0}^{\frac{\pi}{2}}\left(\sin 5x - \sin x\right)dx$	1.	
	$=\frac{1}{2}\left[-\frac{1}{5}\cos 5x + \cos x\right]_0^{\frac{\pi}{2}}$	1/2	
	$=-\frac{2}{5}$	1/2	
Q21(b)	Given $\frac{d}{dx} F(x) = \frac{1}{\sqrt{2x-x^2}}$ and $F(1) = 0$, find $F(x)$.		
Ans	$F(x) = \int \frac{1}{\sqrt{2x - x^2}} dx$		
	$=\int \frac{1}{\sqrt{1-(x-1)^2}} dx$	1/2	
	$=\sin^{-1}(x-1)+c$	1/2	
	when $x = 1$, $y = 0$ gives $c = 0$	1/2	
	$\therefore F(x) = \sin^{-1}(x-1)$	1/2	
Q22	Find the position vector of point C which divides the line segment points A and B having position vectors $\hat{i} + 2\hat{j} - \hat{k}$ and $-\hat{i}$ respectively in the ratio 4: 1 externally. Further, find $ AB $: $ B $	+ j + k	



Ans	Position vector of $C = \vec{r} = \frac{4\vec{b} - \vec{a}}{3}$	
	i.e. $\vec{r} = \frac{1}{3} \left(-5\hat{i} + 2\hat{j} + 5\hat{k} \right)$	1
	Now, $\overrightarrow{AB} = -2\hat{i} - \hat{j} + 2\hat{k} \Rightarrow \left \overrightarrow{AB} \right = 3$	
	$\begin{vmatrix} \vec{BC} = -\frac{1}{3} \left(2\hat{i} + \hat{j} - 2\hat{k} \right) \Rightarrow \begin{vmatrix} \vec{DC} \\ \vec{BC} \end{vmatrix} = 1$	1
	$\left \overrightarrow{AB} \right : \left \overrightarrow{BC} \right = 3:1$	
Q23	If \overrightarrow{a} , \overrightarrow{b} and \overrightarrow{c} are three unit vectors such that \overrightarrow{a} + \overrightarrow{b} - \overrightarrow{c}	$\Rightarrow = \overrightarrow{0}$, find
	the angle between vectors \overrightarrow{a} and \overrightarrow{c} .	
Ans	$\operatorname{Given} \vec{a} = \vec{b} = \vec{c} = 1$	
	Now $\vec{a} - \vec{c} = -\vec{b}$	
	$(\vec{a} - \vec{c}) \cdot (\vec{a} - \vec{c}) = (-\vec{b}) \cdot (-\vec{b})$	1/2
	$\Rightarrow \left \vec{a} \right ^2 + \left \vec{c} \right ^2 - 2\vec{a}.\vec{c} = \left \vec{b} \right ^2$	1/2
	$\Rightarrow 1+1-2 \vec{a} \vec{c} \cos\theta=1$	
	$\Rightarrow 2-2(1)(1)\cos\theta=1$	1/2
	$\Rightarrow \cos \theta = \frac{1}{2} \Rightarrow \theta = \frac{\pi}{3}$	1/2
Q24	Find the value of $\left[\sin^2\left\{\cos^{-1}\left(\frac{3}{5}\right)\right\} + \tan^2\left\{\sec^{-1}\left(3\right)\right\}\right]$.	
Ans	Required value = $ \left[1 - \cos^2 \left(\cos^{-1} \frac{3}{5} \right) \right] + \left[\sec^2 \left(\sec^{-1} 3 \right) - 1 \right] $	1
	$=\left(1-\frac{9}{25}\right)+(9-1)$	1/2
	$=\frac{216}{25}$	1/2
Q25(a)	If $x = e^{x/y}$, prove that $\frac{dy}{dx} = \frac{\log x - 1}{(\log x)^2}$	
Ans	$x = e^{\frac{x}{y}} \Rightarrow \log x = \frac{x}{y} \Rightarrow y = \frac{x}{\log x}$	1
	$\Rightarrow \frac{dy}{dx} = \frac{(\log x)(1) - x\left(\frac{1}{x}\right)}{(\log x)^2} = \frac{\log x - 1}{(\log x)^2}$	1

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Q25(b)	Check the differentiability of $f(x) = \begin{cases} x^2 + 1, & 0 \le x < 1 \\ 3 - x, & 1 \le x \le 2 \end{cases}$	at x = 1.
Ans	LHD at $x = 1$ $= \lim_{h \to 0} \frac{f(1-h) - f(1)}{-h} = \lim_{h \to 0} \frac{\left[(1-h)^2 + 1 \right] - 2}{-h} = 2$ RHD at $x = 1$	1
	$= \lim_{h \to 0} \frac{f(1+h) - f(1)}{h} = \lim_{h \to 0} \frac{\left[3 - (1+h)\right] - 2}{h} = -1$ as LHD \neq RHD, so $f(x)$ is not differentiable at $x = 1$	1/2 1/2
	SECTION C Questions no. 26 to 31 are short answer (SA) type questions, carrying 3 man	rks each.
Q26	Find: $\int \frac{x^{-1}}{(\log x)^2 - 5\log x + 4} dx$	
Ans	Let $\log x = t$; $\frac{1}{x} dx = dt$	1/2
	Given integral = $\int \frac{1}{t^2 - 5t + 4} dt$	
	$= \int \frac{1}{\left(t - \frac{5}{2}\right)^2 - \left(\frac{3}{2}\right)^2} dt$	1
	$= \frac{1}{3} \log \left \frac{t-4}{t-1} \right + C$	1
	$= \frac{1}{3} \log \left \frac{\log x - 4}{\log x - 1} \right + C$	1/2
Q27(a)	Find: $\int \frac{2+\sin 2x}{1+\cos 2x} e^x dx$	





Ans		
	$I = \int \frac{2 + \sin 2x}{1 + \cos 2x} e^x dx$	
	$= \int \frac{2 + 2\sin x \cos x}{e^x} e^x dx$	
	$2\cos^2 x$	1
	$= \int \left(\sec^2 x + \tan x\right) e^x dx$	1
	$=e^{x}.\tan x+c$	1
Q27(b)	Evaluate:	
	$\int_{0}^{\pi/4} \frac{1}{\sin x + \cos x} dx$	
Ans	$\underline{\pi}$	
	$I = \int_0^4 \frac{1}{\sin x + \cos x} dx$	
	$= \frac{1}{\sqrt{2}} \int_{0}^{\frac{\pi}{4}} \frac{1}{\cos \frac{\pi}{4} \sin x + \sin \frac{\pi}{4} \cos x} dx$	1
	$= \frac{1}{\sqrt{2}} \int_{0}^{\frac{\pi}{4}} \frac{1}{\sin\left(x + \frac{\pi}{4}\right)} dx = = \frac{1}{\sqrt{2}} \int_{0}^{\frac{\pi}{4}} \cos ec\left(x + \frac{\pi}{4}\right) dx$	
	$= \frac{1}{\sqrt{2}} \left[\log \left \cos ec \left(x + \frac{\pi}{4} \right) - \cot \left(x + \frac{\pi}{4} \right) \right \right]_0^{\frac{\pi}{4}}$	1
	$= \frac{1}{\sqrt{2}} \log \left(\sqrt{2} + 1\right) \text{ or } -\frac{1}{\sqrt{2}} \log \left(\sqrt{2} - 1\right)$	1
Q28	Solve the following linear programming problem graphica	ally:
	Minimize z = 600x + 400y,	
	subject to the constraints	
	$x + y \ge 8$	
	$x + 2y \le 16$	
	$4x + y \le 29$	
	$x, y \ge 0$.	
L.		



^{*}These answers are meant to be used by evaluators.

Ans			
Ans	C(0,8)		
		4x + y = 29	
	6 -		
		B(6,5)	
	4 -		For correct
		x + 2y = 16	graph 1½ marks
	2 -	A(7,1)	
	0 2 4	6 8 10 12 14 16	
	-2 -	x + y = 8	
	Corner Point	Value of	
		z = 600x + 400y	
	A(7,1)	4600	For correct
	B(6,5)	5600	table
	C(0,8)	3200	1 mark
	22001	. 0	1/2
	$z_{\min} = 3200 \text{ when } x = 0, y$	y = 8	/2
Q29	The chances of P, 6	and R getting selected as CEO of a com	pany are in
		respectively. The probabilities for the	
	_	from the previous year under the new CEO	
		5 respectively. If the company increased	_
	appointment of R as	year, find the probability that it is	due to the
	appointment of it as	OLO.	
Ans	Let $E_1: P$ is appointed as	CEO,	
	$E_2: Q$ is appointed as CE		1./
	$E_3: R$ is appointed as CE	O	1/2
	A: company increase pro	ofits from previous year	
	here, $P(E_1) = \frac{4}{7}$, $P(E_3) =$	$=\frac{1}{1}, P(E_1) = \frac{2}{1}$	1
	$P(A \mid E_1) = 0.3, P(A \mid E_2)$	7^{\prime} 7	s i a
	$P(A \mid E_1) = 0.5, P(A \mid E_2)$		
	$P(E_3 A) = \frac{1}{P(E_1)P(A)}$	$\frac{P(E_3)P(A E_3)}{ E_1 + P(E_2)P(A E_2) + P(E_3)P(A E_3)}$	
	$\frac{2}{7}$ ×		104
	$=\frac{\frac{7}{4\times0.3+\frac{1}{7}\times}}{\frac{1}{7}\times0.3+\frac{1}{7}\times}$	$0.8 + \frac{2}{7} \times 0.5$.
	7 7 1		
	$=\frac{1}{3}$		1/2
T.			1

^{*}These answers are meant to be used by evaluators.



Q30(a)	If $x \cos (p + y) + \cos p \sin (p + y) = 0$, prove that	
	$\cos p \frac{dy}{dx} = -\cos^2 (p + y)$, where p is a constant.	
Ans	$x\cos(p+y)+\cos p\sin(p+y)=0$	
	$\Rightarrow x = \frac{-\cos p \sin(p+y)}{\cos(p+y)} \Rightarrow x = -\cos p \cdot \tan(p+y)$	1
	$\Rightarrow \frac{dx}{dy} = -\cos p \cdot \sec^2(p+y)$	1
	$\Rightarrow \frac{dy}{dx} = \frac{-1}{\cos p \cdot \sec^2(p+y)}$	1/2
	$\Rightarrow \cos p \frac{dy}{dx} = -\cos^2(p+y)$	1/2
Q30(b)	Find the value of a and b so that function f defined as:	
	$\left(\frac{x-2}{x-2}+a\right)$, if $x<2$	
	$f(x) = \begin{cases} \frac{ x-2 }{ x-2 } + a, & \text{if } x < 2 \\ a+b, & \text{if } x = 2 \end{cases}$	
	$\mathbf{x} = \{\mathbf{a} + \mathbf{b}, \\ \mathbf{x} = 2\}$	
	$\begin{cases} \frac{x-2}{ x-2 } + b, & \text{if } x > 2 \\ $	
	is a continuous function.	
Ans	$f(x) = \begin{cases} \frac{x-2}{-(x-2)} + a & ; x < 2 \\ a+b & ; x = 2 \Rightarrow f(x) = \begin{cases} -1+a & ; x < 2 \\ a+b & ; x = 2 \end{cases} \\ x-2 & ; x > 2 \end{cases}$	
	$\begin{vmatrix} -(x-2) & & \\ -1+a & ; x < 2 \end{vmatrix}$	
	$ f(x) \le a+b ; x=2 \Rightarrow f(x) = a+b ; x=2 $	
	$\left \begin{array}{c} \frac{x-2}{(x-2)} + b & ; x > 2 \end{array} \right \left \begin{array}{c} 1+b & ; x > 2 \end{array} \right $	
	$\lim_{x \to 2^{-}} f(x) = -1 + a, \lim_{x \to 2^{+}} f(x) = 1 + b \text{ and } f(2) = a + b$	1
	as f is continous at $x = 2$: $-1 + a = 1 + b = a + b$	1
	$\Rightarrow a = 1, b = -1$	1/2+1/2
Q31(a)	Find the intervals in which the function $f(x) = \frac{\log x}{x}$ is	strictly
	increasing or strictly decreasing.	
Ans	$f(x) = \frac{\log x}{x} \Rightarrow f'(x) = \frac{1 - \log x}{x^2}; x > 0$	1
	for strictly increasing/decreasing, put $f'(x) = 0 \Rightarrow x = e$	1
	for strictly increasing, $x \in (0, e)$ and for strictly decreasing $x \in (e, \infty)$	1/2+1/2





Q31(b)	Find the absolute maximum and absolute minimum values of the	
	function f given by $f(x) = \frac{x}{2} + \frac{2}{x}$, on the interval [1, 2].	
Ans $f(x) = \frac{x}{2} + \frac{2}{x}$; $x \in [1, 2]$		
	$\Rightarrow f'(x) = \frac{1}{2} - \frac{2}{x^2}$	1
	for absolute maximum / minimum, put $f'(x) = 0$	
	$\Rightarrow x^2 = 4 \Rightarrow x = 2$	1/2
	Now, $f(1) = \frac{5}{2}$ and $f(2) = 2$	1/2+1/2
	∴ absolute maximum value = $\frac{5}{2}$ and absolute minimum value = 2	1/2
	SECTION D	
Question	s no. 32 to 35 are long answer (LA) type questions carrying 5 marks each.	
Q32(a) It is given that function $f(x) = x^4 - 62x^2 + ax$		ins local
	maximum value at $x = 1$. Find the value of 'a', hence obtain all	
	other points where the given function f(x) attains local maximum	
	or local minimum values.	
Ans	$f(x)=x^4-62x^2+ax+9 \Rightarrow f'(x)=4x^3-124x+a$	1/2
	as at $x = 1$, f attains local maximum value, $f'(1) = 0 \Rightarrow a = 120$	1
	now, $f'(x)=4x^3-124x+120=4(x-1)(x^2+x-30)=4(x-1)(x-5)(x+6)$	1
	Critical points are $x = -6, 1, 5$	1
	$f''(x)=12x^2-124$	
	f''(-6) > 0, f''(1) < 0, f''(5) > 0	1/2
	so f attains local maximum value at $x = 1$ and local minimum value at $x = -6$, 5	1
Q32(b)	The perimeter of a rectangular metallic sheet is 300 cm. It is rolled	
	along one of its sides to form a cylinder. Find the dimensions of the	
	rectangular sheet so that volume of cylinder so for maximum.	med is





Ans								
	Let length of rectangle be x cm and breadth be $(150 - x)$ cm.							
	Let r be the radius of cylinder $\Rightarrow 2\pi r = x \Rightarrow r = \frac{x}{2\pi}$	1						
	$V = \pi r^2 h = \pi \left(\frac{x^2}{4\pi^2}\right) (150 - x) = \frac{75x^2}{2\pi} - \frac{x^3}{4\pi}$	1						
	$\frac{dV}{dx} = \frac{150x}{2\pi} - \frac{3x^2}{4\pi}$	1						
	$\frac{dV}{dx} = 0 \Rightarrow x = 100 \mathrm{cm}$	1						
	$\left \frac{dx}{dx^2} \right _{x=100 \text{ cm}} = -\frac{75}{\pi} < 0 \Rightarrow V \text{ is maximum when } x = 100 \text{ cm.}$							
	Length of rectangle is 100 cm and breadth of rectangle is 50 cm.	1/2						
Q33	Find the area of the region bounded by the lines $x - 2y = 4$, x and x -axis, using integration.	= -1, x = 6						
Ans	x = -1 $x = 6$	For correct figure 1 mark						
	Required area = $\left \int_{-1}^{4} \left(\frac{x-4}{2} \right) dx \right + \int_{4}^{6} \left(\frac{x-4}{2} \right) dx$	2						
	$= \left \frac{(x-4)^2}{4} \right _{-1}^4 + \frac{(x-4)^2}{4} \right _4^6$	1						
	$= \frac{25}{4} + 1 = \frac{29}{4}$	1						
Q34(a)	Find the equation of the line passing through the point of intersection of the lines $\frac{x}{1} = \frac{y-1}{2} = \frac{z-2}{3}$ and $\frac{x-1}{0} = \frac{y}{-3} = \frac{z-7}{2}$							
	and perpendicular to these given lines.							





Ans	$l_1: \frac{x}{1} = \frac{y-1}{2} = \frac{z-2}{3} = \lambda \ ; \ l_2: \frac{x-1}{0} = \frac{y}{-3} = \frac{z-7}{2} = \mu$						
	any point on l_1 is $(\lambda, 2\lambda + 1, 3\lambda + 2)$ & any point on l_2 is $(1, -3\mu, 2\mu + 7)$						
	If l_1 and l_2 intersect,						
	$\lambda = 1, 2\lambda + 1 = -3\mu$ and $3\lambda + 2 = 2\mu + 7 \Rightarrow \lambda = 1$ and $\mu = -1$	1					
	Point of intersection of l_1 and l_2 is $(1,3,5)$.	1					
	Let d.r.'s of required line be $\langle a,b,c \rangle$. Then,						
	$a + 2b + 3c = 0$ and $-3b + 2c = 0 \Rightarrow \frac{a}{13} = \frac{b}{-2} = \frac{c}{-3}$	1					
	Required equation of line is $\frac{x-1}{13} = \frac{y-3}{-2} = \frac{z-5}{-3}$	1					
Q34(b)	2, 1)						
	and B(1, -2, 5). If the equation of the line passing through C and D						
	is $\frac{x-4}{1} = \frac{y+7}{-2} = \frac{z-8}{2}$, then find the distance between sides AB						
	and CD. Hence, find the area of parallelogram ABCD.						
Ans							

Ans A(-1,2,1) B(1,-2,5) C d.r's of CD are < 1, - 2, 2 >

∴ d.r's of AB are
$$< 1, -2, 2 >$$

$$\therefore \text{ Equation of AB is } \frac{x+1}{1} = \frac{y-2}{-2} = \frac{z-1}{2}$$

$$\therefore \text{ Equation of CD is } \frac{x-4}{1} = \frac{y+7}{-2} = \frac{z-8}{2}$$

Let
$$\overrightarrow{a}_1 = -\overrightarrow{i} + 2\overrightarrow{j} + \overrightarrow{k}$$
, $\overrightarrow{a}_2 = 4\overrightarrow{i} - 7\overrightarrow{j} + 8\overrightarrow{k} \otimes \overrightarrow{b} = \overrightarrow{i} - 2\overrightarrow{j} + 2\overrightarrow{k}$
Now, $\overrightarrow{a}_2 - \overrightarrow{a}_1 = 5\overrightarrow{i} - 9\overrightarrow{j} + 7\overrightarrow{k}$

$$\begin{vmatrix} \overrightarrow{a}_2 - \overrightarrow{a}_1 \\ 1 \end{vmatrix} \times \overrightarrow{b} = \begin{vmatrix} \widehat{i} & \widehat{j} & \widehat{k} \\ 5 & -9 & 7 \\ 1 & -2 & 2 \end{vmatrix} = -4\widehat{i} - 3\widehat{j} - \widehat{k}$$



^{*}These answers are meant to be used by evaluators.

	Distance between AB and CD is given by $d = \frac{\left (\vec{a}_2 - \vec{a}_1) \times \vec{b} \right }{\left \vec{b} \right }$	1/2							
	$d = \frac{\sqrt{16 + 9 + 1}}{\sqrt{1 + 4 + 4}} = \frac{\sqrt{26}}{3}$								
	$CD = \sqrt{2^2 + (-4)^2 + (4)^2} = 6$ Area of parallelogram ABCD = b × h = 6 × $\frac{\sqrt{26}}{3}$ = $2\sqrt{26}$	1							
Q35	A relation R on set $A = \{x : -10 \le x \le 10, x \in Z\}$ is define	A relation R on set $A = \{x : -10 \le x \le 10, x \in Z\}$ is defined as							
	$R = \{(x, y) : (x - y) \text{ is divisible by 5}\}$. Show that R is an equivalence relation. Also, write the equivalence class [5].								
Ans									
	For reflexive relation								
	To prove $(x, x) \in \mathbb{R}$, $x - x = 0$ which is divisible by 5	1							
	\therefore $(x, x) \in R \Rightarrow R$ is reflexive								
	For symmetric relation								
	Let $(x, y) \in R \Rightarrow x - y$ is divisible by 5								
	$\Rightarrow x - y = 5m \Rightarrow y - x = 5(-m)$								
	\Rightarrow y - x is divisible by 5								
	\Rightarrow (y, x) \in R : R is symmetric								
	For transitive relation								
	Let $(x, y) \in R$ and $(y, z) \in R$								
	$x - y$ is divisible by 5 $\Rightarrow x - y = 5$ m								
	$y - z$ is divisible by 5 $\Rightarrow y - z = 5$ n	2							
	$\Rightarrow x - y + y - z = 5(m - n) \Rightarrow x - z = 5(m - n)$								
	\therefore x – z is divisible by 5								
	\Rightarrow (x, z) \in R \therefore R is transitive.								
	R is an equivalence relation.								
	$[5] = \{-10, -5, 0, 5, 10\}$	1							

^{*}These answers are meant to be used by evaluators.

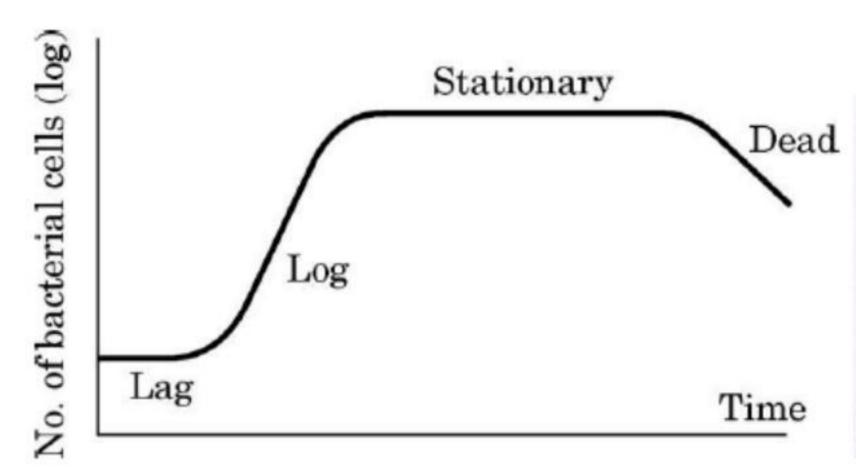


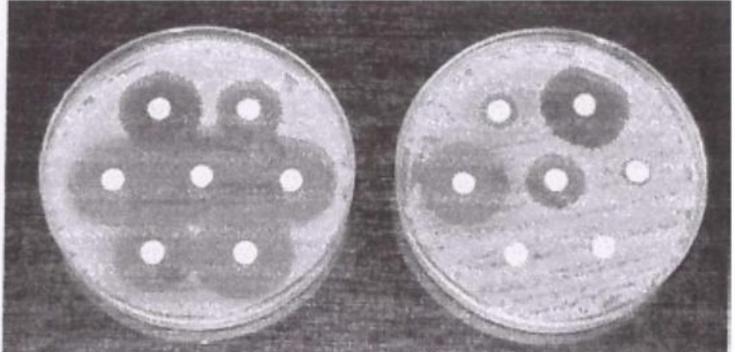
SECTION E

Questions no. 36 to 38 are case study based questions carrying 4 marks each.

Q36

A bacteria sample of certain number of bacteria is observed to grow exponentially in a given amount of time. Using exponential growth model, the rate of growth of this sample of bacteria is calculated.





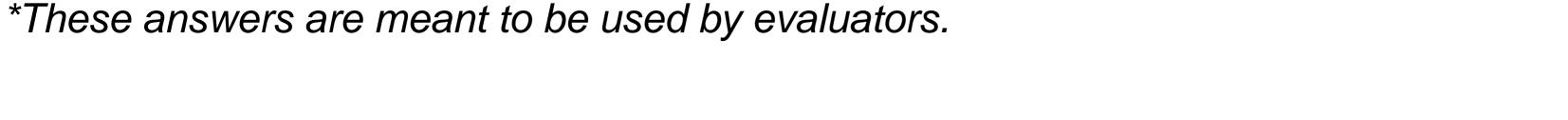
The differential equation representing the growth of bacteria is given as:

 $\frac{dP}{dt}$ = kP, where P is the population of bacteria at any time 't'.

Based on the above information, answer the following questions:

- (i) Obtain the general solution of the given differential equation and express it as an exponential function of 't'.
- (ii) If population of bacteria is 1000 at t = 0, and 2000 at t = 1, find the value of k.

Ans(i)	$\frac{dP}{dt} = kP \Rightarrow \int \frac{dP}{P} = \int k dt$	1
	$\Rightarrow \log P = kt + C \text{ or } P = e^{kt + C}$	1
Ans(ii)	$\log P = kt + C$ when $t = 0$, $P = 1000 \Rightarrow C = \log 1000$ when $t = 1$, $P = 2000 \Rightarrow \log 2000 = k + \log 1000$ $\Rightarrow k = \log 2$	1/2 1/2 1





Q37	A scholarship is a sum of money provided to a student to help him or her pay for education. Some students are granted scholarships based on their academic achievements, while others are rewarded based on their financial needs.								
	Every year a school offers scholarships to girl children and meritorious achievers based on certain criteria. In the session 2022 − 23, the school offered monthly scholarship of ₹ 3,000 each to some girl students and ₹ 4,000 each to meritorious achievers in academics as well as sports.								
	In all, 50 students were given the scholarships and monthly expenditure incurred by the school on scholarships was ₹ 1,80,000.								
	Based on the above information, answer the following questions:								
	(i) Express the given information algebraically using matrices.	1							
	(ii) Check whether the system of matrix equations so obtained is consistent or not.	1							
	(iii) (a) Find the number of scholarships of each kind given by the school, using matrices.	2							
	\mathbf{OR}								
	(iii) (b) Had the amount of scholarship given to each girl child and meritorious student been interchanged, what would be the monthly expenditure incurred by the school?								
Ans(i)	Let No. of girl child scholarships = x								
	No. of meritorious achievers = y								
	x + y = 50								
	$3000x + 4000y = 1800000 \text{ or } 3x + 4y = 180$ $\begin{bmatrix} 1 & 1 \\ 3 & 4 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 50 \\ 180 \end{bmatrix}$	1							
Ans(ii)	$\begin{vmatrix} 1 & 1 \\ 3 & 4 \end{vmatrix} = 1 \neq 0$								
	∴ system is consistent.	1							





Ans (iii)(a)	Let $A = \begin{bmatrix} 1 & 1 \\ 3 & 4 \end{bmatrix}$, $X = \begin{bmatrix} x \\ y \end{bmatrix}$, $B = \begin{bmatrix} 50 \\ 180 \end{bmatrix}$							
	$AX = B \Rightarrow X = A^{-1}B$							
	$X = \begin{bmatrix} 4 & -1 \\ -3 & 1 \end{bmatrix} \begin{bmatrix} 50 \\ 180 \end{bmatrix} = \begin{bmatrix} 20 \\ 30 \end{bmatrix}$							
	$\Rightarrow x = 20, y = 30$							
	$\rightarrow R-20, y-30$, 2						
Ans	OR	19						
(iii)(b)	Required expenditure = \mathbb{Z} [30(3000) + 20(4000)] = \mathbb{Z} 1,70,000	1						
Q38	Self-study helps students to build confidence in learning. It booself-esteem of the learners. Recent surveys suggested that close learners were self-taught using internet resources and up themselves.	to 50%						
	SELF-STUDY							
	A student may spend 1 hour to 6 hours in a day in upskilling self. To probability distribution of the number of hours spent by a student given below:							
	$P(X = x) = \begin{cases} kx^2, & \text{for } x = 1, 2, 3\\ 2kx, & \text{for } x = 4, 5, 6\\ 0, & \text{otherwise} \end{cases}$							
	where x denotes the number of hours.							
	Based on the above information, answer the following questions:							
	(i) Express the probability distribution given above in the form of	fa						
	probability distribution table.	1						
	(ii) Find the value of k.	1						
	(iii) (a) Find the mean number of hours spent by the student.	2						
	\mathbf{OR}							
	(iii) (b) Find P(1 < X < 6).	2						





					1	1	P		8	1	
Ans(i)		X	1	2	3	4	5	6		1	1
	2	P(X)	k	4k	9k	8k	10k	12k		_	
	0								, i	i i	
Ans(ii)											
	K + 4	4k + 9k -	F 8K + 1	.0k + 1	2k = 1					1	
	\Rightarrow_k	_ 1								10 -10 -10	
	K	- 44									
Ans											
(iii) (a)	Mean	Mean = $\sum x_i p_i = k + 8k + 27k + 32k + 50k + 72k$							1		
	= 190k										
	190 95									1	
	$=\frac{190}{44}$ or $\frac{95}{22}$										
A	-					OR					
Ans (iii)(b)	P(1 ·	< X < 6)	=4k+	9k + 8l	z + 10k					78	
(111)(0)	1 (1	P(1 < X < 6) = 4k + 9k + 8k + 10k							1		
		= 31k									
	= 31										
	$= \overline{44}$								1		

