

## ANSWERS

- |          |          |          |          |          |          |          |          |          |          |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 1.1 (b)  | 1.2 (b)  | 1.3 (c)  | 1.4 (d)  | 1.5 (d)  | 1.6 (d)  | 1.7 (c)  | 1.8 (a)  | 1.9 (a)  | 1.10 (a) |
| 1.11 (b) | 1.12 (b) | 1.13 (a) | 1.14 (d) | 1.15 (c) | 1.16 (d) | 1.17 (b) | 1.18 (b) | 1.19 (b) | 1.20 (c) |
| 1.21 (c) | 1.22 (c) | 1.23 (a) | 1.24 (c) | 1.25 (d) | 1.26 (a) | 1.27 (c) | 1.28 (d) | 1.29 (c) | 1.30 (a) |
| 1.31 (a) | 1.32 (a) | 1.33 (c) | 1.34 (a) | 1.35 (d) | 1.36 (b) | 1.37 (c) | 1.38 (b) | 1.39 (d) | 1.40 (b) |
| 1.41 (b) | 1.42 (a) | 1.43 (b) | 1.44 (c) | 1.45 (b) | 1.46 (*) | 1.47 (c) | 1.48 (b) |          |          |

## EXPLANATIONS

**EE.1.**

1.1.  $C(t) = -te^{-t} + 2e^{-t},$   
 $(t \geq 0)$

$$C(s) = -\frac{1}{(s+1)^2} + \frac{2}{s+1} = \frac{2s+1}{(s+1)^2}$$

$$C(s) = \frac{G(s)}{1+G(s)},$$

$$G(s) = \frac{C(s)}{1-C(s)} = \frac{\frac{2s+1}{(s+1)^2}}{1-\frac{2s+1}{(s+1)^2}} = \frac{2s+1}{s^2}$$

1.2.  $\frac{C(s)}{R(s)} = \frac{G(s)}{1+G(s)},$

$$\frac{G(s)}{1-G(s)} = \frac{\frac{1}{s(s+1)}}{1+\frac{1}{s(s+1)}} = \frac{1}{s^2+s+1}$$

$$\omega_n = 1, \quad \omega_n = \frac{1}{2}, \quad \zeta = \frac{1}{2}$$

$$M_p = e^{-\xi\sqrt{1-\zeta^2}} = e^{(-\pi/2)/\sqrt{1-(1/4)}} \\ = e^{-\pi/4} = 0.163$$

1.4.  $\frac{C(s)}{R(s)} = \frac{1}{1+s}, \quad \frac{C(j\omega)}{R(j\omega)} = \frac{1}{1+j\omega}$

From  $r(t) \sin t, \quad \omega = 1, \quad \left| \frac{C(j\omega)}{R(j\omega)} \right| = \frac{1}{\sqrt{1+1}} = \frac{1}{\sqrt{2}}$

$$\left| \frac{C(j\omega)}{R(j\omega)} \right| = -\tan^{-1} 1 = -\frac{\pi}{4}$$

$$\therefore \text{SS value of } c(t) = \frac{1}{\sqrt{2}} \sin \left( t - \frac{\pi}{4} \right)$$

1.5. The Periodic time = 4 ms =  $4 \times 10^{-3}$  sec.

$\therefore$  Fundamental frequency

$$= \frac{10^3}{4} = 250 \text{ Hz}$$

$\therefore$  Frequency of the 5th harmonic  
 $= 250 \times 5 = 1250 \text{ Hz}$

1.6. As the element absorbs power, let it be  $R_x$ .

$$i = 1 = \frac{6}{R_x + 1}$$

$$R_x = 5 \Omega$$

$$P = \left(\frac{6}{6}\right)^2 2 \times 5 = 5 \text{ W.}$$

For 5 A,

$$P = 52 \times 5 = 125 \text{ W}$$

For  $3 + \sqrt{14}$ ,

$$P = 227 \text{ W}$$

For  $3 - \sqrt{14}$ ,

$$P = 2.75 \text{ W.}$$

Hence none of the above is correct

1.7.  $P = \frac{1}{2} (1 - \cos 2\omega t) = 100 \text{ Hz}$

1.8. Voltage across the capacitor at any time  $t$

$$v_c = V (1 - e^{-t/RC})$$

$$= 1 - e^{-t/RC}$$

since

$$V = 1 \text{ volt}$$

$$\therefore \frac{dv_c}{dt} = \frac{1}{RC} e^{-t/RC},$$

At  $t = 0^+$ ,  $\frac{dv_c}{dt} = \frac{1}{RC}$

1.9.  $R = \frac{8}{4 \times 10^{-3}} = 2000 \Omega.$

$$\text{Time constant} = \frac{L}{R} = \frac{6 \times 10^{-3}}{2 \times 10^3} = 3 \mu \text{sec.}$$

