



# JEE (MAIN) 2024

MEMORY BASED QUESTIONS & SOLUTIONS

SHIFT-2

**DATE & DAY:** 29<sup>th</sup> January 2024 & Monday

**PAPER-1**

**Duration:** 3 Hrs.

**Time:** 03:00 PM - 06:00 PM

**SUBJECT: MATHEMATICS**

**ADMISSIONS OPEN FOR CLASS 12+**

ACADEMIC SESSION 2024-25



TARGET: JEE (ADV.) 2024

For Class XII Passed Student  
**VISHESH COURSE**  
MODE: OFFLINE/ONLINE



CLASS STARTS  
08<sup>th</sup> APRIL, 2024



TARGET: JEE (MAIN) 2024

For Class XII Passed Student  
**ABHYAAS COURSE**  
MODE: OFFLINE/ONLINE



CLASS STARTS  
08<sup>th</sup> APRIL, 2024

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**PART : MATHEMATICS**

1. If  $\sin \frac{y}{x} = \ln |x| + \frac{\alpha}{2}$  is a solution of differential equation  $x \cos \frac{y}{x} \frac{dy}{dx} = y \cos \frac{y}{x} + x$  where  $y(1) = \frac{\pi}{3}$  then

$\alpha^2 =$

Ans. (3)

Sol. Given differential equation is  $x \cos \frac{y}{x} \frac{dy}{dx} - y \cos \frac{y}{x} = x$

$$\Rightarrow \cos \frac{y}{x} \left( x \frac{dy}{dx} - y \right) = x$$

$$\Rightarrow \cos \frac{y}{x} \left( \frac{x \frac{dy}{dx} - y \cdot 1}{x^2} \right) = \frac{1}{x}$$

$$\text{Let } \frac{y}{x} = t$$

$$\cos t \frac{dt}{dx} = \frac{1}{x}$$

$$\cos t dt = \frac{1}{x} dx$$

on integration

$$\sin t = \ln |x| + c$$

$$y(1) = \frac{\pi}{3} \Rightarrow \sin \frac{\pi}{3} = 0 + c$$

$$\Rightarrow c = \frac{\sqrt{3}}{2}$$

$$\therefore \text{ solution is } \sin \frac{y}{x} = \ln |x| + \frac{\sqrt{3}}{2}$$

$$\therefore \frac{\alpha}{2} = \frac{\sqrt{3}}{2} \Rightarrow \alpha^2 = 3$$

2. Find remainder when  $(64)^{32}$  divided by 9.

Ans. (1)

$$\begin{aligned} \text{Sol. } & (64)^{32} = (8^4)^{32} \\ & = 8^{2048} \\ & = (9-1)^{2048} \\ & = {}^{2048}C_0 9^{2048} - {}^{2048}C_1 9^{2047} + {}^{2048}C_2 9^{2046} - \dots + {}^{2048}C_{2045} 9 - {}^{2048}C_{2046} \\ & = 9K + 1 \\ & \text{Remainder} = 1 \end{aligned}$$

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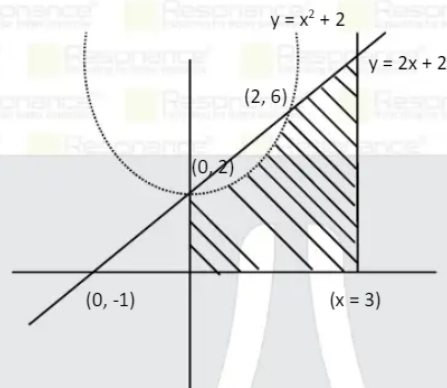
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3. Area bounded by  $0 \leq x \leq 3$ ,  $0 \leq y \leq \text{minimum}(2x+2, x^2+2)$  is A then 12A is  
(1) 164 (2) 170 (3) 180 (4) 184

Ans. (1)

Sol.



$$A = \int_0^2 (x^2 + 2) dx + \int_2^3 (2x + 2) dx$$

$$A = \left( \frac{x^3}{3} + 2x \right)_0^2 + \left( x^2 + 2x \right)_2^3$$

$$A = \frac{41}{3} \Rightarrow 12A = 164$$

4. Let  $\cos(2\sin^{-1}x) = \frac{1}{9}$ ,  $x > 0$  holds true for  $x = \frac{m}{n}$ , where  $m$  and  $n$  are co-prime further  $\alpha$  and  $\beta$  are root of quadratic equation  $mx^2 - nx - m + n = 0$ , ( $\alpha > \beta$ ) then point  $(\alpha, \beta)$  lies on the line
- (1)  $5x - 8y = 9$       (2)  $5x + y = 9$       (3)  $8x + 5y = 9$       (4)  $8x - 5y = 9$

**Ans.** (3)

**Sol.**  $\sin^{-1}x = \theta \in 1^{\text{st}}$  quadrant

$$\cos 2\theta = \frac{1}{9} \Rightarrow 1 - 2\sin^2\theta = \frac{1}{9} \Rightarrow \sin^2\theta = \frac{4}{9}$$

$$\Rightarrow x^2 = \frac{4}{9} \Rightarrow x = \frac{2}{3} = \frac{m}{n}$$

So  $mx^2 - nx - m + n = 0$

$$\Rightarrow 2x^2 - 3x + 1 = 0$$

roots are  $1, \frac{1}{2}$

$$\alpha = 1, \beta = \frac{1}{2}$$

So  $(\alpha, \beta) = \left(1, \frac{1}{2}\right)$  lies on  $5x + 8y = 9$

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5.  $\int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \sqrt{1 - \sin 2\theta} d\theta = \alpha + \beta\sqrt{2} + \gamma\sqrt{3}$  then  $3\alpha + 4\beta - \gamma =$

- (1) 6      (2) 8      (3) 9      (4) 12

**Ans.** (1)

**Sol.**  $I = \int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \sqrt{1 - \sin 2\theta} d\theta$

$$= \int_{\frac{\pi}{6}}^{\frac{\pi}{3}} |\sin\theta - \cos\theta| d\theta$$

$$= \int_{\frac{\pi}{6}}^{\frac{\pi}{4}} (\cos\theta - \sin\theta) d\theta + \int_{\frac{\pi}{4}}^{\frac{\pi}{3}} (\sin\theta - \cos\theta) d\theta$$

$$= [\sin\theta + \cos\theta]_{\frac{\pi}{6}}^{\pi/4} + [-\cos\theta - \sin\theta]_{\frac{\pi}{4}}^{\pi/3}$$

$$= \frac{2}{\sqrt{2}} - \frac{1}{2} - \frac{\sqrt{3}}{2} - \left( \frac{1}{2} + \frac{\sqrt{3}}{2} - \frac{2}{\sqrt{2}} \right)$$

$$= \frac{2}{\sqrt{2}} - \frac{1}{2} - \frac{\sqrt{3}}{2} - \frac{1}{2} - \frac{\sqrt{3}}{2} + \frac{2}{\sqrt{2}}$$

$$= -1 + \frac{4}{\sqrt{2}} - \sqrt{3}$$

$$= -1 + 2\sqrt{2} - \sqrt{3}$$

$$\alpha = -1, \beta = 2, \gamma = -1$$

$$\therefore 3\alpha + 4\beta - \gamma = -3 + 8 + 1 = 6$$

6. 8 identical book are to be place in 4 identical shelf. Find the number of different ways can be done.

**Ans.** (165)

**Sol.**  $x_1 + x_2 + x_3 + x_4 = 8$        $x_i \geq 0 \forall i \in \{1, 2, 3\}$

$${}^8 P_4 {}^4 C_3 = {}^{11} C_3 = \frac{11 \cdot 10 \cdot 9}{6} = 165$$

7. Find the probability that number selected from 1 to 50 such that number is divisible by at least by 4, 6 or 7

- (1)  $\frac{21}{50}$       (2)  $\frac{1}{2}$       (3)  $\frac{19}{50}$       (4)  $\frac{23}{50}$

**Ans.** (1)

**Sol.** Number divisible by 4, 6 or 7 (from 1 to 5)  
 $= \{4, 8, 12, \dots, 48\} \cup \{6, 18, 30, 42\} \cup \{7, 14, 21, 35, 49\}$   
 Favourable no's = 21 no's  
 Probability =  $\frac{21}{50}$

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8. If  $a_1, a_2, \dots$  are in G.P. such that  $a_1 = \frac{1}{8}$ ,  $a_1 \neq a_2$  and every term is equal to arithmetic mean of its two successive terms then find  $S_{20} - S_{18}$ .

(1)  $-2^{15}$  (2)  $-2^{18}$  (3)  $-2^{20}$  (4)  $-2^{21}$

**Ans.** (1)

**Sol.**  $T_n = \frac{T_{n+1} + T_{n+2}}{2}$

$$\Rightarrow 2ar^{n-1} = ar^n + ar^{n+1}$$

$$\Rightarrow r^2 + r = 2 \Rightarrow r = 1 \text{ or } -2$$

$$\Rightarrow r \neq 1 \because (a_1 \neq a_2) \Rightarrow r = -2$$

Now

$$S_{20} - S_{18} = T_{19} + T_{20}$$

$$= ar^{18} + ar^{19}$$

$$= ar^{18}(1 + r)$$

$$= \frac{1}{8} (-2)^{18} (-1) = -2^{15}$$

9. Distance of  $(2, 4)$  from the line  $2x + y + 2 = 0$  measured parallel to the  $\sqrt{3}x + y + 2 = 0$  is

(1)  $20(2 - \sqrt{3})$  (2)  $20(2 + \sqrt{3})$  (3)  $20(3 - \sqrt{2})$  (4)  $20(3 + \sqrt{2})$

**Ans.** (2)

**Sol.** Slope of line  $\sqrt{3}x + y + 2 = 0$  is  $-\sqrt{3} = \tan\theta$

$$\cos\theta = -\frac{1}{2}, \sin\theta = \frac{\sqrt{3}}{2}$$

line through  $(2, 4)$  whose slope is  $-\sqrt{3}$  is

$$\frac{x-2}{-\frac{1}{2}} = \frac{y-4}{\frac{\sqrt{3}}{2}} = r$$

$$x = 2 - \frac{r}{2}, y = 4 + \frac{\sqrt{3}}{2}r$$

$$\text{line is } 2x + y + 2 = 0$$

$$4 - r + 4 + \frac{\sqrt{3}}{2}r + 2 = 0$$

$$\left(1 - \frac{\sqrt{3}}{2}\right)r = 10 \Rightarrow r = \frac{20}{2 - \sqrt{3}} = 20(2 + \sqrt{3})$$

10. If  $\alpha$  and  $\beta$  are roots of the equation  $x^2 - \sqrt{6}x + 3 = 0$  and where  $\text{Im}(\beta) < 0$  if  $\frac{\alpha^{99}}{\beta} + \beta^{98} = 3(a + ib)$  then

find  $a + b + n$

**Ans.** (47)

**Sol.**  $x^2 - \sqrt{6}x + 3 = 0$

$$x = \frac{\sqrt{6} \pm \sqrt{6-12}}{2} = \frac{\sqrt{6} \pm \sqrt{-6}}{2}$$

$$\frac{\sqrt{6}(1+i)}{2} = \alpha$$

$$\frac{\sqrt{6}(1-i)}{2} = \beta$$

$$\therefore \alpha^2 = 3i, \beta^2 = -3i$$

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$$\begin{aligned} \frac{\alpha^{99} + \beta^{98}}{\beta} + \beta^{98} &= \frac{\alpha^{99} + \beta^{99}}{\beta} = \frac{\alpha(\alpha^2)^{49} + \beta(\beta^2)^{49}}{\beta} \\ &= \frac{\alpha(3i)^{49} + \beta(-3i)^{49}}{\beta} = \frac{3^{49}(\alpha i - \beta i)}{\beta} \\ &= \frac{3^{49}(-\sqrt{6})2}{\sqrt{6}(1-i)2} = \frac{-3^{49}(1+i)2}{2} \\ &= -3^{49}(1+i) = 3^{49}(-1-i) \\ n &= 49, a = -1, b = -1 \end{aligned}$$

11. If mean of 5 terms =  $\frac{24}{5}$  & variance of terms =  $\frac{194}{25}$  & mean of 4 terms =  $\frac{7}{2}$ , then find variance of 4 terms ?

- (1)  $\frac{5}{2}$  (2)  $\frac{5}{3}$  (3)  $\frac{5}{4}$  (4) 1

Ans. (3)

Sol.  $\frac{X_1 + X_2 + X_3 + X_4 + X_5}{5} = \frac{24}{5} \Rightarrow X_1 + X_2 + X_3 + X_4 + X_5 = 24$

&  $\frac{X_1 + X_2 + X_3 + X_4}{4} = \frac{7}{2} \Rightarrow X_1 + X_2 + X_3 + X_4 = 14$

$\therefore X_5 = 10$

also  $\frac{X_1^2 + X_2^2 + X_3^2 + X_4^2 + X_5^2}{5} - \frac{576}{25} = \frac{194}{25}$

$\Rightarrow X_1^2 + X_2^2 + X_3^2 + X_4^2 = 54$

$\therefore \text{Var.} = \frac{\sum_{i=1}^4 X_i^2}{4} - \left(\frac{\sum_{i=1}^4 X_i}{4}\right)^2$

$= \frac{54}{4} - \frac{49}{4} = \frac{5}{4}$

12. If  $r = |z|$ ,  $\theta = \arg(z)$  and  $z = 2 - 2i \tan\left(\frac{5\pi}{8}\right)$  then find  $(r, \theta)$

- (1)  $\left(2 \sec \frac{5\pi}{8}, \frac{3\pi}{8}\right)$  (2)  $\left(2 \sec \frac{3\pi}{8}, \frac{3\pi}{8}\right)$  (3)  $\left(2 \tan \frac{3\pi}{8}, \frac{5\pi}{8}\right)$  (4)  $\left(2 \tan \frac{3\pi}{8}, \frac{3\pi}{8}\right)$

Ans. (2)

Sol.  $z = 2 - 2i \tan \frac{5\pi}{8}$

$= 2 + 2i \tan\left(\pi - \frac{5\pi}{8}\right)$

$= 2 + 2i \tan \frac{3\pi}{8}$

$= 2 \sec \frac{3\pi}{8} \left(\cos \frac{3\pi}{8} + i \sin \frac{3\pi}{8}\right)$

$\therefore r = 2 \sec \frac{3\pi}{8}, \theta = \frac{3\pi}{8}$

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13. If  $A = \{1, 2, 3, 4\}$  then minimum number of ordered pair added to make it equivalence relation on set A containing (1,3) and (1,2) is

- (1) 8 (2) 9 (3) 12 (4) 16

Ans. (1)

Sol. Minimum ordered pairs are (1,1) (2,2), (3,3), (4,4), (3,1), (2,1), (2,3), (3,2) "8 ordered pairs"

14. If  $\ell na, \ell nb, \ell nc$  are in A.P. and  $\ell na - \ell n2b, \ell n2b - \ell n3c, \ell n3c - \ell na$  are in A.P. then  $a : b : c$  is

- (1) 1 : 2 : 3 (2) 7 : 7 : 4 (3) 9 : 6 : 4 (4) 4 : 6 : 9

Ans. (3)

Sol.  $\ell na, \ell nb, \ell nc$  are in A.P.  $\Rightarrow a, b, c$  are in G.P.



$\ln a - \ln 2b, \ln 2b - \ln 3c$  and  $\ln 3c - \ln a$  are in A.P.

$$\Rightarrow \frac{a}{2b}, \frac{2b}{3c}, \frac{3c}{a} \text{ are also in G.P.}$$

Let  $a = a, b = ar, c = ar^2$

So,  $\frac{1}{2r}, \frac{2}{3r}, 3r^2$  are in G.P.

$$\Rightarrow \frac{4}{9r^2} = \frac{3}{2}r \Rightarrow r^3 = \frac{8}{27} \Rightarrow r = \frac{2}{3}$$

$$a : b : c = 1 : \frac{2}{3} : \frac{4}{9} \Rightarrow 9 : 6 : 4$$

15.  $y = \log_e \left( \frac{1+x^2}{1-x^2} \right)$  then find  $225(y'' - y')$  at  $x = \frac{1}{2}$

Ans. (736)

Sol.  $y = \ln(1+x^2) - \ln(1-x^2)$

$$\frac{dy}{dx} = \frac{2x}{1+x^2} + \frac{2x}{1-x^2}$$

$$= \frac{2x(1-x^2+1+x^2)}{1-x^4} = \frac{4x}{1-x^4}$$

$$\frac{d^2y}{dx^2} = 4 \cdot \frac{(1-x^4) \cdot 1 - x \cdot (-4x^3)}{(1-x^4)^2}$$

$$= 4 \cdot \frac{1-x^4+4x^4}{(1-x^4)^2} = \frac{4(1+3x^4)}{(1-x^4)^2}$$

$$\therefore \frac{dy}{dx} - \frac{d^2y}{dx^2} = \frac{4x}{1-x^4} - \frac{4(1+3x^4)}{(1-x^4)^2}$$

$$\text{Put } x = \frac{1}{2}$$

$$\left( \frac{dy}{dx} - \frac{d^2y}{dx^2} \right)_{\text{at } x = \frac{1}{2}} = \frac{2}{1 - \frac{1}{16}} - \frac{4 \left( 1 + \frac{3}{16} \right)}{\left( 1 - \frac{1}{16} \right)^2}$$

$$= \frac{32}{15} - \frac{4 \cdot 19 \cdot 16}{225} = \frac{480 - 1216}{225} = \frac{-736}{225}$$

$$\Rightarrow 225(y'' - y') \text{ at } x = \frac{1}{2} = 736$$

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16. If  $p(3, 2, 3)$ ,  $Q(4, 6, 2)$ ,  $R(7, 3, 2)$  are the vertices of  $\Delta PQR$ , then find  $\angle QPR =$

- (1)  $\cos^{-1} \frac{1}{18}$  (2)  $\frac{\pi}{6}$  (3)  $\frac{\pi}{3}$  (4)  $\cos^{-1} \frac{7}{18}$

Ans. (3)

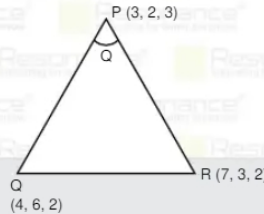
Sol. A

D.R of  $PR = \langle 1, 4, -1 \rangle$

D.R of  $PQ = \langle 4, 1, -1 \rangle$

$$\cos \theta = \frac{1 \times 4 + 4 \times 1 + (-1) \times (-1)}{\sqrt{1+16+1} \sqrt{16+1+1}}$$

$$\Rightarrow \cos \theta = \frac{1}{2} \Rightarrow \theta = \frac{\pi}{3}$$



17.  $(\alpha, \beta)$  lies on the  $y^2 = 4x$  and  $(\alpha, \beta)$  also lies on chord with mid point  $\left(1, \frac{5}{4}\right)$  of another parabola  $x^2 = 8y$ ,

then value  $|(8 - \beta)(\alpha - 28)|$  is

- (1) 192 (2) 92 (3) 64 (4) 128

Ans. (A)

Sol. Let  $(\alpha, \beta) = (t^2, 2t)$

Now equation chord with mid point  $\left(1, \frac{5}{4}\right)$  to the parabola  $x^2 = 8y$

$$\Rightarrow x - 4 \left( y + \frac{5}{4} \right) = 1 - 10$$

$$\Rightarrow x - 4y + 4 = 0$$

$$(t^2, 2t) \text{ satisfy } x - 4y + 4 = 0$$

$$t^2 - 8t + 4 = 0$$

$$\begin{aligned} |(8-\beta)(\alpha-28)| &= |(8-2t)(t^2-28)| \\ &= |(8-2t)(8t-4-28)| = 2(4-t)8(t-4) = 16|t^2-8t+16| \\ 16 \times 12 &= 192 \end{aligned}$$

18. In which interval the function  $f(x) = \frac{x}{x^2-6x-16}$  is increasing

- (1)  $\phi$                       (2)  $\left[1, \frac{3}{7}\right) \cup \left(\frac{5}{4}, \infty\right)$                       (3)  $\left(\frac{5}{4}, \infty\right)$                       (4)  $\left[\frac{3}{4}, \frac{5}{4}\right]$

Ans. (1)

Sol.  $f(x) = \frac{x}{x^2-6x-16}$

$$= f'(x) = \frac{(x^2-6x-16)1-x(2x-6)}{(x^2-6x-16)^2}$$

$$= \frac{x^2-6x-16-2x^2+6x}{(x^2-6x-16)^2}$$

$$= \frac{-x^2-16}{(x^2-6x-16)^2} < 0 \forall x \in Df$$

$\therefore f(x)$  is decreasing

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19. If  $\vec{OA} = \vec{a}$ ,  $\vec{OC} = \vec{b}$  and area of  $\Delta OAC$  is  $S$  and a parallelogram with sides parallel to  $\vec{OA}$  and  $\vec{OC}$  and diagonal  $\vec{OB} = 12\vec{a} + 4\vec{b}$ , has area equal to  $B$ , then  $\frac{B}{S}$  is equal to \_\_\_\_\_.

Ans. (96)

Sol. area of  $\Delta = \frac{1}{2} |\vec{a} \times \vec{b}| = S$                       (1)

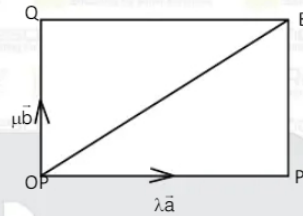
$$\therefore \vec{OB} = \lambda\vec{a} + \mu\vec{b} = 12\vec{a} + 4\vec{b}$$

$$\therefore \text{area of } ||gm = |\vec{OP} \times \vec{OQ}|$$

$$= |12\vec{a} \times 4\vec{b}|$$

$$B = 48 |\vec{a} \times \vec{b}|$$

$$\therefore \frac{B}{S} = \frac{48 |\vec{a} \times \vec{b}|}{\frac{1}{2} |\vec{a} \times \vec{b}|} = 96$$



20. Unit vector  $\hat{u} = x\hat{i} + y\hat{j} + z\hat{k}$  makes angles  $\frac{\pi}{2}, \frac{\pi}{3}, \frac{2\pi}{3}$  with  $\left(\frac{1}{\sqrt{2}}\hat{i} + \frac{1}{\sqrt{2}}\hat{k}\right), \left(\frac{1}{\sqrt{2}}\hat{j} + \frac{1}{\sqrt{2}}\hat{k}\right)$  and  $\left(\frac{1}{\sqrt{2}}\hat{i} + \frac{1}{\sqrt{2}}\hat{j}\right)$  respectively and  $\vec{v} = \frac{1}{\sqrt{2}}\hat{i} + \frac{1}{\sqrt{2}}\hat{j} + \frac{1}{\sqrt{2}}\hat{k}$ . Find  $|\vec{u} - \vec{v}|$

- (1)  $\sqrt{\frac{5}{2}}$                       (2)  $\sqrt{\frac{7}{2}}$                       (3)  $\sqrt{\frac{2}{5}}$                       (4)  $\sqrt{\frac{7}{3}}$

Ans. (1)

Sol.  $\vec{u} = x\hat{i} + y\hat{j} + z\hat{k}$ ,  $\vec{a}_1 = \frac{1}{\sqrt{2}}\hat{i} + \frac{1}{\sqrt{2}}\hat{k}$ ,  $\vec{a}_2 = \frac{1}{\sqrt{2}}\hat{j} + \frac{1}{\sqrt{2}}\hat{k}$ ,  $\vec{a}_3 = \frac{1}{\sqrt{2}}\hat{i} + \frac{1}{\sqrt{2}}\hat{j}$

$$\because \vec{u} \perp \vec{a}_1 \therefore \vec{u} \cdot \vec{a}_1 = 0 \Rightarrow \frac{x}{\sqrt{2}} + \frac{z}{\sqrt{2}} = 0 \Rightarrow x + z = 0$$

$$\vec{u} \cdot \vec{a}_2 = \frac{\pi}{3} \therefore \vec{u} \cdot \vec{a}_2 = |\vec{u}| |\vec{a}_2| \cos \frac{\pi}{3}$$

$$\frac{1}{\sqrt{2}}y + \frac{1}{\sqrt{2}}z = \frac{1}{2} \Rightarrow y + z = \frac{1}{\sqrt{2}}$$

$$\vec{u} \cdot \vec{a}_3 = \frac{2\pi}{3} \therefore \frac{1}{\sqrt{2}}x + \frac{1}{\sqrt{2}}y = -\frac{1}{2} \Rightarrow x + y = -\frac{1}{\sqrt{2}}$$

$$\therefore x + y + z = 0$$

$$y = 0, x = \frac{-1}{\sqrt{2}}, z = \frac{1}{\sqrt{2}}$$

$$\therefore -1, 1, 1$$

$$u = \frac{1}{\sqrt{2}}i + \frac{1}{\sqrt{2}}k$$

$$\vec{u} - \vec{v} = \frac{-2}{\sqrt{2}}i - \frac{1}{\sqrt{2}}j$$

$$\therefore |\vec{u} - \vec{v}| = \sqrt{\frac{4}{2} + \frac{1}{2}} = \sqrt{\frac{5}{2}}$$

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21. Consider function  $f(x) = 2x + 3x^{2/3}$
- (1) Exactly 1 local minima & no local maxima
  - (2) Exactly 1 local minima & 1 local maxima
  - (3) No local minima & 1 local maxima
  - (4) No local maxima & 1 local minima

Ans. (2)

Sol.  $f(x) = 2x + 3x^{2/3}$

$$f'(x) = 2 + 3 \cdot \frac{2}{3} x^{\frac{2}{3}-1}$$

$$= 2 + 2x^{-\frac{1}{3}}$$

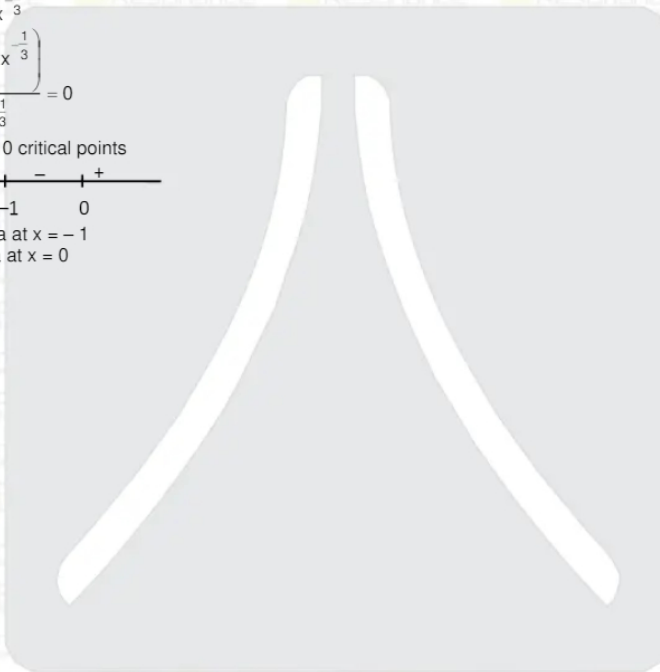
$$= \frac{2 \left( 1 + x^{-\frac{1}{3}} \right)}{x^{\frac{1}{3}}} = 0$$

$$x = -1, 0 \text{ critical points}$$

$$\begin{array}{c} + \quad - \quad + \\ | \quad | \quad | \\ -1 \quad 0 \end{array}$$

Maxima at  $x = -1$

Minima at  $x = 0$



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