

Optics JEE Main PYQ - 3

Total Time: 25 Minute **Total Marks:** 40

Instructions

Instructions

- 1. Test will auto submit when the Time is up.
- 2. The Test comprises of multiple choice questions (MCQ) with one or more correct answers.
- 3. The clock in the top right corner will display the remaining time available for you to complete the examination.

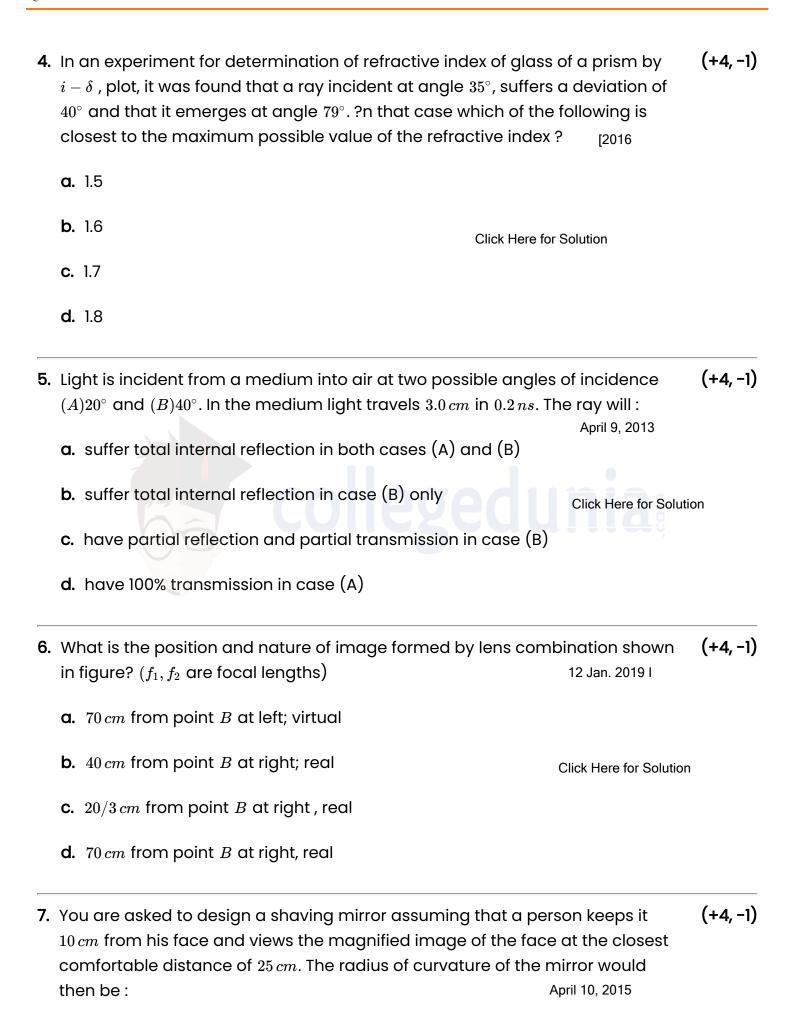
Navigating & Answering a Question

- 1. The answer will be saved automatically upon clicking on an option amongst the given choices of answer.
- 2. To deselect your chosen answer, click on the clear response button.
- 3. The marking scheme will be displayed for each question on the top right corner of the test window.



Optics

1.	. An observer looks at a distant tree of height $10m$ with a telescope of magnifying power of $20.$ To the observer the tree appears : 2016		(+4, -1)
	a. 10 times taller.		
	b. 10 times nearer.	Click Here for Solution	
	c. 20 times taller.		
	d. 20 times nearer.		
2.	If we need a magnification of 375 from a complength $150mm$ and an objective of focal length eye-piece, should be close to: a. $22mm$ b. $12mm$ c. $33mm$	·	(+4, -1)
3.	In an experiment a convex lens of focal length $15cm$ is placed coaxially on an optical bench in front of a convex mirror at a distance of $5cm$ from it. It is found that an object and its image coincide, if the object is placed at a distance of $20cm$ from the lens. The focal length of the convex mirror is : April 9, 2017		(+4, -1)
	b. 20.0 cm	Click Here for Solution	
	c. 25.0 cm		
	d. 30.5 cm		
_			





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b. 24 cm

Click Here for Solution

- **C.** $-60 \, cm$
- **d.** $-24 \, cm$
- 8. One plano-convex and one plano-concave lens of same radius of curvature 'R' but of different materials are joined side by side as shown in the figure. If the refractive index of the material of 1 is μ_1 and that of 2 is μ_2 , then the focal length of the combination is: 10 Apr. 2019 I

(+4, -1)

(+4,

-1)

a.
$$\frac{R}{2-(\mu_1-\mu_2)}$$

Click Here for Solution



- (+4, **9.** A convex lens of refractive index 15 and focal length $18\,cm$ in air is immersed in -1) water. The change in focal length of the lens will be_____ cm (Given refractive index of water = $\frac{4}{3}$) Click Here for Solution 24-Jan-2023 Shift 21
- 10. In an experiment for estimating the value of focal length of converging mirror, image of an object placed at $40\,cm$ from the pole of the mirror is formed at distance $120\,cm$ from the pole of the mirror These distances are measured with a modified scale in which there are 20 small divisions in 1 cm The value of error in measurement of focal length of the mirror is $\frac{1}{K}cm$ The value of K is _____ [30-Jan-2023 Shift 1

Click Here for Solution



Answers

1. Answer: d

Explanation:

Magnification of a telescope is given by:

$$M = \frac{\theta_i}{\theta}$$

$$M=rac{ heta_i}{ heta_o} \ 20=rac{h/d_i}{h/d_o}$$

$$20 = \frac{d_0}{d_i}$$

Distance of image, $d_i = \frac{d_o}{20}$

Concepts:

1. Ray Optics and Optical Instruments:

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Ray optics is also known as the geometrical optics and it is a branch of science which describes light propagation.

Reflection is the change in direction of light at an interface in-between two different media so that the wave-front returns into a medium from which it was originated.

Speed of light is the rate at which the light travels in free space.

A phenomenal change in image formed when the light is passed from one medium to another which is called **Refraction**.

Total Internal Reflection is the reflection of light when the light ray enters into a rarer medium from a denser medium and the angle of incidence is higher than the critical angle of incidence then that light ray will be reflected back to the denser medium.

Read More: <u>Ray Optics and Optical Instruments</u>

2. Answer: a

Explanation:

Given $M = 375, L = 150 \, mm, f_0 = 5 \, mm, f_0 = ?, d = 25 \, cm$.

M for a compound microscope is given by

$$M=rac{v_0}{+u_0}\left(1+rac{d}{fe}
ight)$$

focal length of objective lens is small $u_0 \simeq f_0$.

Alos as focal length of eye is small $v_0 \simeq L$

$$\therefore M = rac{L}{+f_0} \left(1 + rac{d}{f_e}
ight)$$

$$ightarrow 375 = rac{150}{5} \left(1 + rac{250}{f_e}
ight)$$

$$\Rightarrow \frac{375}{30} = \left(1 + \frac{250}{f_e}\right)$$

$$\Rightarrow \frac{375}{30} - 1 = \frac{250}{f_e}$$
$$\Rightarrow \frac{345}{30} = \frac{250}{f_e}$$

$$\Rightarrow \frac{345}{30} = \frac{250}{f_c}$$

$$\Rightarrow f_e = 2.2 \, cm$$

$$F_e=22\,mm$$

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3. Answer: a

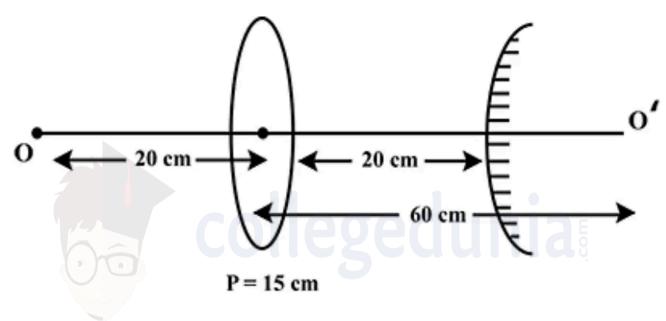
Explanation:

The correct answer is (A): 27.5 cm

Given: u= -20cm

f = 15 cm

distance (d) of convex lens= 5cm



By substituting the values in equation (1) we get,

$$\frac{1}{v} + \frac{1}{20} = \frac{1}{15}$$

$$\Rightarrow \frac{1}{v} = \frac{1}{15} - \frac{1}{20}$$

$$\Rightarrow \frac{1}{v} = \frac{5}{300}$$

$$\Rightarrow v = \frac{300}{5}$$

$$\Rightarrow v = 60 \ cm$$

Thus, the image will be formed at 60cm to the right of the lens and it will be inverted.

Therefore, distance between lens and mirror will be

d = image distance - radius of curvature of convex mirror

$$d = v - 2f$$

By substituting the values in above equation we get,

$$5 = 60 - R$$

$$\Rightarrow R = 55$$

But, the radius of curvature (R) is given by,

$$R = 2f$$

$$\Rightarrow f = rac{55}{2}$$

 $\Rightarrow f = 27.5$

Hence, the focal length of the convex mirror is 27.5cm.

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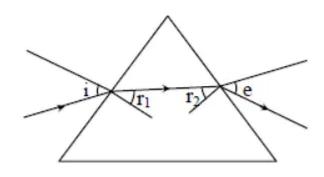
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4. Answer: a

Explanation:





$$\delta = i + e - A$$
 $40 = 35 + 79 - A$
 $40 = 114 - A$
 $A = 114 - 40 = 74 = r_1 + r_2$

From this we get,

$$\mu = 1.5$$

$$\therefore \delta_{min} < 40^{\circ}$$

$$\mu < \frac{\sin\left(\frac{70+40}{2}\right)}{\sin 37}$$

$$\therefore \mu_{max} = 1.44$$

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5. Answer: b

Explanation:

Velocity of light in medium

$$V_{med} = rac{3 \ cm}{0.2 ns} = rac{3 imes 10^{-2} m}{0.2 imes 10^{-9} s} = 1.5 \ m/s$$

Refractive index of the medium

$$\mu=rac{V_{air}}{V_{med}}=rac{3 imes 10^8}{1.5}=2\,m/s$$
 As $\mu=rac{1}{sin\,C}$

As
$$\mu = \frac{1}{\sin C}$$

$$\therefore \sin C = \frac{1}{u} = \frac{1}{2} = 30^{\circ}$$

Condition of TIR is angle of incidence i must be greater than critical angle. Hence ray will suffer TIR in case of (B) ($i=40^{\circ}>30^{\circ}$) only.

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6. Answer: d

Explanation:

For first lens

$$\frac{\frac{1}{V} - \frac{1}{-20} = \frac{1}{5}}{V = \frac{20}{3}}$$

For second lens

$$V = \frac{20}{3} - 2 = \frac{14}{3}$$

$$\frac{1}{V} - \frac{1}{\frac{14}{3}} = \frac{1}{-5}$$

$$V = 70cm$$

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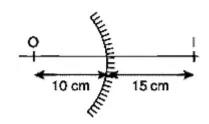
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7. Answer: c

Explanation:

When object before a concave mirror line within its focal length, its image is virtual, erect and on the other side. Since he wants his image to lie at 25cm from him, it is 15cm behind the mirror.



$$\frac{1}{u} + \frac{1}{v} = \frac{1}{f}$$

$$\Rightarrow \frac{1}{-10} + \frac{1}{15} = \frac{1}{f}$$

$$\Rightarrow \frac{-3+2}{30} = \frac{1}{f}$$

$$\Rightarrow f = -30 cm \text{ (Concave mirror)}$$

$$R = 2f = -60 cm$$

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8. Answer: d

Explanation:

For 1st lens
$$\frac{1}{f_1}=\left(\frac{\mu_1-1}{1}\right)\left(\frac{1}{\infty}-\frac{1}{-R}\right)=\frac{\mu_1-1}{R}$$
 for 2nd lens $\frac{1}{f_2}=\left(\frac{\mu_2-1}{1}\right)\left(\frac{1}{-R}-0\right)=-\frac{\mu_2-1}{R}$ $\frac{1}{f_{eq}}=\frac{1}{f_1}+\frac{1}{f_2}$ $\frac{1}{f_{eq}}=\frac{R}{\mu_1-1}+\frac{R}{-(\mu_2-1)}\Rightarrow \frac{1}{f_{eq}}=\frac{R}{\mu_1-\mu_2}$ Hence $f_{eq}=\frac{\mu_1-\mu_2}{R}$

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9. Answer: 54 - 54

Explanation:

The correct answer is 54.

$$\begin{split} &\frac{I}{f_{H_2O}} = \left(\frac{\mu_g}{\mu_{H_2O}} - 1\right) \left(\frac{2}{R}\right) \\ &= \frac{1}{8} \left(\frac{2}{R}\right) \\ &= \frac{1}{(4f_{air})} \\ \text{So, } &f_{H_2O} = 4f_{\text{air}} = 72\,cm \\ \text{So change in focal length} &= 72 - 18 = 54\,cm \end{split}$$

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Explanation:

The correct answer is 32.

$$\begin{array}{l} \frac{1}{v}+\frac{1}{u}=\frac{1}{f}\\ \frac{-1}{120}-\frac{1}{40}=\frac{1}{f},\ \ f=-30\,cm\\ \text{Now,}\\ \frac{-1}{v^2}dv-\frac{1}{u^2}du=-\frac{1}{f^2}df\\ \text{Also } dv=du=\frac{1}{20}cm\\ \therefore \frac{\frac{1}{20}}{(120)^2}+\frac{\frac{1}{20}}{(40)^2}=\frac{df}{(30)^2}\\ \text{On solving}\\ df=\frac{1}{32}\,cm\\ \therefore k=32 \end{array}$$

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