



JEE (MAIN) 2024

MEMORY BASED QUESTIONS & SOLUTIONS

SHIFT-2

DATE & DAY: 30th January 2024 & Tuesday

PAPER-1

Duration: 3 Hrs.

Time: 03:00 PM - 06:00 PM

SUBJECT: MATHEMATICS

ADMISSIONS OPEN FOR CLASS 12+

ACADEMIC SESSION 2024-25



TARGET: JEE (ADV.) 2024

For Class XII Passed Student
VISHESH COURSE
MODE: OFFLINE/ONLINE



CLASS STARTS
08th APRIL, 2024



TARGET: JEE (MAIN) 2024

For Class XII Passed Student
ABHYAAS COURSE
MODE: OFFLINE/ONLINE



CLASS STARTS
08th APRIL, 2024

SCHOLARSHIP ON THE BASIS OF JEE (MAIN) 2024 %ILE/AIR

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PART : MATHEMATICS

1. Let S_k denotes sum of first k terms of sequence 3, 7, 11, 15, Value of n, if

$$40 < \frac{6}{n(n+1)} \sum_{k=1}^n S_k < 42, \text{ is } \underline{\hspace{2cm}}$$

Ans. (9)

Sol. $S_k = 3 + 7 + 11 + \dots$ up to k terms

$$= \frac{k}{2} [6 + (k-1)4] = k(2k+1)$$

$$\sum_{k=1}^n (2k^2 + k) = \frac{2n(n+1)(2n+1)}{6} + \frac{n(n+1)}{2}$$

$$40 < 2(2n+1) + 3 < 42$$

$$35 < 4n < 37$$

$$8.75 < n < 9.25$$

$$n = 9$$

2. Let $f(x) = \frac{x}{(1+x^4)^{\frac{1}{4}}}$ & $g(x) = f(f(f(f(x))))$ then $\int_0^{\sqrt{2\sqrt{5}}} x^2 g(x) dx$ is

(1) $\frac{13}{6}$

(2) $\frac{6}{13}$

(3) $\frac{2}{5}$

(4) $\frac{7}{2}$

Ans. (1)

Sol. $\frac{x}{(1+x^4)^{\frac{1}{4}}} = \frac{x}{(1+2x^4)^{\frac{1}{4}}}$
 $\left(\frac{x}{1+x^4}\right)^{\frac{1}{4}} = \frac{x}{(1+2x^4)^{\frac{1}{4}}}$

So $f(f(f(f(x)))) = \frac{x}{(1+4x^4)^{\frac{1}{4}}} = g(x)$

$$\int_0^{\sqrt{2\sqrt{5}}} x^2 g(x) dx = \int_0^{\sqrt{2\sqrt{5}}} \frac{x^3}{(1+4x^4)^{\frac{1}{4}}} dx$$

$$\int_1^3 \frac{1}{4} \frac{t^3 dt}{t} = \frac{1}{4} \int_1^3 t^2 dt = \frac{1}{12} (27-1) = \frac{26}{12} = \frac{13}{6}$$

$$1+4x^4 = t^4$$

$$16x^3 dx = 4t^3 dt$$

$$x^3 dx = \frac{1}{4} t^3 dt$$

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3. $\vec{a} \cdot \vec{b} = 3\sqrt{2}$ & $|\vec{b}|^2 = 6$ such that $\vec{a} = \hat{i} + \alpha\hat{j} + \beta\hat{k}$. If angle between \vec{a} & \vec{b} is $\frac{\pi}{4}$ then value of

$$(\alpha^2 + \beta^2) |\vec{a} \times \vec{b}|^2 \text{ is } \underline{\hspace{2cm}}$$

Ans. (90)

Sol. $\vec{a} \cdot \vec{b} = 3\sqrt{2}$

$$|\vec{a}| |\vec{b}| \cos \frac{\pi}{4} = 3\sqrt{2}$$

$$|\vec{a}| \sqrt{6} \cdot \frac{1}{\sqrt{2}} = 3\sqrt{2}$$

$$|\vec{a}| = \sqrt{6} = \sqrt{1 + \alpha^2 + \beta^2}$$

$$\alpha^2 + \beta^2 = 5$$

$$|\vec{a} \times \vec{b}|^2 = |\vec{a}|^2 |\vec{b}|^2 \sin^2 \frac{\pi}{4} = 6 \times 6 \times \frac{1}{2} = 18$$

So $(\alpha^2 + \beta^2) |\vec{a} \times \vec{b}|^2 = 5 \times 18 = 90$

4. $R = \begin{bmatrix} x & 0 & 0 \\ 0 & y & 0 \\ 0 & 0 & z \end{bmatrix}$, $x \sin \theta = y \sin \left(0 + \frac{2\pi}{3}\right) = z \sin \left(0 + \frac{4\pi}{3}\right) \neq 0$

Statement - 1 : Trace (R) = 0

Statement - 2 : Trace (adj(adj(R))) = 0

- (1) Statement -1 is true and statement - 2 is false (2) Statement -1 is false and statement - 2 is false
 (3) Statement -1 is false and statement - 2 is true (4) Statement -1 is true and statement - 2 is true

Ans. (2)

Sol. $y = \frac{x \sin \theta}{\sin\left(\theta + \frac{2\pi}{3}\right)}, z = \frac{x \sin \theta}{\sin\left(\theta + \frac{4\pi}{3}\right)}$

$$x + y + z = \frac{-3x}{4 \sin\left(\theta + \frac{2\pi}{3}\right) \sin\left(\theta + \frac{4\pi}{3}\right)} \neq 0$$

⇒ Statement-1 is wrong

$$R = \begin{bmatrix} x & 0 & 0 \\ 0 & y & 0 \\ 0 & 0 & z \end{bmatrix}, \text{adj } R = \begin{bmatrix} yz & 0 & 0 \\ 0 & xz & 0 \\ 0 & 0 & xy \end{bmatrix}$$





$$\text{adj}(\text{adj } R) = \begin{bmatrix} x^2 yz & 0 & 0 \\ 0 & y^2 xz & 0 \\ 0 & 0 & z^2 xy \end{bmatrix} \Rightarrow \text{Tr}(\text{adj}(\text{adj } R)) = xyz(x + y + z) \neq 0$$

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5. If $|\vec{a} \times \vec{b}| = 2$, and $|\vec{a}| = 1$, then $|\vec{a} \times \vec{b}| - |\vec{a}|^2$ is

Ans. (5)

Sol. $|\vec{a} \times \vec{b}| = 2$ and $|\vec{a}| = 1 = |\vec{a} \times \vec{b}| - |\vec{a}|^2 = |\vec{a} \times \vec{b}|^2 + |\vec{a}|^2 - 2\vec{a}(\vec{a} \times \vec{b}) = (2)^2 + 1 - 0 = 5$

6. If 11th term of G.P., whose 1st term is 'a' and 3rd term is 'b', is equal to pth term of G.P. whose first term is 'a' and 5th term is 'b', then value of p is

Ans. (21)

Sol. ($T_1 = a, T_3 = ar_1^2 = b \Rightarrow r_1^2 = b/a$) and ($T_1 = a, T_5 = ar_2^4 = b$)

11th term of first GP = pth term of second G.P.

$$a(r_1)^{10} = a(r_2)^{p-1}$$

$$\left(\frac{b}{a}\right)^{10} = \left(\frac{b}{a}\right)^{p-1} \Rightarrow 5 = \frac{p-1}{4} \Rightarrow p = 21$$

7. Let $f(x) = \begin{cases} x^2 + 3x + a; & x \leq 1 \\ bx + 2; & x > 1 \end{cases}$ is differentiable everywhere. The value of $\int_{-2}^2 f(x) dx$ is

(1) $\frac{37}{2}$

(2) $\frac{36}{2}$

(3) $\frac{37}{4}$

(4) $\frac{36}{4}$

Ans. (1)

Sol. f(x) is continuous at x = 1

$$f(1^-) = f(1) = f(1^+)$$

$$a + 4 = b + 2 \Rightarrow b = a + 2$$

f(x) is differential at x = 1

$$f'(1^-) = f'(1^+)$$

$$5 = b \Rightarrow a = 3$$

$$\text{Now } \int_{-2}^2 f(x) dx = \int_{-2}^1 (x^2 + 3x + 3) dx + \int_1^2 (5x + 2) dx$$

$$= \left(\frac{x^3}{3} + \frac{3x^2}{2} + 3x\right)_{-2}^1 + \left(\frac{5x^2}{2} + 2x\right)_1^2 = \left(\frac{1}{3}(1+8) + \frac{3}{2}(1-4) + 9\right) + \frac{5}{2}(4-1) + 2$$

$$= 3 - \frac{9}{2} + 9 + \frac{15}{2} + 2 = 14 + \frac{9}{2} = \frac{37}{2}$$

8. Bag A contains 3 white & 7 red balls and bag B contains 2 white & 3 Red balls. If a ball is picked up randomly then what is the probability that the ball picked is white from bag A

(1) $\frac{3}{20}$

(2) $\frac{2}{20}$

(3) $\frac{3}{10}$

(4) $\frac{4}{20}$

Ans. (1)

Sol. Let

A is event that bag A is selected

B is event that red bag B is selected

W is event that white ball is drawn

$$P(A) = P(B) = \frac{1}{2}$$

$$P(A \cap W) = P(A)P\left(\frac{W}{a}\right) = \frac{1}{2} \cdot \frac{3}{10} = \frac{3}{20}$$

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9. $f(x)$ is double differentiable function. Tangent at $(1, f(1))$ and $(3, f(3))$ cuts positive x -axis at an angle $\frac{\pi}{6}$

and $\frac{\pi}{4}$ then value of $\int_1^3 ((f'(x))^2 + 1) f''(x) dx$ is:

(1) $\frac{4}{3} - \frac{10}{9\sqrt{3}}$

(2) $\frac{3}{4} - \frac{10}{9\sqrt{3}}$

(3) $\frac{4}{3} - \frac{10}{\sqrt{3}}$

(4) $\frac{4}{3} - \frac{1}{9\sqrt{3}}$

Ans. (1)

Sol. $f'(1) = \tan \frac{\pi}{6} = \frac{1}{\sqrt{3}}, f'(3) = 1$

$$I = \int_1^3 ((f'(x))^2 + 1) f''(x) dx$$

Let $f(x) = t$

$f''(x) dx = dt$

$$I = \int_{\frac{1}{\sqrt{3}}}^1 (t^2 + 1) dt = \left(\frac{t^3}{3} + t \right) \Big|_{\frac{1}{\sqrt{3}}}^1 = \frac{4}{3} - \frac{10}{9\sqrt{3}}$$

10. Area bounded by $(y-2)^2 = x-1$, $x-2y+4=0$ and positive coordinate axes, is

Ans. (5)

Sol. Solving $y-2 = \frac{x}{2}$ and $(y-2)^2 = x-1$

$$x^2 = 4x - 4$$

$$(x-2)^2 = 0$$

$$x = 2$$

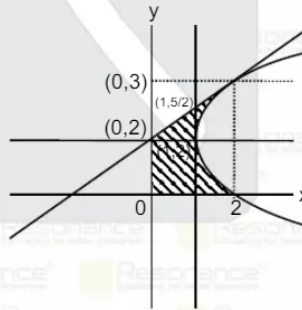
$$y = 3$$

$$\text{Area} = \int_0^3 (x_P - x_L) dy$$

$$= \int_0^3 (y-2)^2 + 1 - 2y + 4 dy = \int_0^3 (y^2 - 6y + 9) dy = \int_0^3 (y-3)^2 dy$$

$$\left(\frac{(y-3)^3}{3} \right) \Big|_0^3 = 0 + \frac{27}{3} = 9$$

required area = $9 - \frac{1}{2} \times 4 \times 2 = 5$



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PAGE # 4

11. Let $f(x) = ae^{2x} + be^x + cx$, where $f(0) = -1$, $f'(\log_e 2) = 21$ and $\int_0^{\log_e 4} (f(x) - cx) dx = \frac{39}{2}$ then the value of

$|a + b + c|$ is _____.

Ans. (8)

Sol. $f(0) = a + b = -1$ _____ (1)

$$f(x) = 2ae^{2x} + be^x + c$$

$$f'(\log_e 2) = 8a + 2b + c = 21$$
 _____ (2)

$$\int_0^{\log_e 4} (f(x) - cx) dx = \int_0^{\log_e 4} (ae^{2x} + be^x) dx$$

$$= \frac{a}{2}(16-1) + b(4-1)$$

$$= \frac{15a}{2} + 3b = \frac{39}{2}$$
 _____ (3)

$$\Rightarrow \frac{9a}{2} + 3(a+b) = \frac{39}{2} \Rightarrow \frac{9a}{2} = \frac{45}{2} \Rightarrow a = 5$$

From (2) $b = -6$ also $c = -7$

$$|a + b + c| = |5 - 6 - 7| = 8$$

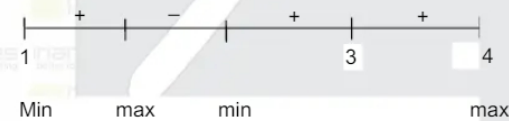
12. If $f(x) = (x-2)^2(x-3)^3$ for $x \in [1, 4]$. If M and m denote maximum and minimum values respectively then $M-m$ is

Ans. (12)

Sol. $f(x) = 2(x-2)(x-3)^3 + 3(x-2)^2(x-3)^2$

$$= (x-2)(x-3)^2(2x-6+3x-6)$$

$$= (5x-12)(x-2)(x-3)^2$$



Local max at $x = 2$ and $x = 4$

Local min at $x = \frac{12}{5}$ and $x = 1$

$$f(1) = 1 \times (-8) = -8$$

$$\begin{cases} f(2) = 0 \\ f\left(\frac{12}{5}\right) = -\frac{12}{125} \\ f(4) = 4 \times 1 = 4 \end{cases}$$

$$M = 4$$

$$m = -8$$

$$M - m = 4 - (-8) = 12$$

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13. A question paper has three sections A, B, C having 8, 6, 4 questions respectively. If the student has to answer 15 questions attempting atleast four from each section. Find the number of ways the paper can be answered by student.

(1) 342 (2) 344 (3) 374 (4) 340

Ans. (2)

Sol. 8 6 4

A B C

$$7 \quad 4 \rightarrow {}^8C_7 \times {}^6C_4 \times {}^4C_4$$

$$6 \quad 5 \quad 4 \rightarrow {}^8C_6 \times {}^6C_5 \times {}^4C_4$$

$$5 \quad 6 \quad 4 \rightarrow {}^8C_5 \times {}^6C_6 \times {}^4C_4$$

An adding all cases we get

$$({}^8C_7 \times {}^6C_4 \times {}^4C_4) + ({}^8C_6 \times {}^6C_5 \times {}^4C_4) + ({}^8C_5 \times {}^6C_6 \times {}^4C_4)$$

$$= \left(8 \times \frac{6 \times 5}{2} \times 1\right) + \left(\frac{8 \times 7}{2} \times 6 \times 1\right) + \left(\frac{8 \times 7 \times 6}{3 \times 2}\right)$$

$$= 120 + 168 + 56 = 344$$

14. Consider the system of equations

$$x + y + z = 5$$

$$x + 2y + \lambda^2 z = 9$$

$$x + 3y + \lambda z = \mu$$

(1) system has unique solution for $\lambda = 1, \mu \neq 13$

(2) system has infinite solution for $\lambda = 1, \mu = 13$

(3) system is inconsistent for $\lambda = 1, \mu \in \mathbb{R}$

(4) system has infinite solution for $\lambda = 1, \mu \neq 13$

Ans. (2)

Sol. $x + y + z = 5$ (1)

$x + 2y + \lambda^2 z = 9$ (2)

$x + 3y + \lambda z = \mu$ (3)

from (1) + (3) - 2(2)

$$z(\lambda + 1 - 2\lambda^2) = (\mu - 13)$$

for infinite solution $\lambda = -1/2, 1$ and $\mu = 13$

15. Let $\alpha, \beta \in \left(0, \frac{\pi}{2}\right)$, $3\sin(\alpha + \beta) = 2\sin(\alpha - \beta)$ and $\tan \alpha = k \tan \beta$ then the value of k is

(1) -5

(2) 5

(3) 3

(4) -3

Ans. (1)

Sol. $3\sin(\alpha + \beta) = 2\sin(\alpha - \beta)$

$$\frac{\sin(\alpha + \beta)}{\sin(\alpha - \beta)} = \frac{2}{3}$$

$$\frac{\sin(\alpha + \beta) + \sin(\alpha - \beta)}{\sin(\alpha + \beta) - \sin(\alpha - \beta)} = \frac{5}{-1}$$

$$\frac{2\sin \alpha \cos \beta}{2\cos \alpha \sin \beta} = \frac{5}{-1}$$

$$\frac{\tan \alpha}{\tan \beta} = -5$$

$$k = -5$$

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16. $L_1 = \hat{i} - \hat{j} + 2\hat{k} + \lambda(\hat{i} - \hat{j} + 2\hat{k})$ $\lambda \in \mathbb{R}$

$$L_2 = \hat{j} - \hat{k} + \mu(3\hat{i} + \hat{j} + p\hat{k})$$

$$L_3 = s(\hat{i} + m\hat{j} + n\hat{k})$$

L_1 is perpendicular to L_2

L_3 is perpendicular to L_1 & L_2

then (ℓ, m, n) can be

(1) (-1, 7, 4)

(2) (4, -1, 7)

(3) (7, 4, -1)

(4) (7, -1, 4)

Ans. (1)

Sol. Since L_1 is perpendicular to L_2

$$\Rightarrow (\hat{i} - \hat{j} + 2\hat{k}) \cdot (3\hat{i} + \hat{j} + p\hat{k}) = 0$$

$$3 - 1 + 2p = 0 \Rightarrow p = -1$$

$L_3 \perp L_1$ & L_2

$$\Rightarrow L_3 \text{ is parallel to } (\hat{i} - \hat{j} + 2\hat{k}) \times (3\hat{i} + \hat{j} + p\hat{k})$$

$$(\hat{i} - \hat{j} + 2\hat{k}) \times (3\hat{i} + \hat{j} + p\hat{k}) = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & -1 & 2 \\ 3 & 1 & -1 \end{vmatrix} = -\hat{i} + 7\hat{j} + 4\hat{k}$$

$$\ell = -1, m = 7, n = 4$$

17. If $A = \{1, 2, 3, 4\}$ then find number of symmetric relation on A which is not reflexive is

Ans. (960)

Sol. If set A has n elements then number of symmetric relation = $2^{\frac{n^2+n}{2}} = 2^{10} (\because n = 4)$

number of reflexive and symmetric relation = $2^{\frac{n^2-n}{2}} = 2^6 (\because n = 4)$

number of relation which is symmetric but not reflexive = $2^{10} - 2^6 = 960$

18. Find number of common roots of the equations $Z^{1901} + Z^{100} + 1 = 0$ and $Z^3 + 2Z^2 + 2Z + 1 = 0$
 (1) 2 (2) 3 (3) 4 (4) 6

Ans. (1)

Sol. $Z^3 + 2Z^2 + 2Z + 1 = 0$

$(Z+1)(Z^2 - Z + 1) + 2Z(Z+1) = 0$

$(Z+1)(Z^2 + Z + 1) = 0$

$\Rightarrow Z = -1, Z = \omega, \omega^2$

$Z = -1$ does not satisfy $Z^{1901} + Z^{100} + 1 = 0$

If $Z = \omega \Rightarrow Z^{1901} + Z^{100} + 1 = \omega^{1901} + \omega^{100} + 1$

$= \omega^{1899} \cdot \omega^2 + \omega^{99} \times \omega + 1$

$= \omega^2 + \omega + 1 = 0$

If $Z = \omega^2 \Rightarrow Z^{1901} + Z^{100} + 1 = \omega^{2(1901)} + \omega^{100} + 1$

$= \omega + \omega^2 + 1 = 0$

Number common roots = 2

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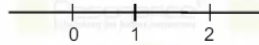
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19. Find number of real solutions of the equation $x(x^2 + |x| + 5|x-1| - 6|x-2|) = 0$
 (1) 2 (2) 3 (3) 4 (4) 6

Ans. (2)
 Sol.



Case-I : If $x \geq 2$

$x(x^2 + x + 5x - 5 - 6x + 12) = 0$

$x(x^2 + 7) = 0 \Rightarrow x = 0$ (Rejected)

Case-II : if $1 \leq x < 2$

$x(x^2 + x + 5x - 5 + 6x - 12) = 0$

$x(x^2 + 12x - 17) = 0 \Rightarrow$ one solution in $[1, 2)$

Case-III: If $0 \leq x < 1$

$x(x^2 + x - 5x + 5 + 6x - 12) = 0$

$x(x^2 + 2x - 7) = 0 \Rightarrow x = 0$ is only solution in $[0, 1)$

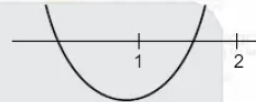
Case-IV : If $x < 0$

$x(x^2 - x - 5x + 5 + 6x - 12) = 0$

$x(x^2 - 7) = 0 \Rightarrow x = 0, \sqrt{7}, -\sqrt{7}$

$x = -\sqrt{7}$ is only the solution

So number of required solution is 3



20. $f\left(\frac{x}{y}\right) = \frac{f(x)}{f(y)}$ and $f(1) = 2024$, then

(1) $x f(x) - 2024 f(x) = 0$

(2) $2024 f(x) = f(x)$

(3) $f(x) - 2024 f(x) = 0$

(4) None of these

Ans. (1)

Sol. Put $x = y = 1$

$f(1) = 1$

Now put $x = 1 \Rightarrow f\left(\frac{1}{y}\right) = \frac{1}{f(y)}$

$f(y) = \pm y^n$

but $f(1) = 1 \Rightarrow f(y) = y^n$

$$r(y) = ny^{n-1} \Rightarrow r(1) = n = 2024$$

$$f(x) = x^{2024}$$

$$f'(x) = 2024 x^{2023}$$

$$xf'(x) = 2024 f(x) \Rightarrow xf'(x) - 2024f(x) = 0$$

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21. $\sum_{r=0}^n \frac{{}^n C_r \cdot {}^n C_r}{r+1} = \alpha, \sum_{r=0}^n \frac{{}^n C_r \cdot {}^{n+1} C_r}{r+1} = \beta$. If $4\beta = 7\alpha$ then n is

Ans. (6)

Sol. $\alpha = \frac{1}{n+1} \sum_{r=0}^n {}^{n+1} C_{r+1} \cdot {}^n C_r$

$$\alpha = \frac{1}{n+1} (2^{n+1} C_n)$$

$$\beta = \frac{1}{n+1} \sum_{r=0}^n {}^{n+1} C_{r+1} \cdot {}^{n+1} C_r$$

$$\beta = \frac{1}{n+1} (2^{n+2} C_n)$$

Now $4\beta = 7\alpha$

$$\frac{4}{n+1} (2^{n+2} C_n) = 7 \left(\frac{2^{n+1} C_n}{n+1} \right)$$

$$\frac{4}{n+1} 2^{n+2} C_n = \frac{7}{n+1} 2^{n+1} C_{n+1}$$

$$4 \binom{2n+2}{n+2} = 7$$

$$n = 6$$

22. If the domain of $f(x) = \ln \left(\frac{2x+3}{4x^2-x-3} \right) + \cos^{-1} \left(\frac{2x+1}{x+2} \right)$ is (α, β) find $5\alpha - 4\beta$.

(1) -2

(2) 2

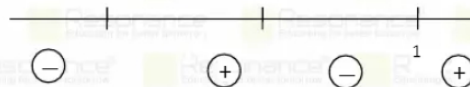
(3) 4

(4) -4

Ans. (1)

Sol. For $\ln \left(\frac{2x+3}{4x^2-x-3} \right)$ to be defined

$$\frac{2x+3}{4x^2-x-3} > 0 \Rightarrow \frac{(2x+3)}{(4x+3)(x-1)} > 0$$



$$x \in \left(-\frac{3}{2}, -\frac{3}{4} \right) \cup (1, \alpha)$$

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PAGE # 9

for $\cos^{-1}\left(\frac{2x+1}{x+2}\right)$ to be defined

$$-1 \leq \frac{2x+1}{x+2} \leq 1 \Rightarrow \frac{3(x+1)}{x+2} \geq 0 \text{ \& \ } \frac{x-1}{x+2} \leq 0 \Rightarrow x \in [-1, 1] \dots(2)$$

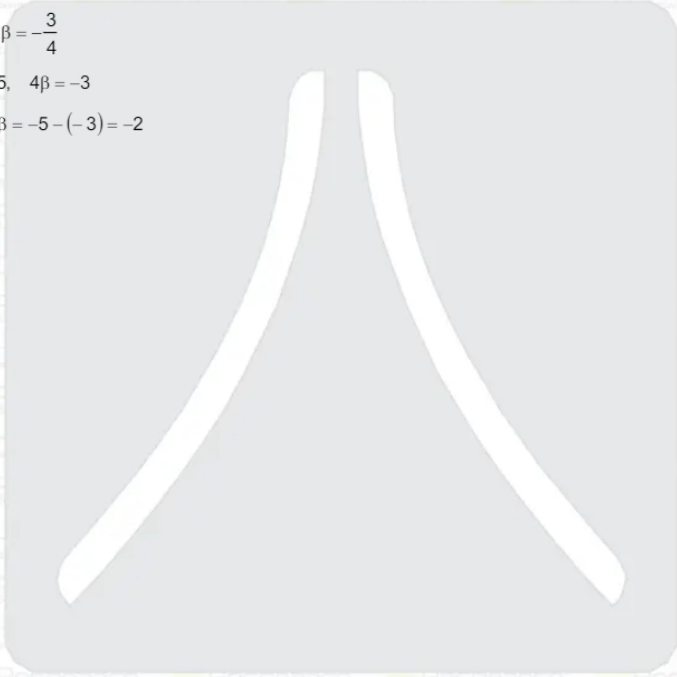
(1) \cap (2)

$$x \in \left[-1, -\frac{3}{4}\right]$$

$$\alpha = -1, \beta = -\frac{3}{4}$$

$$5\alpha = -5, \quad 4\beta = -3$$

$$5\alpha - 4\beta = -5 - (-3) = -2$$



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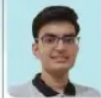
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