



JEE (MAIN) 2024

MEMORY BASED QUESTIONS & SOLUTIONS

SHIFT-2

DATE & DAY: 27th January 2024 & Saturday

PAPER-1

Duration: 3 Hrs.

Time: 03:00 PM - 06:00 PM

SUBJECT: MATHEMATICS

ADMISSIONS OPEN FOR CLASS 12+

ACADEMIC SESSION 2024-25



TARGET: JEE (ADV.) 2024

For Class XII Passed Student
VISHESH COURSE
MODE: OFFLINE/ONLINE



CLASS STARTS
08th APRIL, 2024



TARGET: JEE (MAIN) 2024

For Class XII Passed Student
ABHYAAS COURSE
MODE: OFFLINE/ONLINE



CLASS STARTS
08th APRIL, 2024

SCHOLARSHIP ON THE BASIS OF JEE (MAIN) 2024 %ILE/AIR

REGISTERED & CORPORATE OFFICE (CIN: U80302RJ2007PLC024029):

CG Tower, A-46 & 52, IPIA, Near City Mall, Jhalawar Road, Kota (Rajasthan) - 324005

0744-2777777 | 73400 10345 | contact@resonance.ac.in | www.resonance.ac.in | Follow Us: @ResonanceEdu

This solutions was download from Resonance JEE (Main) 2024 Solution Portal

PART : MATHEMATICS

1. The coefficient of x^{2012} in $(1-x)^{2008} (1+x+x^2)^{2007}$ is
 (1) 0 (2) 1 (3) 2 (4) 3

Ans. (1)

Sol. $(1-x)^{2008} (1+x+x^2)^{2007} = (1-x) (1-x^3)^{2007}$
 $= (1-x) \sum_{r=0}^{2007} {}^{2007}C_r (-x^3)^r$

$$3r = 2012 \quad \text{or} \quad 3r + 1 = 2012$$

$$r \notin W \quad \quad \quad r \in W$$

2. If the equation $2\tan^2\theta - 5\sec\theta = 1$ has 7 solution in $\theta \in [0, n\frac{\pi}{2}]$, for least value of $n \in \mathbb{N}$ then value of

$$\sum_{k=1}^n \frac{k}{2^n} \text{ is equal to}$$

- (1) $\frac{9}{2^9}$ (2) $\frac{91}{2^{13}}$ (3) $\frac{11}{2^{12}}$ (4) $\frac{7}{2^7}$

Ans. (2)

Sol. $2(\sec^2\theta - 1) - 5\sec\theta - 1 = 0$

$$2\sec^2\theta - 5\sec\theta - 3 = 0$$

$$(2\sec\theta + 1)(\sec\theta - 3) = 0$$

$$(\sec\theta = -\frac{1}{2}) \text{ or } (\sec\theta = 3)$$

↓

Rejected

the solution are in 1st and 4th quadrant only

the least value of n is 13 for which equation has 7 solutions in $[0, \frac{13\pi}{2}]$

$$\text{now } \sum_{k=1}^n \frac{k}{2^n} = \sum_{k=1}^{13} \frac{k}{2^{13}} = \frac{91}{2^{13}}$$

3. $\lim_{x \rightarrow 0} \frac{3 + \alpha \sin x + \beta \cos x + \log_e(1+x)}{3 \tan^2 x} = \frac{1}{3}$, then the value of $(2\alpha - \beta)$ is equal to

Ans. (1)

Sol. $\lim_{x \rightarrow 0} \frac{3 + \alpha \left(x - \frac{x^3}{3!} + \frac{x^5}{5!} \dots \right) + \beta \left(1 - \frac{x^2}{2!} + \frac{x^4}{4!} \right) + \left(x - \frac{x^2}{2} + \frac{x^3}{3} \dots \right)}{3 \tan^2 x} = \frac{1}{3}$

$$\Rightarrow \lim_{x \rightarrow 0} \frac{(3 + \beta) + (\alpha + 1)x - \left(\frac{\beta + 1}{2}\right)x^2 \dots}{3 \tan^2 x} = \frac{1}{3}$$

Resonance Eduventures Ltd.

Reg. Office & Corp. Office : CG Tower, A-46 & 52, IPIA, Near City Mall, Jhalawar Road, Kota (Raj.) - 324005

Ph. No.: +91-744-2777777, 2777700 | FAX No. : +91-022-39167222

To Know more : sms RESO at 56677 | Website : www.resonance.ac.in | E-mail : contact@resonance.ac.in | CIN : U80302RJ2007PLC024029

Toll Free : 1800 258 5555 | 7340010333 | [facebook.com/ResonanceEdu](https://www.facebook.com/ResonanceEdu) | twitter.com/ResonanceEdu | www.youtube.com/resowatch | blog.resonance.ac.in

This solution was download from Resonance JEE (main) 2023 Solution portal

PAGE # 1

$$3 + \beta = 0 \text{ and } \alpha + 1 = 0 \Rightarrow \alpha = -1 \text{ and } \beta = -3$$

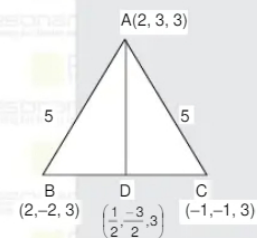
$$\lim_{x \rightarrow 0} \frac{x^2 + \frac{1}{2}x^3 \dots}{3 \tan^2 x} = \frac{1}{3}$$

$$\text{Hence } 2\alpha - \beta = -2 + 3 = 1$$

4. The position vector of the vertices A, B, C of a triangle are $2\hat{i} + 3\hat{j} + 3\hat{k}$, $2\hat{i} - 2\hat{j} + 3\hat{k}$, $-\hat{i} - \hat{j} + 3\hat{k}$ respectively. Let l denotes the length of the angle bisector AD of $\angle BAC$ Where 'D' is on the line segment BC, then $2l^2$ equals ?

Ans. (45)

Sol.



$$l^2 = \left(2 - \frac{1}{2}\right)^2 + \left(3 + \frac{3}{2}\right)^2 + 0$$

$$l^2 = \frac{\pi}{4} + \frac{\pi}{4}$$

$$l^2 = \frac{45}{2}$$

$$2l^2 = 45$$

5. $\int_0^{\pi} \frac{dx}{1 + \alpha^2 - 2\alpha \cos x}$ is equal (where $|\alpha| > 1$)

(1) $\frac{\pi}{1 - \alpha^2}$

(2) $\frac{\pi}{\alpha^2 - 1}$

(3) $\frac{\pi}{2(\alpha^2 - 1)}$

(4) $\frac{\pi}{2(1 - \alpha^2)}$

Ans. (2)

Sol. Let $I = \int_0^{\pi} \frac{dx}{1 + \alpha^2 - 2\alpha \cos x}$

$$I = \frac{1}{2\alpha} \int_0^{\pi} \frac{dx}{\frac{1 + \alpha^2}{2\alpha} - \cos x}$$

Let $a = \frac{1 + \alpha^2}{2\alpha}$ then $|a| > 1$

$$I = \frac{1}{2\alpha} \int_0^{\pi} \frac{dx}{a - \cos x} \text{ where}$$

Resonance Eduventures Ltd.

Reg. Office & Corp. Office : CG Tower, A-46 & 52, IPIA, Near City Mall, Jhalawar Road, Kota (Raj.) - 324005

Ph. No. : +91-744-2777777, 2777700 | FAX No. : +91-022-39167222

To Know more : sms RESO at 56677 | Website : www.resonance.ac.in | E-mail : contact@resonance.ac.in | CIN : U80302RJ2007PLC024029

Toll Free : 1800 258 5555 | 7340010333 | [facebook.com/ResonanceEdu](https://www.facebook.com/ResonanceEdu) | twitter.com/ResonanceEdu | www.youtube.com/resonance | blog.resonance.ac.in

This solution was download from Resonance JEE (main) 2023 Solution portal

PAGE # 2

$$= \frac{1}{2\alpha} \int_0^{\pi} \frac{dx}{a - \frac{1 - \tan^2 x/2}{1 + \tan^2 x/2}}$$

$$= \frac{1}{2\alpha} \int_0^{\pi} \frac{\sec^2 x/2}{(a-1) + (a+1)\tan^2 x/2} dx$$

Let $\tan \frac{x}{2} = t \Rightarrow \frac{1}{2} \sec^2 \frac{x}{2} dx = dt$

$$= \frac{1}{\alpha} \int_0^{\infty} \frac{dt}{(a-1) + (a+1)t^2}$$

$$= \frac{1}{\alpha(a+1)} \int_0^{\infty} \frac{dt}{\left(\frac{a-1}{a+1}\right) + t^2}$$

$$= \frac{1}{\alpha(a+1)} \int_0^{\infty} \frac{dt}{\left(\frac{a-1}{a+1}\right) + t^2}$$

$$= \frac{1}{\alpha(a+1)} \frac{1}{\sqrt{\frac{a-1}{a+1}}} \tan^{-1} \left(\frac{t}{\sqrt{\frac{a-1}{a+1}}} \right) \Bigg|_0^{\infty}$$

$$= \frac{1}{\alpha\sqrt{a^2-1}} [\tan^{-1} \infty - \tan^{-1} 0]$$

$$= \frac{\pi}{2\alpha\sqrt{a^2-1}} = \frac{\pi}{2\alpha\sqrt{\left(\frac{1+\alpha^2}{2\alpha}\right)^2 - 1}} = \frac{\pi}{\sqrt{(1-\alpha^2)^2}} = \frac{\pi}{|1-\alpha^2|} = \frac{\pi}{\alpha^2-1}$$

6. Number of solution of equation $\tan^{-1}x + \tan^{-1}2x = \frac{\pi}{4}$ is

(1) 0

(2) 1

(3) 2

(4) 3

Ans. (2)

Sol. $\tan^{-1}x + \tan^{-1}2x = \frac{\pi}{4}$

$$\tan^{-1}2x = \tan^{-1}1 - \tan^{-1}x$$

$$2x = \frac{1-x}{1+x}$$

$$3x = 1 - 2x^2$$

$$2x^2 + 3x - 1 = 0$$

$$x = \frac{-3 \pm \sqrt{9+8}}{4}$$

$$x = \frac{-3 \pm \sqrt{17}}{4}$$

$$x = \frac{-3 + \sqrt{17}}{4} \text{ is accepted}$$

Number of solution is 1.

Resonance Eduventures Ltd.

Reg. Office & Corp. Office : CG Tower, A-46 & 52, IPIA, Near City Mall, Jhalawar Road, Kota (Raj.) - 324005

Ph. No.: +91-744-2777777, 2777700 | FAX No.: +91-022-39167222

To Know more : sms RESO at 56677 | Website : www.resonance.ac.in | E-mail : contact@resonance.ac.in | CIN : U80302RJ2007PLC024029

Toll Free : 1800 258 5555 | 7340010333 | Facebook.com/ResonanceEdu | Twitter.com/ResonanceEdu | www.youtube.com/resowatch | blog.resonance.ac.in

This solution was download from Resonance JEE (main) 2023 Solution portal

PAGE # 3

Resonance Educating for better tomorrow | JEE (Main) 2024 | DATE : 27-01-2024 (SHIFT-2) | PAPER-1 | MEMORY BASED | MATHEMATICS

7. 20th term from the end of the progression $20, 19\frac{1}{4}, 18\frac{1}{2}, 17\frac{3}{4}, \dots, -129\frac{1}{4}$ is ____.
- (1) -120 (2) -115 (3) -125 (4) -110

Ans. (2)

Sol. $20, 19\frac{1}{4}, 18\frac{1}{2}, 17\frac{3}{4}, \dots, -129\frac{1}{4}$
are in A.P. with common difference

$$d = 19\frac{1}{4} - 20 = -\frac{3}{4}$$

$$20^{\text{th}} \text{ term from end} = -129\frac{1}{4} + (20-1)\left(\frac{3}{4}\right)$$

$$= -129\frac{1}{4} + 19\frac{3}{4}$$

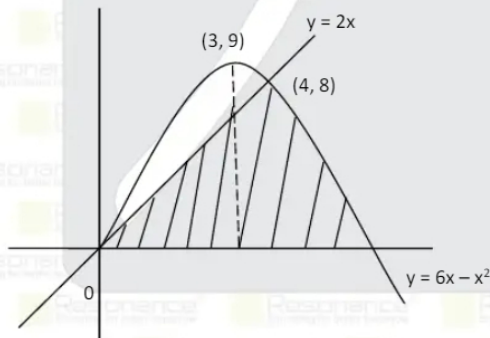
$$= \frac{-517}{4} + \frac{57}{4}$$

$$= \frac{-460}{4} = -115$$

8. A is the area of region $0 \leq y \leq \min(2x; 6x - x^2)$ then find 12A

Ans. (304)

Sol.



Solving $y = 2x$ and $y = 6x - x^2$

$$2x = 6x - x^2$$

$$x^2 - 4x = 0$$

$$y = x = 0, x = 4, y = 8$$

$$A = \frac{1}{2} \cdot 4 \cdot 8 + \int_4^6 (6x - x^2) dx$$

$$= 16 + \left(3x^2 - \frac{x^3}{3} \right)_4^6$$

Resonance Eduventures Ltd.

Reg. Office & Corp. Office : CG Tower, A-46 & 52, IPIA, Near City Mall, Jhalawar Road, Kota (Raj.) - 324005

Ph. No.: +91-744-2777777, 2777700 | FAX No.: +91-022-39167222

To Know more : sms RESO at 56677 | Website : www.resonance.ac.in | E-mail : contact@resonance.ac.in | CIN : U80302RJ2007PLC024029

Toll Free : 1800 258 5555 | 7340010333 | Facebook.com/ResonanceEdu | Twitter.com/ResonanceEdu | www.youtube.com/resowatch | blog.resonance.ac.in

This solution was download from Resonance JEE (main) 2023 Solution portal

PAGE # 4

$$A = 16 + 3(36 - 16) - \frac{1}{3}(216 - 64)$$

$$A = 16 + 60 - \frac{152}{3}$$

$$A = 16 + \frac{28}{3}$$

$$12A = 304 \text{ Ans.}$$

9. α and β are the roots of $x^2 - x - 1 = 0$ and $S_n = 2023\alpha^n + 2024\beta^n$ then
 (1) $S_{12} = S_{11} + S_{10}$ (2) $2S_{12} = S_{11} + S_{10}$ (3) $S_{11} = 2S_{10} + S_{12}$ (4) $S_{10} = S_{11} + S_{12}$

Ans. (1)

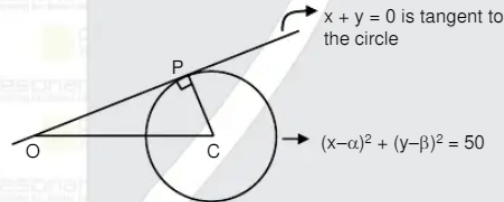
Sol. $x^2 - x - 1 = 0$
 $S_n - S_{n-1} - S_{n-2} = 0$
 $S_n = S_{n-1} + S_{n-2}$
 $S_{12} = S_{11} + S_{10}$
 $n = 12$

10. If circle $(x-\alpha)^2 + (y-\beta)^2 = 50$ and line $x + y = 0$ intersect at only one point P distance of P from origin is $4\sqrt{2}$ then $\alpha^2 + \beta^2$ is

- (1) 81 (2) 82 (3) 85 (4) 169

Ans. (2)

Sol.



$$OP = 4\sqrt{2} \qquad CP = \sqrt{50} = 5\sqrt{2}$$

$$(OC)^2 = \alpha^2 + \beta^2 = (OP)^2 + (PC)^2$$

$$= 16 \times 2 + 50 = 82$$

11. Two finite set A and B have m and n elements respectively. If subset of A is 56 more than that of B then the distance between A (m,n) and B(-2,-3) is

- (1) 8 (2) 10 (3) 11 (4) 15

Ans. (2)

Sol. $2^m - 2^n = 56$

we know that $64 - 8 = 56$

$m = 6, n = 3$

A (6,3), B(-2,-3)

$AB = \sqrt{64+36} = 10$

Resonance Eduventures Ltd.

Reg. Office & Corp. Office : CG Tower, A-46 & 52, IPIA, Near City Mall, Jhalawar Road, Kota (Raj.) - 324005

Ph. No.: +91-744-2777777, 2777700 | FAX No.: +91-022-39167222

To Know more : sms RESO at 56677 | Website : www.resonance.ac.in | E-mail : contact@resonance.ac.in | CIN : U80302RJ2007PLC024029

Toll Free : 1800 258 5555 7340010333 facebook.com/ResonanceEdu twitter.com/ResonanceEdu www.youtube.com/resowatch blog.resonance.ac.in

This solution was download from Resonance JEE (main) 2023 Solution portal

PAGE # 5

12. The value of $\int \frac{(x^9 - x^2)}{(x^{12} + 3x^6 + 1)\tan^{-1}\left(x^3 + \frac{1}{x^3}\right)} dx$

(1) $n \left| \tan^{-1}\left(x^3 + \frac{1}{x^3}\right) \right| + C$

(2) $\frac{1}{2} n \left| \tan^{-1}\left(x^3 - \frac{1}{x^3}\right) \right| + C$

(3) $\frac{1}{3} n \left| \tan^{-1}\left(x^3 + \frac{1}{x^3}\right) \right| + C$

(4) $\frac{1}{2} n \left| \tan^{-1}\left(x^3 + \frac{1}{x^3}\right) \right| + C$

Ans. (3)

$$\begin{aligned}\text{Sol. } \tan^{-1}\left(x^3 + \frac{1}{x^3}\right) &= t \\ \frac{1}{1 + \left(x^3 + \frac{1}{x^3}\right)^2} \times 3\left(x^2 - \frac{1}{x^4}\right) dx &= dt \\ \int \frac{1}{3t} dt &= \frac{1}{3} \ln|t| + C \\ &= \frac{1}{3} \ln\left|\tan^{-1}\left(x^3 + \frac{1}{x^3}\right)\right| + C\end{aligned}$$

13. If mean and standard deviation of 15 observations are 12 and 3 respectively. But an error is found that 10 is written in place of 12. If the correct mean is μ and the correct variance σ^2 then find the value of $15(\mu + \mu^2 + \sigma^2)$

Ans. (2521)

$$\text{Sol. Since } \frac{x_1 + x_2 + x_3 + \dots + x_{15}}{15} = 12 \Rightarrow \sum_{i=1}^{15} x_i = 180$$

but when data's are corrected the new mean is

$$\Rightarrow \mu = \frac{\sum_{i=1}^{15} x_i - 10 + 12}{15} = \frac{180 - 10 + 12}{15} = \frac{182}{15}$$

$$\text{also given SD} = \sqrt{\frac{\sum x_i^2}{15} - (12)^2}$$

$$\Rightarrow 9 + 144 = \frac{\sum x_i^2}{15}$$

$$\Rightarrow \sum_{i=1}^{15} x_i^2 = 153 \times 15 = 2295$$

$$\text{new variance } \sigma^2 = \frac{\sum x_i^2 - 100 + 144}{15} - (\mu)^2$$

$$\sigma^2 + \mu^2 = \frac{2295 + 44}{15}$$

Resonance Eduventures Ltd.

Reg. Office & Corp. Office : CG Tower, A-46 & 52, IPIA, Near City Mall, Jhalawar Road, Kota (Raj.) - 324005

Ph. No.: +91-744-2777777, 2777700 | FAX No.: +91-022-39167222

To Know more : sms RESO at 56677 | Website : www.resonance.ac.in | E-mail : contact@resonance.ac.in | CIN : U80302RJ2007PLC024029

Toll Free : 1800 258 5555 | 7340010333 | Facebook.com/ResonanceEdu | Twitter.com/ResonanceEdu | www.youtube.com/resowatch | blog.resonance.ac.in

This solution was download from Resonance JEE (main) 2023 Solution portal

PAGE # 6

Resonance® Educating for better tomorrow | JEE (Main) 2024 | DATE : 27-01-2024 (SHIFT-2) | PAPER-1 | MEMORY BASED | MATHEMATICS

$$\sigma^2 + \mu^2 = \frac{2339}{15}$$

$$\Rightarrow 15(\mu + \mu^2 + \sigma^2) = 15\left(\frac{182}{15} + \frac{2339}{15}\right)$$

$$= 2521$$

14. If $\frac{dy}{dx} = \frac{x+y-2}{x-y}$ and $y(0) = 2$ then $y(2)$ is

(1) 0

(2) 2

(3) e

(4) e^2

Ans. (1)

Sol. Put $x = X + 1$ & $y = Y + 1$

$$\frac{dY}{dX} = \frac{X+Y}{X-Y}$$

$$Y = vX$$

$$\frac{dY}{dX} = v + X \frac{dv}{dX}$$

$$v + X \frac{dv}{dX} = \frac{1+v}{1-v}$$

$$X \frac{dv}{dX} = \frac{1+v-v+v^2}{1-v}$$

$$\frac{1-v}{1+v^2} dv = \frac{dX}{X}$$

$$\tan^{-1} v - \frac{1}{2} \ln(1+v^2) = \ln(x-1) + c$$

$$\tan^{-1} \left(\frac{y-1}{x-1} \right) - \frac{1}{2} \ln \left(1 + \left(\frac{y-1}{x-1} \right)^2 \right) = \ln(x-1) + c$$

$$x=0, y=2$$

$$-\frac{\pi}{4} - \frac{1}{2} \ln 2 = \ln 1 + c$$

$$c = -\frac{\pi}{4} - \frac{1}{2} \ln 2$$

$$\text{hence at } x=2 \Rightarrow \tan^{-1}(y-1) - \frac{1}{2} \ln(1+(y-1)^2) = c = -\frac{\pi}{4} - \frac{1}{2} \ln 2$$

$$y=0$$

15. A is a 2×2 matrix, I is 2×2 identity matrix. $|A - xI| = 0$ has the roots $-1, 3$. Then find the sum of diagonal elements of A^2 .

Ans. (10)

Sol. Let $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$

$$|A - xI| = 0 \Rightarrow \begin{vmatrix} a-x & b \\ c & d-x \end{vmatrix} = 0$$

Resonance Eduventures Ltd.

Reg. Office & Corp. Office : CG Tower, A-46 & 52, IPIA, Near City Mall, Jhalawar Road, Kota (Raj.) - 324005

Ph. No.: +91-744-2777777, 2777700 | FAX No.: +91-022-39167222

To Know more : sms RESO at 56677 | Website : www.resonance.ac.in | E-mail : contact@resonance.ac.in | CIN : U80302RJ2007PLC024029

Toll Free : 1800 258 5555 | 7340010333 | Facebook.com/ResonanceEdu | Twitter.com/ResonanceEdu | www.youtube.com/resonance | blog.resonance.ac.in

This solution was download from Resonance JEE (main) 2023 Solution portal

PAGE # 7

$$(a-x)(d-x) - bc = 0$$

$$x^2 - (a+d)x + ad - bc = 0$$

has roots -1 & 3

$$a+d=2 \quad ad-bc=-3$$

$$A^2 = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} a & b \\ c & d \end{bmatrix}$$

$$= \begin{bmatrix} a^2+bc & ab+bd \\ ac+cd & bc+d^2 \end{bmatrix}$$

Sum of diagonal element of A^2

$$= a^2 + d^2 + 2bc$$

$$= (a+d)^2 + 2(bc-ad)$$

$$= 4 + 6 = 10$$

16. For $x \in (0, 3)$, $g(x) = 3f\left(\frac{x}{3}\right) + f(3-x)$ and $f''(x) > 0 \forall x \in (0, 3)$

If $g(x)$ is increasing in $(\alpha, 3)$ and decreasing in $(0, \alpha)$ then find ' α '

(1) $\frac{1}{2}$

(2) $\frac{9}{4}$

(3) $\frac{3}{2}$

(4) $\frac{1}{4}$

Ans. (2)

Sol. Since $f''(x) > 0 \Rightarrow f(x)$ is increasing in $(0, 3)$.

$$\text{Now } g'(x) = f'\left(\frac{x}{3}\right) - f'(3-x)$$

For $g(x)$ to be increasing

$$g'(x) = f'\left(\frac{x}{3}\right) - f'(3-x) > 0$$

$$\Rightarrow f'\left(\frac{x}{3}\right) > f'(3-x)$$

$$\Rightarrow \frac{x}{3} > 3-x \Rightarrow x > 9-3x \Rightarrow x > \frac{9}{4}$$

For $g(x)$ to be decreasing

$$g'(x) < 0 \Rightarrow x < \frac{9}{4}$$

$$\alpha = \frac{9}{4}$$

17. Let $f(x) = \int_0^x g(t) \ln\left(\frac{1-t}{1+t}\right) dt$. If g is odd continuous function and $\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \left(f(x) + \frac{x^2 \cos x}{1+e^x} \right) dx = \frac{\pi^2}{\alpha^2} - \alpha$, then

value of α is _____
 (1) 1 (2) 2 (3) 3 (4) 4

Ans. (2)

Sol. $f(x) = \int_0^x g(t) \ln\left(\frac{1-t}{1+t}\right) dt$ is odd function.

Resonance Eduventures Ltd.

Reg. Office & Corp. Office : CG Tower, A-46 & 52, IPIA, Near City Mall, Jhalawar Road, Kota (Raj.) - 324005

Ph. No.: +91-744-2777777, 2777700 | FAX No. : +91-022-39167222

To Know more : sms RESO at 56677 | Website : www.resonance.ac.in | E-mail : contact@resonance.ac.in | CIN : U80302RJ2007PLC024029

Toll Free : 1800 258 5555 | 7340010333 | [facebook.com/ResonanceEdu](https://www.facebook.com/ResonanceEdu) | twitter.com/ResonanceEdu | www.youtube.com/reswatch | blog.resonance.ac.in

This solution was download from Resonance JEE (main) 2023 Solution portal

PAGE # 8

Resonance
 Educating for better tomorrow | JEE (Main) 2024 | DATE : 27-01-2024 (SHIFT-2) | PAPER-1 | MEMORY BASED | MATHEMATICS

Now $\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \left(f(x) + \frac{x^2 \cos x}{1+e^x} \right) dx = \int_0^{\frac{\pi}{2}} \left(\frac{x^2 \cos x (1+e^x)}{1+e^x} \right) dx$

$$= \int_0^{\frac{\pi}{2}} x^2 \cos x dx = (x^2 \sin x) \Big|_0^{\frac{\pi}{2}} - 2 \int_0^{\frac{\pi}{2}} x \sin x dx$$

$$= \frac{\pi^2}{4} + 2(x \cos x) \Big|_0^{\frac{\pi}{2}} - 2 \int_0^{\frac{\pi}{2}} \cos x dx$$

$$= \frac{\pi^2}{4} - 2 \times 1 = \frac{\pi^2}{4} - 2 \Rightarrow \alpha = 2$$

18. Let R be the interior region between the lines $3x - y + 1 = 0$ and $x + 2y - 5 = 0$ containing the origin. The set of all values of a for which the points $(a^2, a + 1)$ lies in R is

- (1) $(-\infty, -1) \cup (3, \infty)$ (2) $(-3, 0) \cup \left(\frac{1}{3}, 1\right)$ (3) $(-\infty, -1) \cup \left(0, \frac{1}{3}\right)$ (4) $(-\infty, -2) \cup \left(0, \frac{1}{3}\right)$

Ans. (2)

Sol. $(a^2, a + 1)$ and $(0, 0)$ lies on the same side of $3x - y + 1 = 0$ and $x + 2y - 5 = 0$
 $\Rightarrow 3a^2 - a - 1 + 1 > 0$ and $a^2 + 2a + 2 - 5 < 0$
 $a(3a - 1) > 0$ and $(a + 3)(a - 1) < 0$



$$a \in (-3, 0) \cup \left(\frac{1}{3}, 1\right)$$

19. If $\begin{vmatrix} 1 & \frac{3}{2} & \alpha + \frac{3}{2} \\ 1 & \frac{1}{3} & \alpha + \frac{1}{3} \\ 2\alpha + 3 & 3\alpha + 1 & 0 \end{vmatrix} = 0$ then α lies in the interval

- (1) $(0, 3)$ (2) $(-3, 0)$ (3) $(-2, 1)$ (4) $(-2, 0)$

Ans. (2)

Sol. $C_3 \rightarrow C_3 - (\alpha C_1 + C_2)$

$$\begin{vmatrix} 1 & \frac{3}{2} & 0 \\ 1 & \frac{1}{3} & 0 \\ 2\alpha + 3 & 3\alpha + 1 & -(2\alpha^2 + 6\alpha + 1) \end{vmatrix} = 0$$

$$\Rightarrow (2\alpha^2 + 6\alpha + 1) = 0$$

$$\Rightarrow \alpha = \frac{-3 + \sqrt{7}}{2}, \frac{-3 - \sqrt{7}}{2}$$

Resonance Eduventures Ltd.

Reg. Office & Corp. Office : CG Tower, A-46 & 52, IPIA, Near City Mall, Jhalawar Road, Kota (Raj.) - 324005

Ph. No.: +91-744-2777777, 2777700 | FAX No. : +91-022-39167222

To Know more : sms RESO at 56677 | Website : www.resonance.ac.in | E-mail : contact@resonance.ac.in | CIN : U80302RJ2007PLC024029

Toll Free : 1800 258 5555 | 7340010333 | [facebook.com/ResonanceEdu](https://www.facebook.com/ResonanceEdu) | twitter.com/ResonanceEdu | www.youtube.com/reswatch | blog.resonance.ac.in

This solution was download from Resonance JEE (main) 2023 Solution portal

PAGE # 9

20. If $f(x) = 6x - x^2$; $x \in [0,2]$ and $g(x) = \begin{cases} \min\{g(t); 0 \leq t \leq x\}, & 0 \leq x < 1 \\ 3+x; & x \in [1,2] \end{cases}$, then numbers of points where $g(x)$

is not differentiable is :

- (1) 1 (2) 0 (3) 2 (4) 3

Ans. (1)

Sol. $f(x) = 6x - x^2$

$$g(x) = \begin{cases} 0; & 0 \leq x < 1 \\ 3+x & 1 \leq x \leq 2 \end{cases}$$

$g(x)$ is not differentiable at $x = 1$

21. Three lines $2x - y - 3 = 0$, $6x + 3y + 4 = 0$, $\alpha x + 2y + 4 = 0$ does not form triangle then find $\left[\sum \alpha^2 \right]$ (where $[.]$ denotes the greatest integer functions)

Ans. (32)

Sol. Triangle will not form if either at least two lines are parallel or lines are concurrent.

If two line are parallel

$$\frac{2}{\alpha} = \frac{-1}{2} \Rightarrow \alpha = -4$$

$$\frac{6}{\alpha} = \frac{3}{2} \Rightarrow \alpha = 4$$

If lines are concurrent

$$\begin{vmatrix} 2 & -1 & -3 \\ 6 & 3 & 4 \\ \alpha & 2 & 4 \end{vmatrix} = 0$$

$$2(12 - 8) + 1(24 - 4\alpha) - 3(12 - 3\alpha) = 0$$

$$8 + 24 - 4\alpha - 36 + 9\alpha = 0$$

$$\alpha = \frac{4}{5}$$

$$\sum \alpha^2 = 16 + 16 + \frac{16}{25}$$

$$\left[\sum \alpha^2 \right] = 32$$

22. Let $S_1 = \frac{(4)!}{4!(3!)}$ and $S_2 = \frac{(5)!}{(5!)^4}$ then

- (1) $S_1 \in \mathbb{N}$ and $S_2 \notin \mathbb{N}$ (2) $S_1 \in \mathbb{N}$ and $S_2 \in \mathbb{N}$
 (3) $S_1 \notin \mathbb{N}$ and $S_2 \in \mathbb{N}$ (4) $S_1 \notin \mathbb{N}$ and $S_2 \notin \mathbb{N}$

Ans. (2)

Sol. divide 24 different objects into 6 persons of 4 each

$$\text{Number of ways of making groups} = \frac{24!}{(4!)^6} = I_1$$

$S_1 \in \mathbb{N}$

divide 120 different objects into 24 persons of 5 each

$$\frac{5!}{(5!)^{24}} = I_2$$

Hence $S_2 \in \mathbb{N}$

Resonance Eduventures Ltd.

Reg. Office & Corp. Office : CG Tower, A-46 & 52, IPIA, Near City Mall, Jhalawar Road, Kota (Raj.) - 324005

Ph. No.: +91-744-2777777, 2777700 | FAX No.: +91-022-39167222

To Know more : sms RESO at 56677 | Website : www.resonance.ac.in | E-mail : contact@resonance.ac.in | CIN : U80302RJ2007PLC024029

Toll Free : 1800 258 5555 | 7340010333 | facebook.com/ResonanceEdu | twitter.com/ResonanceEdu | www.youtube.com/resonance | blog.resonance.ac.in

This solution was download from Resonance JEE (main) 2023 Solution portal

PAGE # 10

Resonance®
Educating for better tomorrow

Boost your Percentile with

PERCENTILE
BOOSTER
COURSE



COURSE

COURSE COMMENCEMENT: 5th FEBRUARY 2024

TARGET

JEE (Main) 2024
April Attempt

MODE:
OFFLINE/
ONLINE

COURSE

Concept

Percentile Booster Course (PBC) is for those students who want to boost their percentile in JEE-Main 2024 through a systematic complete course revision & practice plan.

In this course, daily chapter wise tests, Full Syllabus Test, JEE Preparatory Test will be conducted and each test will be followed by proper offline/online discussion class.

COURSE FEE

Offline: ₹4999 | Online: ₹2499

COURSE FEATURES

- Complete Course Coverage
- Regular Practice through Daily Online Practice Test
- Full Syllabus Test
- Approx 2500 practice Que.
- Chapter wise Test
- Joint Preparatory Test
- Back up support of recorded lectures
- Regular Test discussion classes for concept clearance.

JEE (Main) 2024 April Attempt में

अधिकतम %ile प्राप्त करने के लिए आज ही Join करें।

SCAN TO
APPLY



*T & C Apply

ADMISSIONS OPEN FOR CLASS 12+

ACADEMIC SESSION 2024-25



TARGET: JEE (ADV.) 2024

For Class XII Passed Student
VISHESH COURSE

MODE: OFFLINE/ONLINE



CLASS STARTS
08TH APRIL, 2024



TARGET: JEE (MAIN) 2024

For Class XII Passed Student
ABHYAAS COURSE

MODE: OFFLINE/ONLINE



CLASS STARTS
08TH APRIL, 2024

SCHOLARSHIP ON THE BASIS OF JEE (MAIN) 2024 %ILE/AIR



Resonance[®]
Educating for better tomorrow

JEE (Advanced) 2023 RESULT

AIR
7

BIKINA A. CHOWDARY

All India Ranks (AIR-CRL) in
Top 50 : 8 Top 100 : 15
All Students are from Our
Offline/Online Classroom Programs

AIR **22**



DESHANK P. SINGH

AIR **26**



MAYANK SONI

AIR **29**



TANISHQ M. MANDHANE

AIR **32**



KRITIN GUPTA

AIR **33**



NAMAN GOYAL

AIR **37**



S S SUMEDH

AIR **44**



KAUSHAL VIJAYVERGIYA

JEE (Main) 2023 RESULT

22 वर्षों से लगातार... श्रेष्ठ शिक्षण, श्रेष्ठ परिणाम...

6 AIRs in TOP-50

AIR 5 300/300 Marks	AIR 26 100%ile	AIR 29 100%ile	AIR 31 100%ile	AIR 34 100%ile	AIR 50 100%ile (Maths)
					
KAUSHAL VIJAYVERGIYA	SOHAM DAS	ASHIK STENNY	KRISH GUPTA	MAYANK SONI	HARSHAL LASOD

ADMISSIONS OPEN

Academic Session 2024-25

Class: V to XII & XII+



JEE
(Advanced)



JEE
(Main)



NEET
(UG)

SCHOLARSHIP UPTO



100%

Based on ResoNET (Scholarship Test)

REGISTERED & CORPORATE OFFICE (CIN: U80302RJ2007PLC024029)

CG Tower, A-46 & 52, IPIA, Near City Mall, Jhalawar Road, Kota (Rajasthan) - 324005

0744-2777777 | 73400 10345 | contact@resonance.ac.in | www.resonance.ac.in | Follow Us: [@ResonanceEdu](#) | [@Resonance_Edu](#)